

Silk damping at early times: spectral distortion, BBN, and small scale fluctuations

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references: [1306.5751](#), [1403.3697](#)

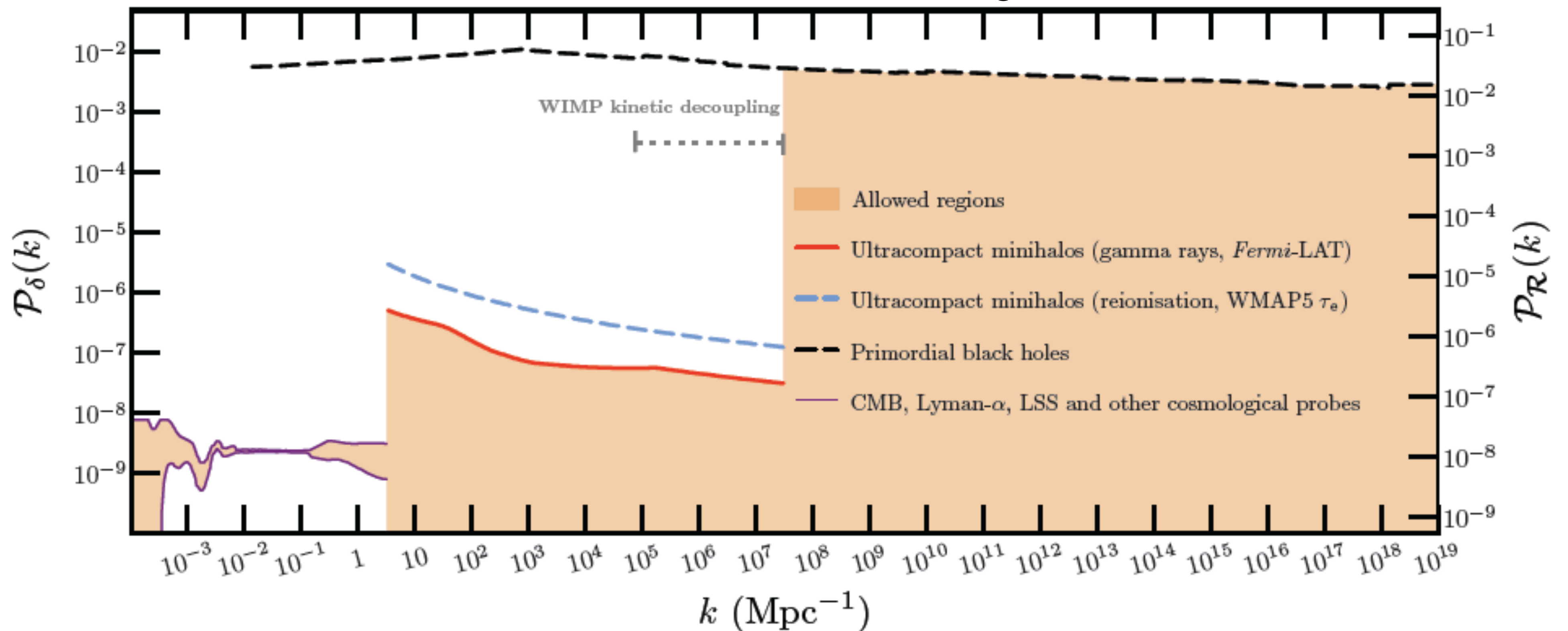
Collaborators: Jens Chluba, Josef Pradler, Marc Kamionkowski (JHU)

CosKASI Conference
17 April 2014

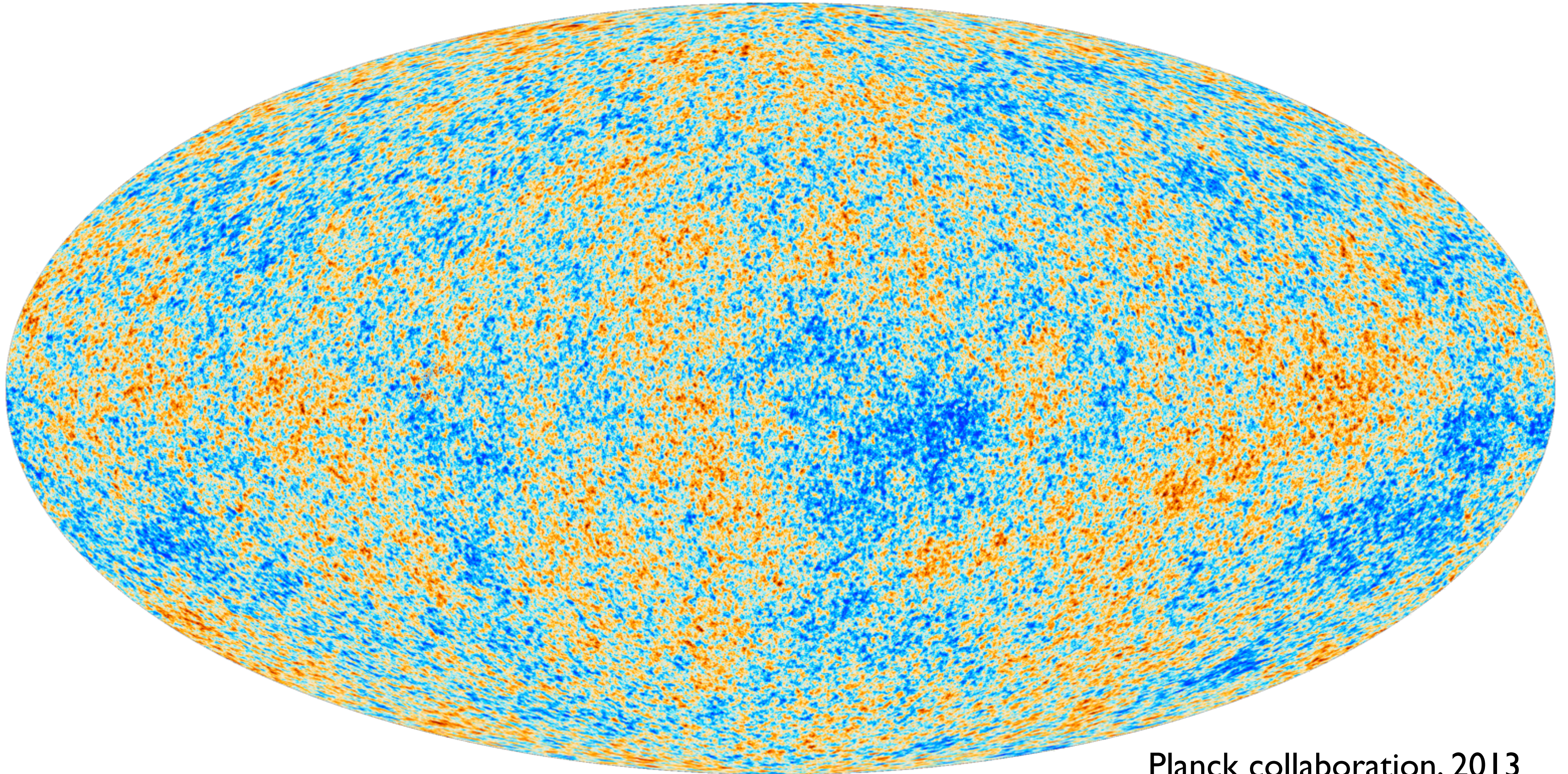
Primordial power spectrum

- is rather unconstrained on small scales ($k \gtrsim 1 \sim 3 \text{ Mpc}^{-1}$)!
- Where else can we look at to put other constraints?

Bringmann, Scott & Akrami 2011

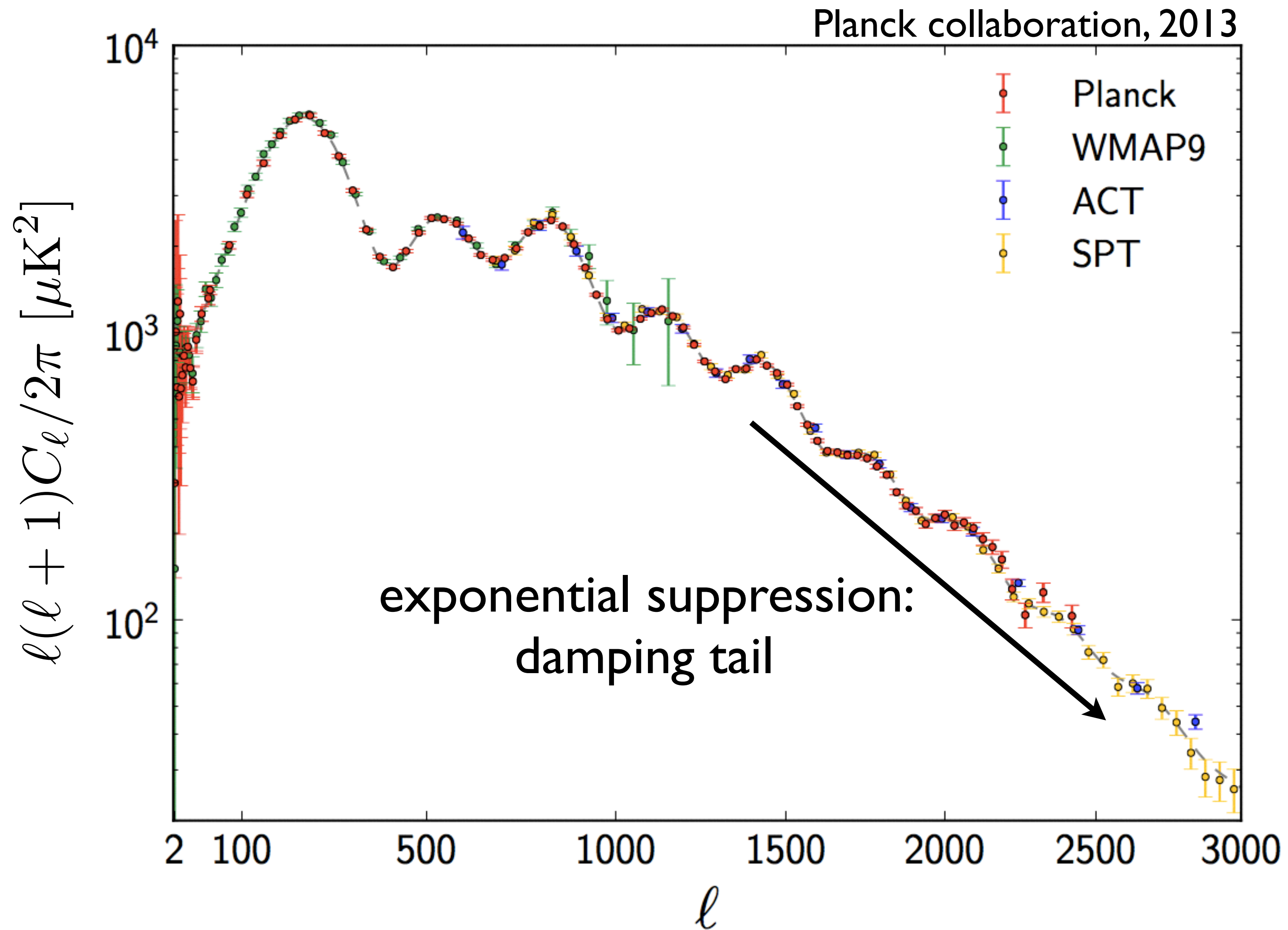


CMB temperature anisotropies

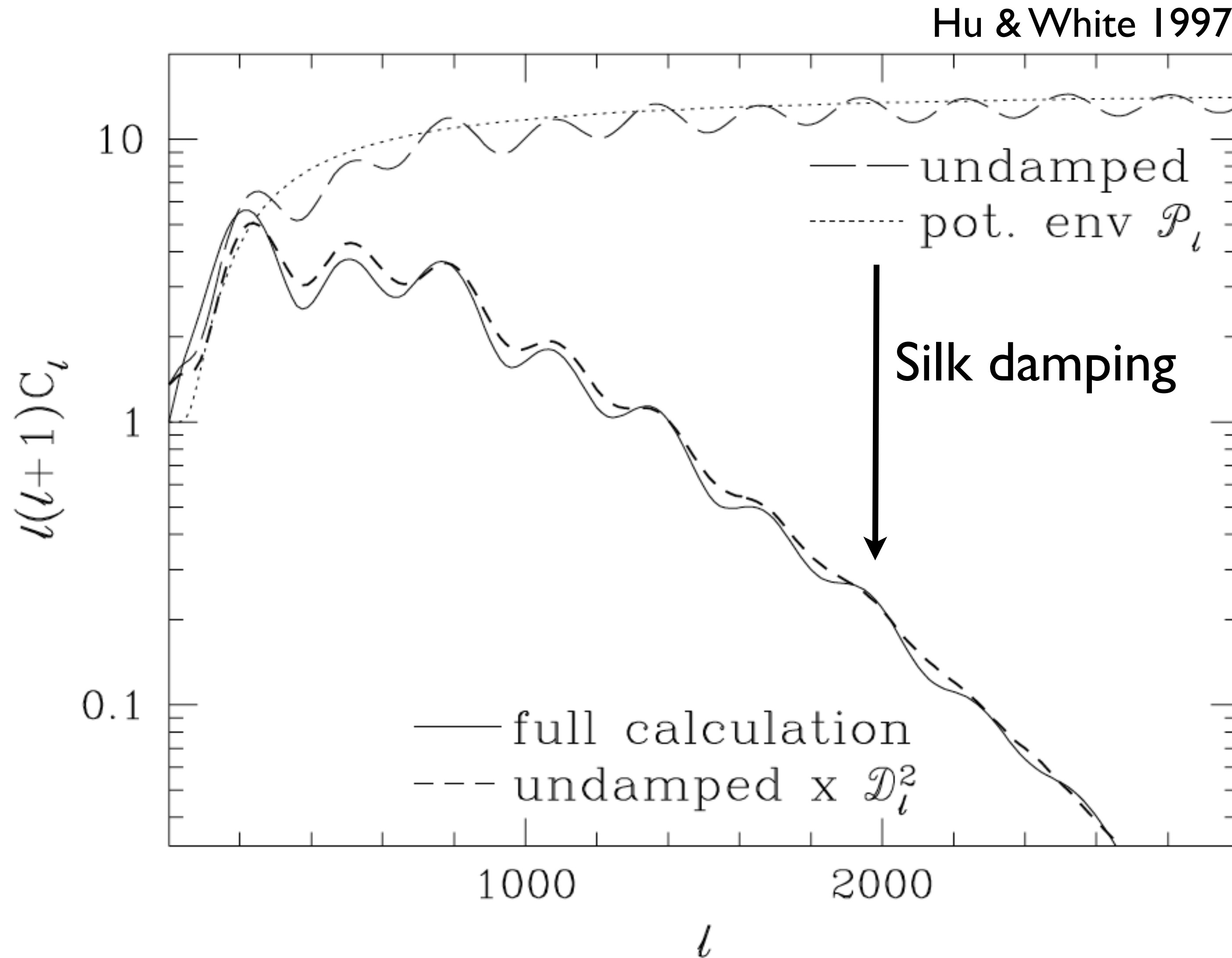


Planck collaboration, 2013

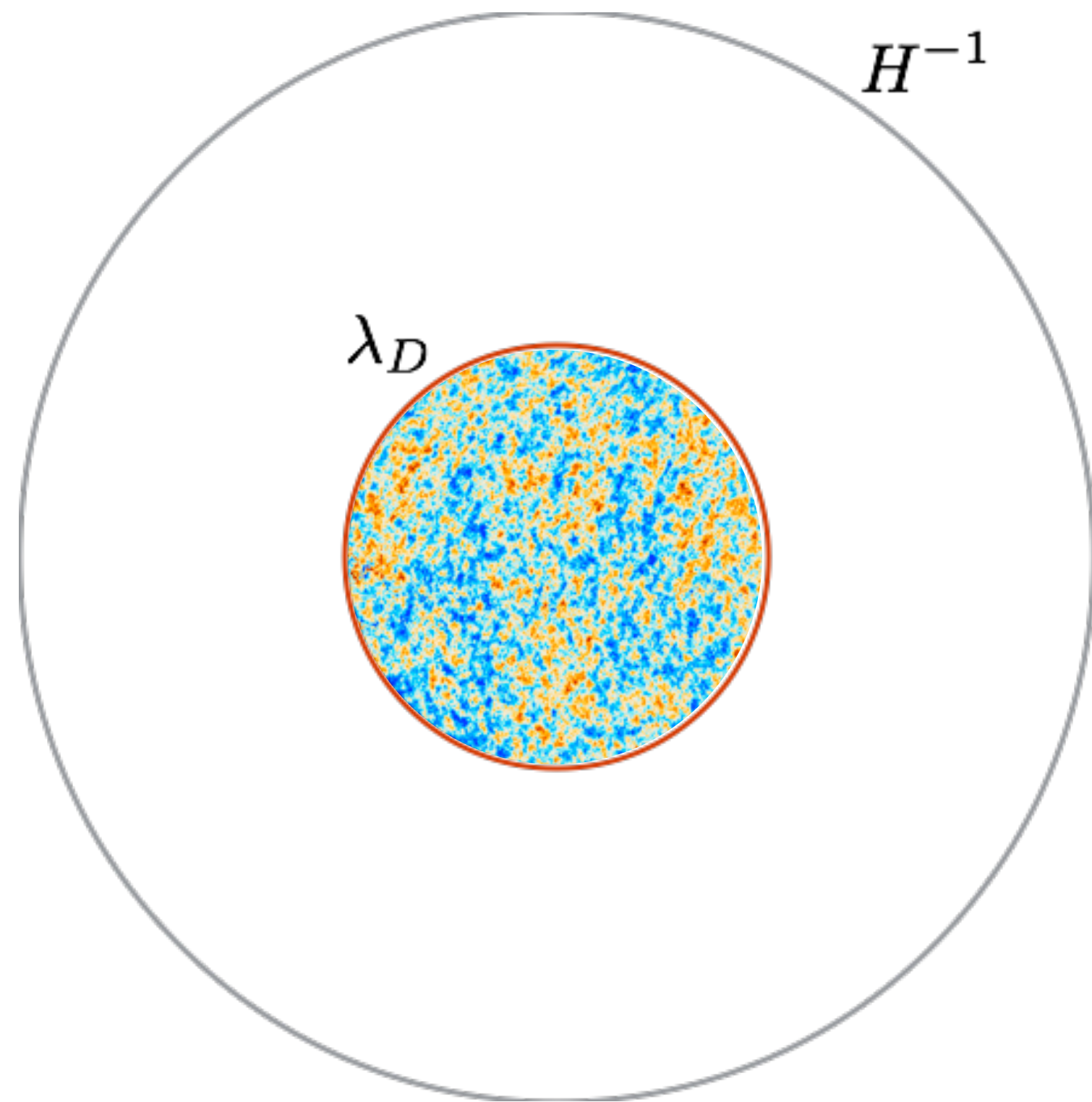
CMB power spectrum C_ℓ



Why call it a damping tail?



Silk damping: diffusion of photon



temperature anisotropies
at $\sim 0.0001''$ scale

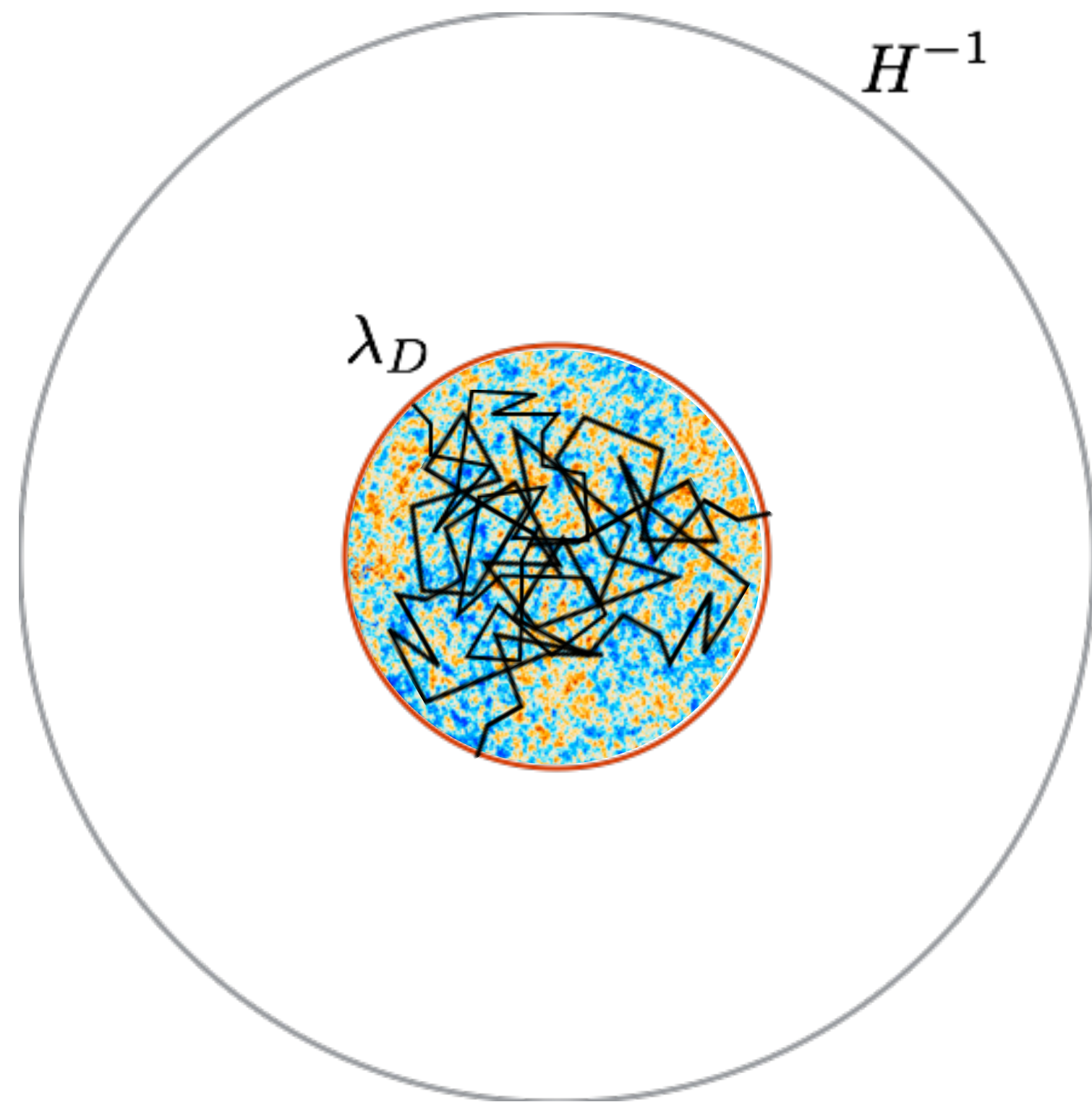
mean free path: $\lambda_{\text{mfp}} \simeq \frac{1}{\sigma_{e\gamma} n_e}$

of scatters: $N \simeq \sigma_{e\gamma} n_e H^{-1}$

diffusion scale (r.m.s. of random walk):

$$\lambda_D \simeq \lambda_{\text{mfp}} \sqrt{N} \simeq \frac{1}{\sqrt{\sigma_{e\gamma} n_e H}}$$

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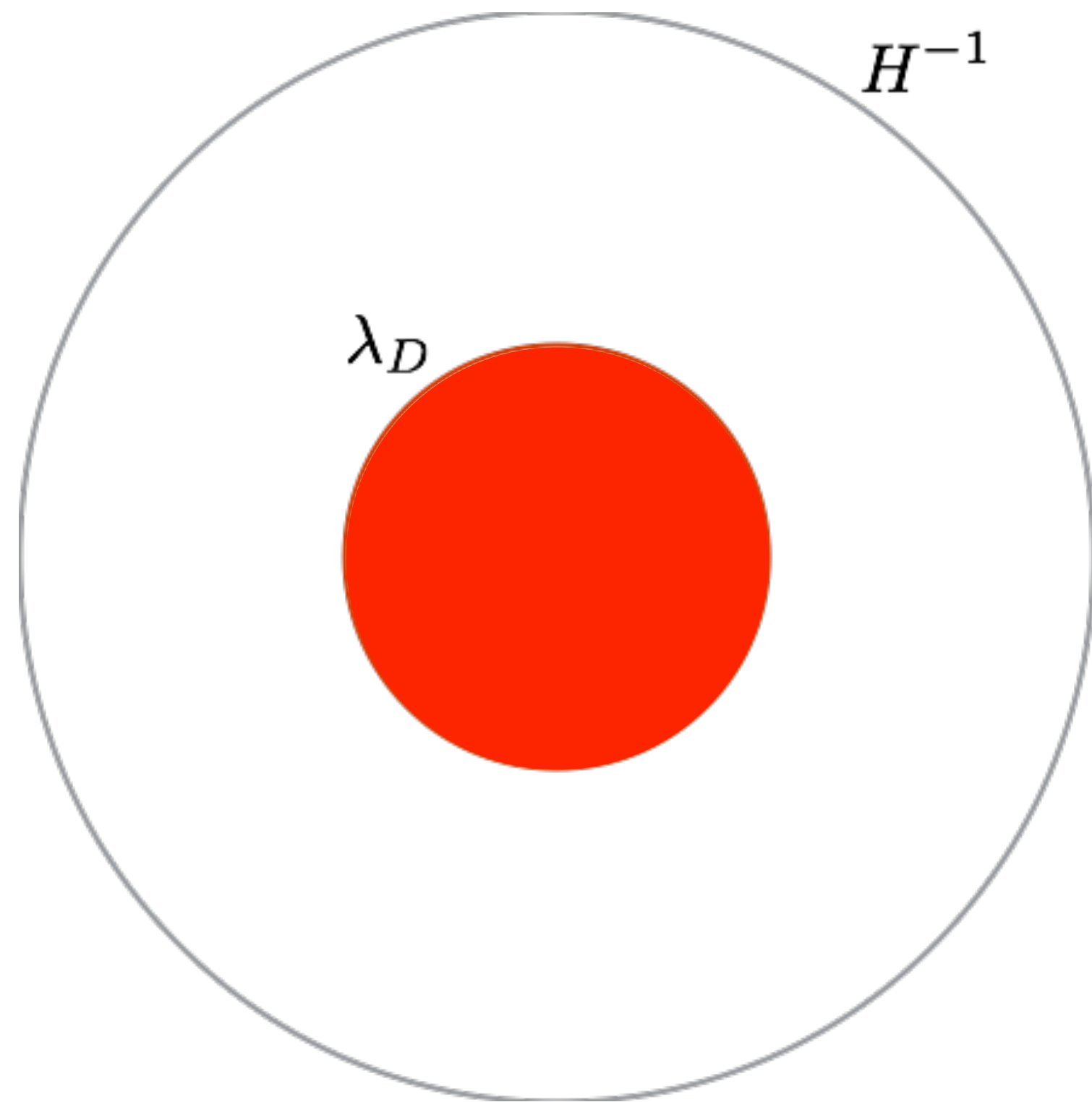
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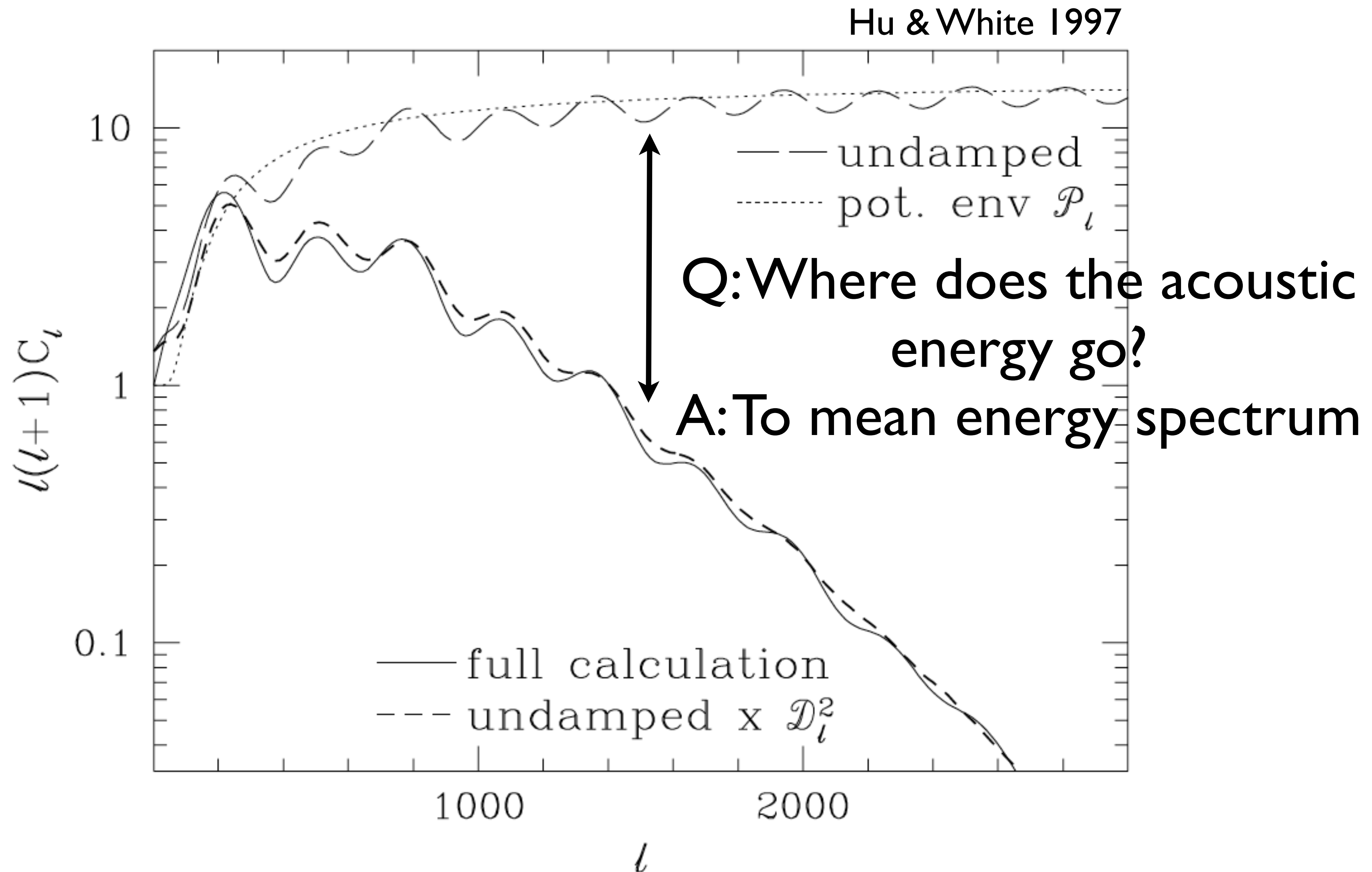
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Temperature fluctuations inside of the diffusion scales are smoothed out!

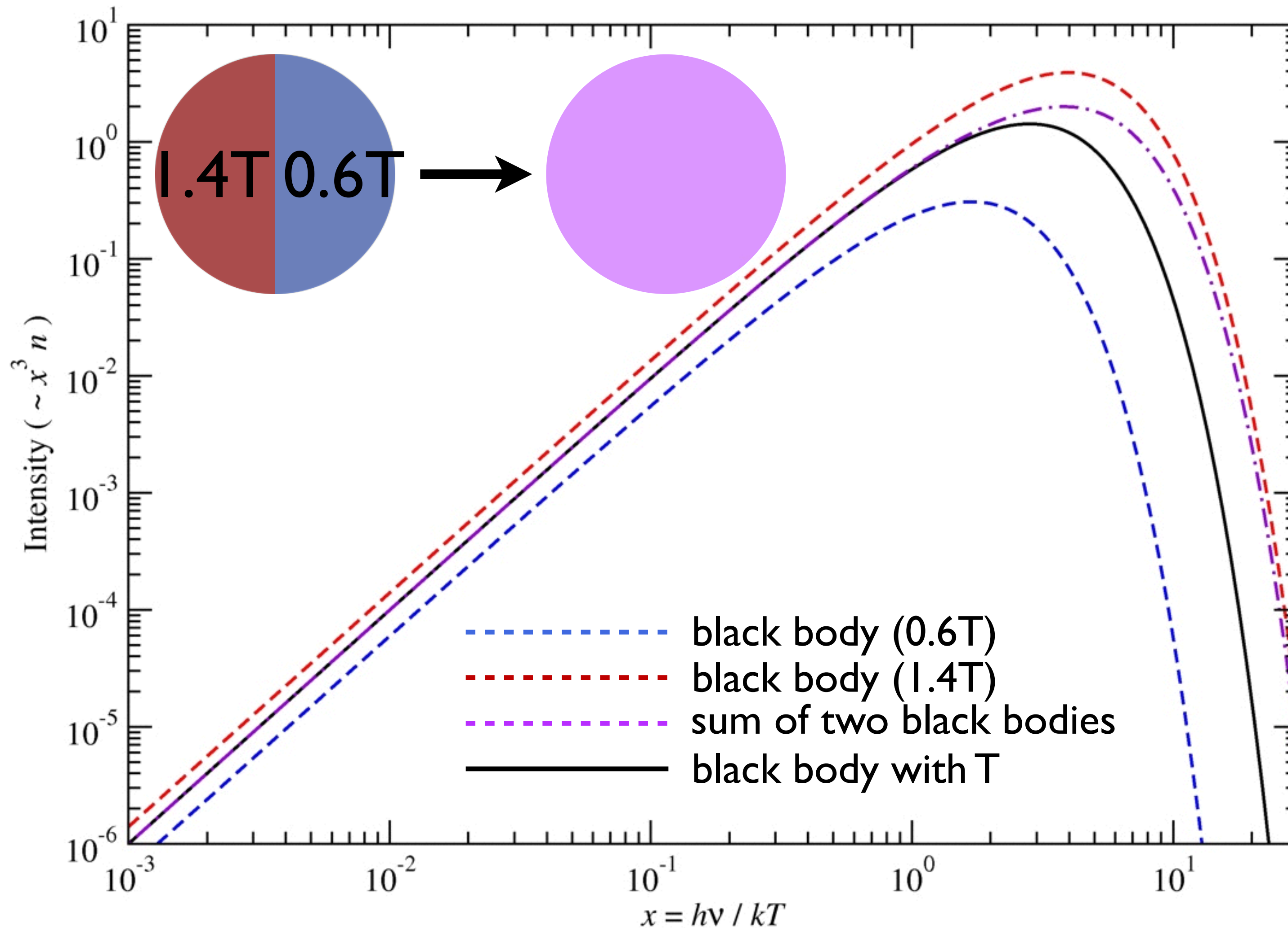
temperature anisotropies
at $\sim 0.0001''$ scale

So, it damps the acoustic waves



Smoothed intensity spectrum

is NOT a black body (Zeldovich, Illarionov & Sunyaev 1972)



Energy and Number density

- Smoothing the black bodies with temperature $T = \bar{T}(1 + \Theta)$
 - superposed energy density $\rho \propto \langle (1 + \Theta)^4 \rangle = \rho(\bar{T})(1 + 6 \langle \Theta^2 \rangle)$
 - superposed number density $n \propto \langle (1 + \Theta)^3 \rangle = n(\bar{T})(1 + 3 \langle \Theta^2 \rangle)$
- Need to *produce* (It is well known that $3/4 \times 6 - 3 = 3/2$.)

$$\frac{\Delta n}{n} = \frac{3}{2} \langle \Theta^2 \rangle$$

in order to maintain the black body form:

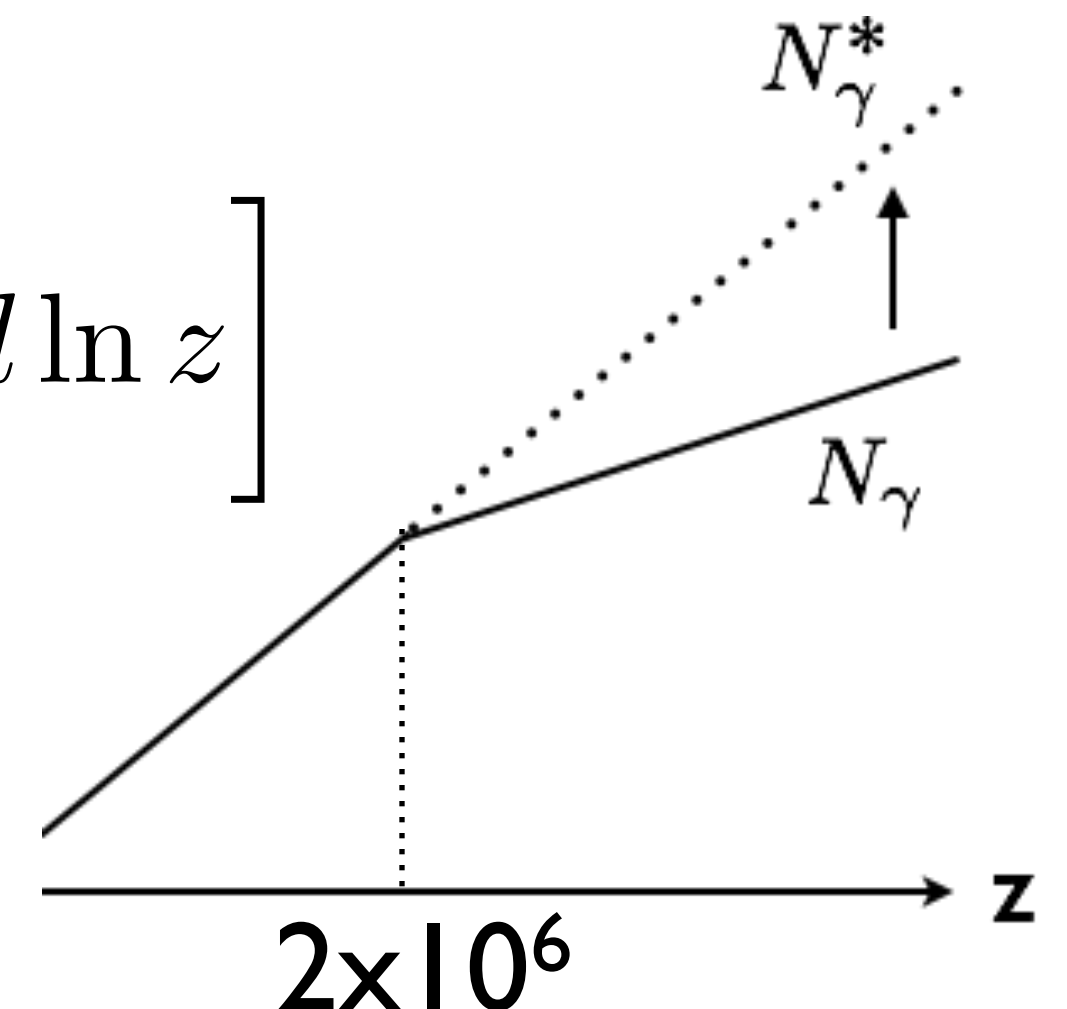
$$\frac{\Delta n}{n} = \frac{3}{4} \frac{\Delta \rho}{\rho}$$

Thermalization at $z \approx 2 \times 10^6$

- Photon (entropy) production due to **double-Compton scattering** and **Bremsstrahlung** + photon transport is efficient
- Thermalization follows immediately after the diffusion process
- Net **entropy production** is proportional to **the amplitude of primordial power spectrum** ($k_D \sim 1/\lambda_D$):

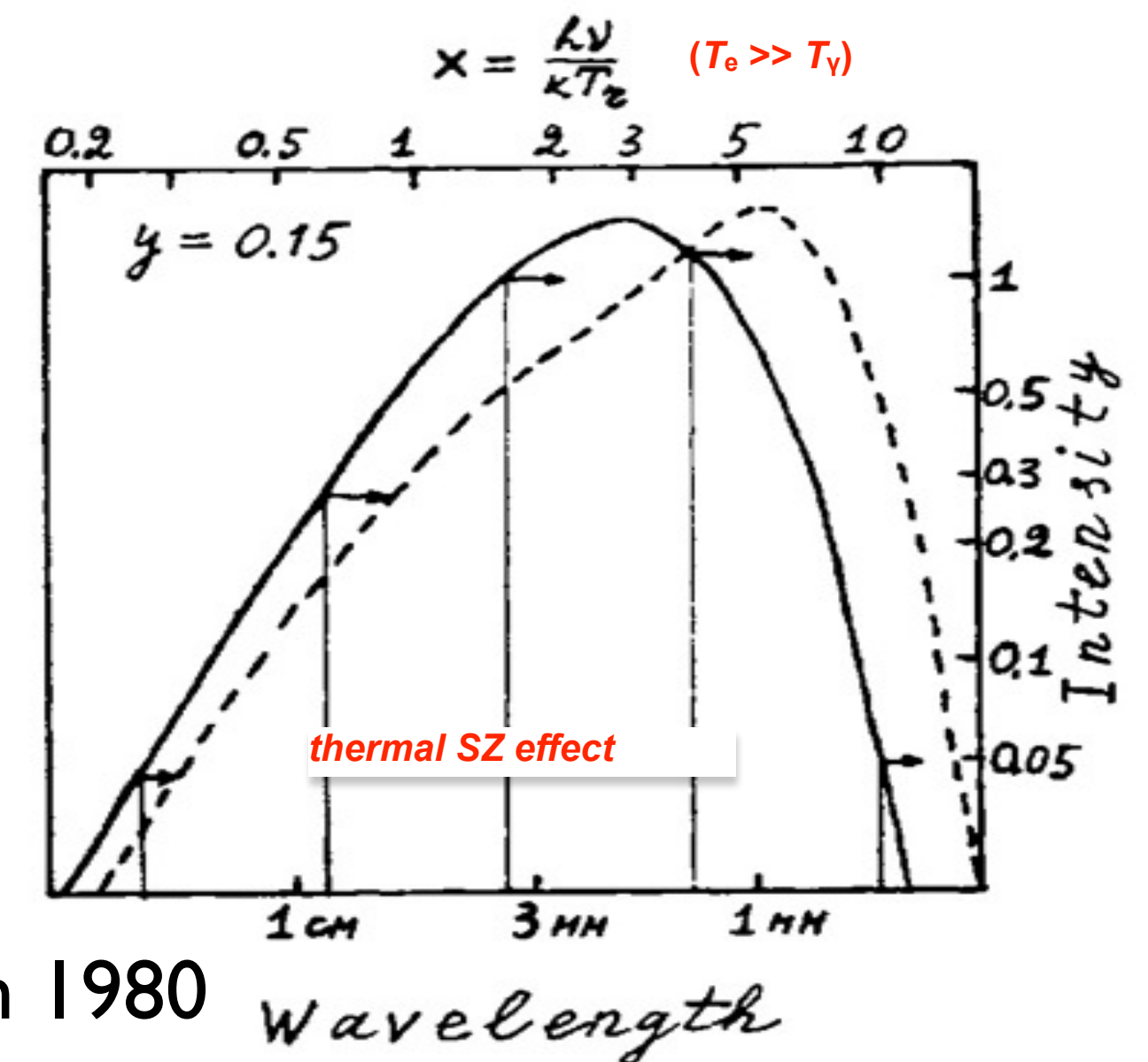
$$N_\gamma(z) \simeq N_\gamma^*(z) \exp \left[-\frac{3}{2} C^2 \int_0^z \Delta_{\mathcal{R}}^2(k_D) \frac{d \ln k_D}{d \ln z} d \ln z \right]$$

↑
number density extrapolated
from 411 cm^{-3} today



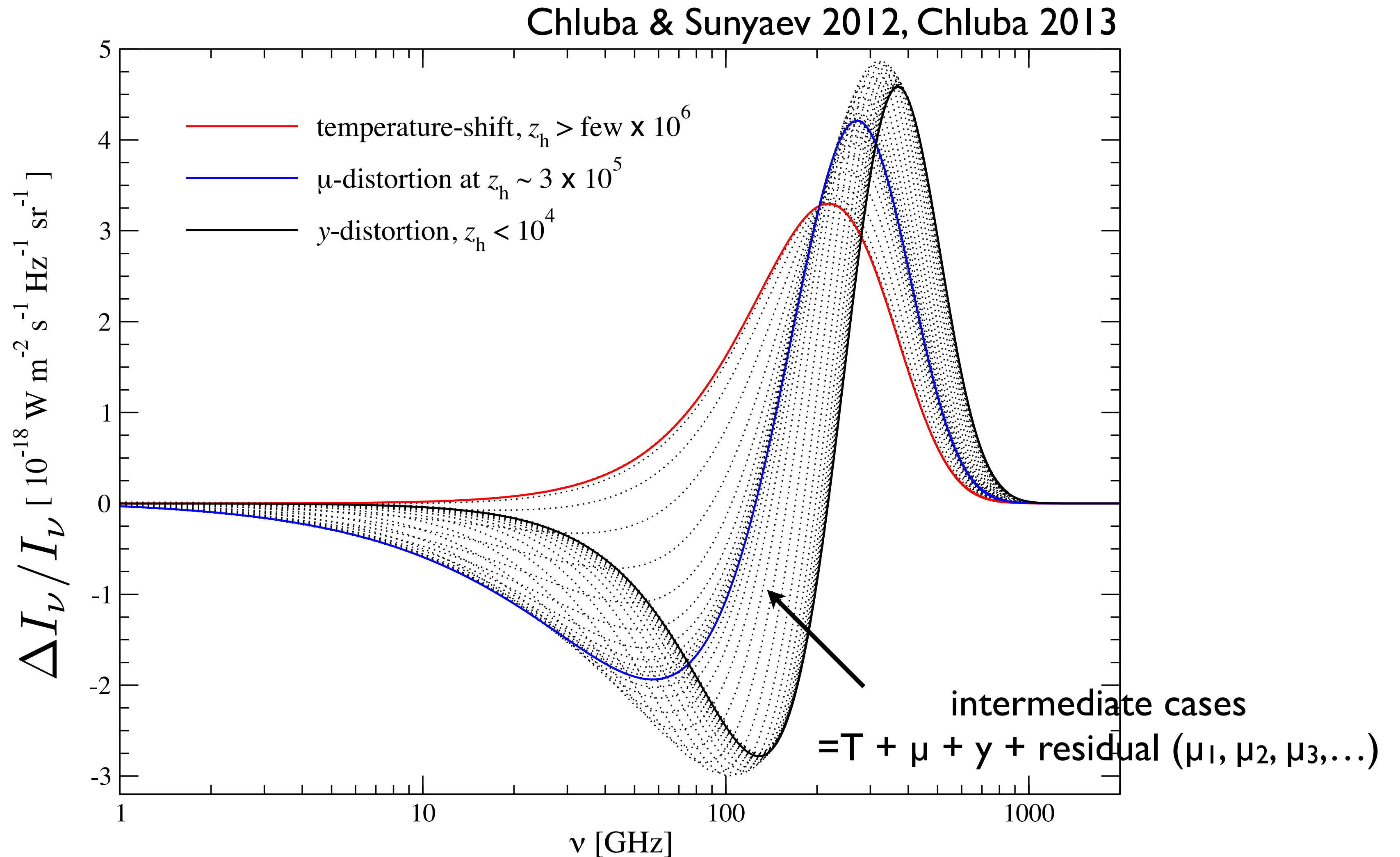
Spectral distortion at $z \lesssim 2 \times 10^6$

- Two extreme cases with excess energy (compared to number)
- At higher redshifts ($z \gtrsim 3 \times 10^5$): μ -distortion
 - Interaction is fast enough to relax the intensity spectrum to the Bose-Einstein form with 'effective' chemical potential
- At lower redshifts ($z \lesssim 10^4$): y -distortion
 - inefficient energy exchange leads to the Compton y -type distortion (a.k.a. thermal SZ effect)

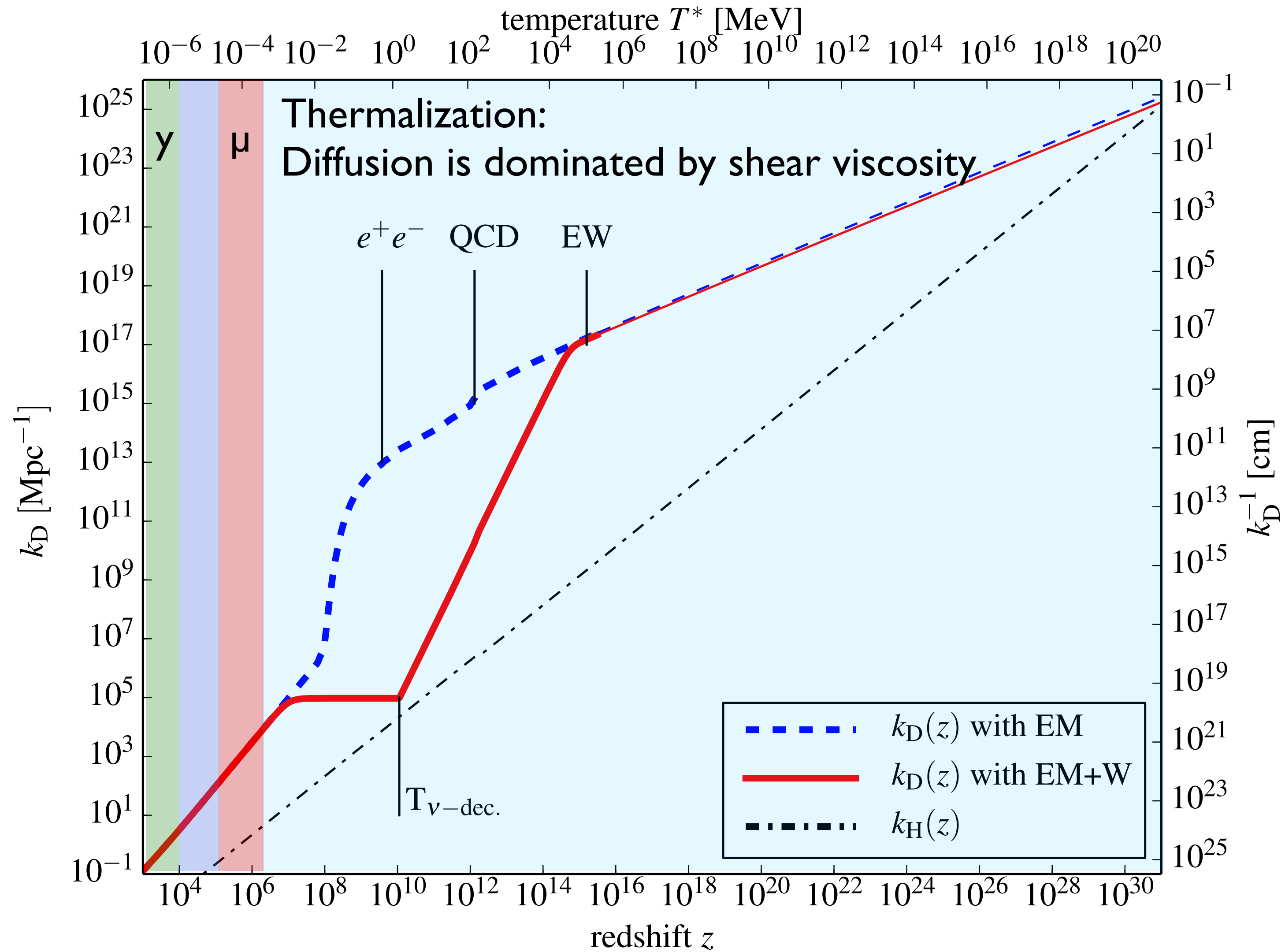


Sunyaev & Zeldovich 1980

How does the distortion look?



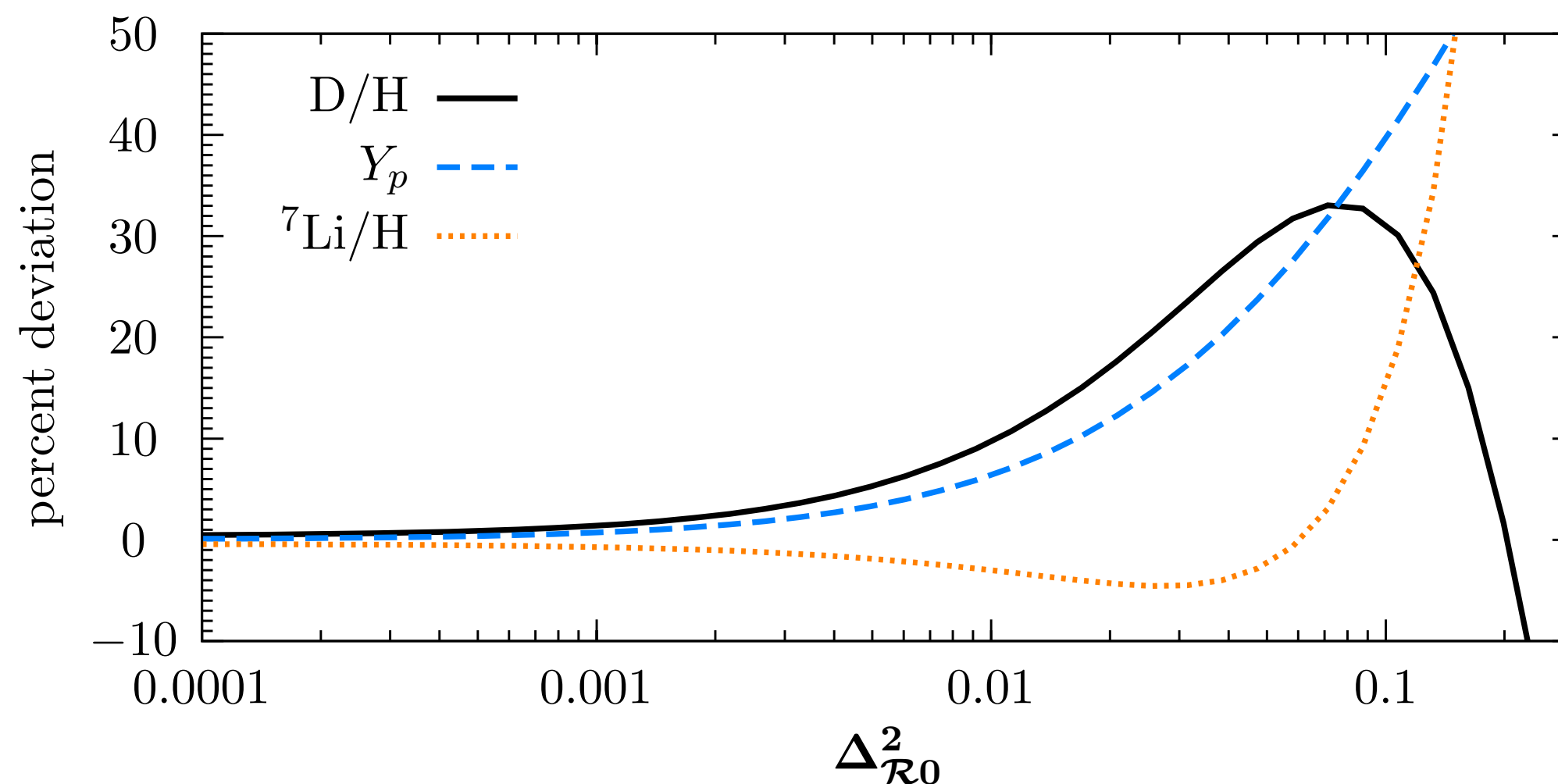
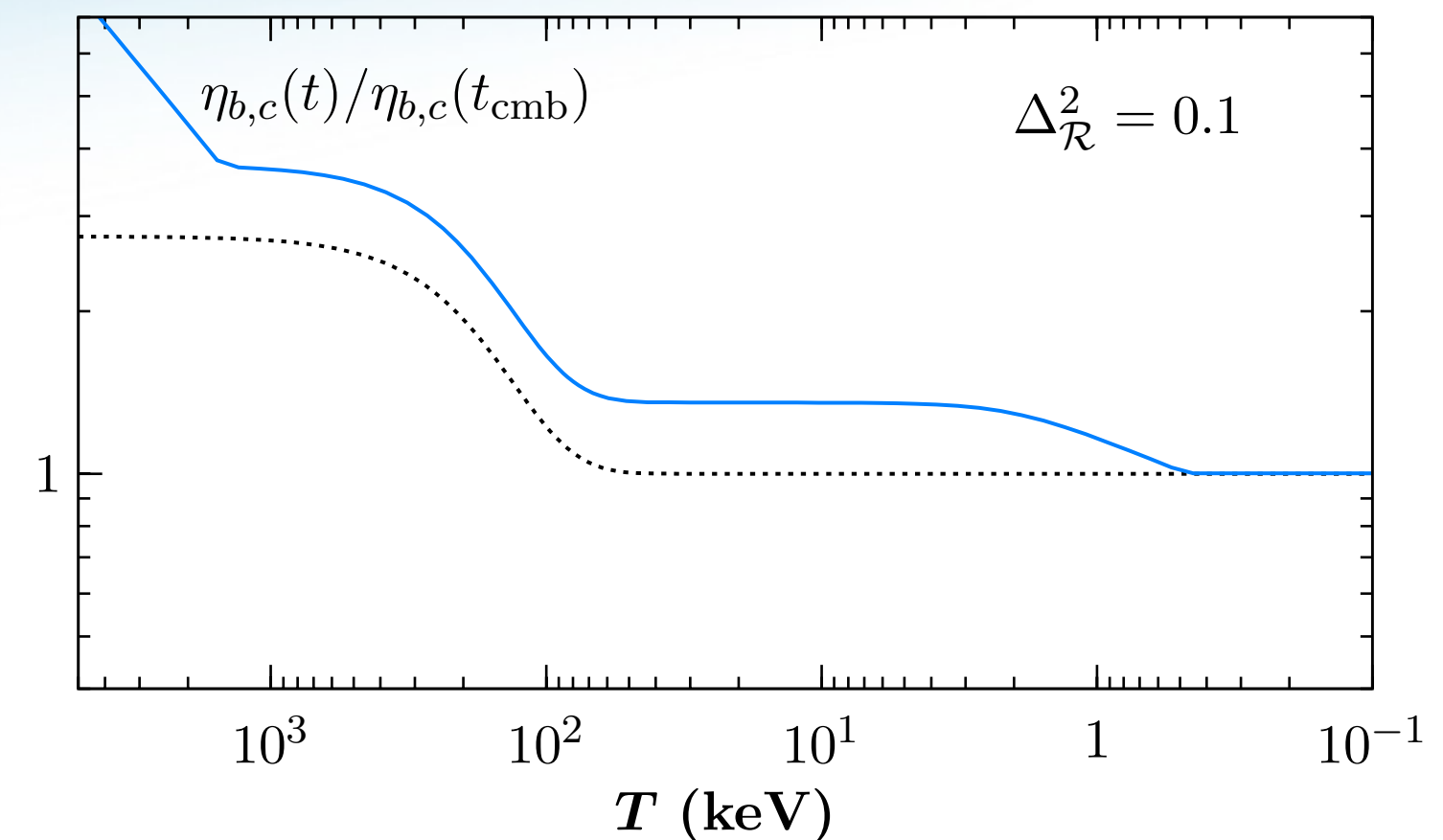
k_D with the Standard Model



Constraint from BBN

Corrections to BBN come from modes that dissipate *after* BBN (present *during* BBN)

=> elevated baryon asymmetry
=> modified avg. energy/particle
(because of the neutrino spectral distortion!)



$$Y_p : \Delta_{\mathcal{R}0}^2 < 0.007$$

$$(D/H)_p : \Delta_{\mathcal{R}0}^2 < 0.2$$

$$10^4 \text{ Mpc}^{-1} \lesssim k \lesssim 10^5 \text{ Mpc}^{-1}$$

only constraint from *direct*
early Universe observable

slide courtesy: Josef Pradler

Constraint from Baryon Asymmetry

Dilution $\frac{\eta_b}{\eta_b^*} = e^{3\Delta_{\mathcal{R}0}^2 \Theta_p}$

If quarks are thermalized,
principal bound:

$$(N_B - N_{\bar{B}})/N_\gamma \lesssim \mathcal{O}(1)$$

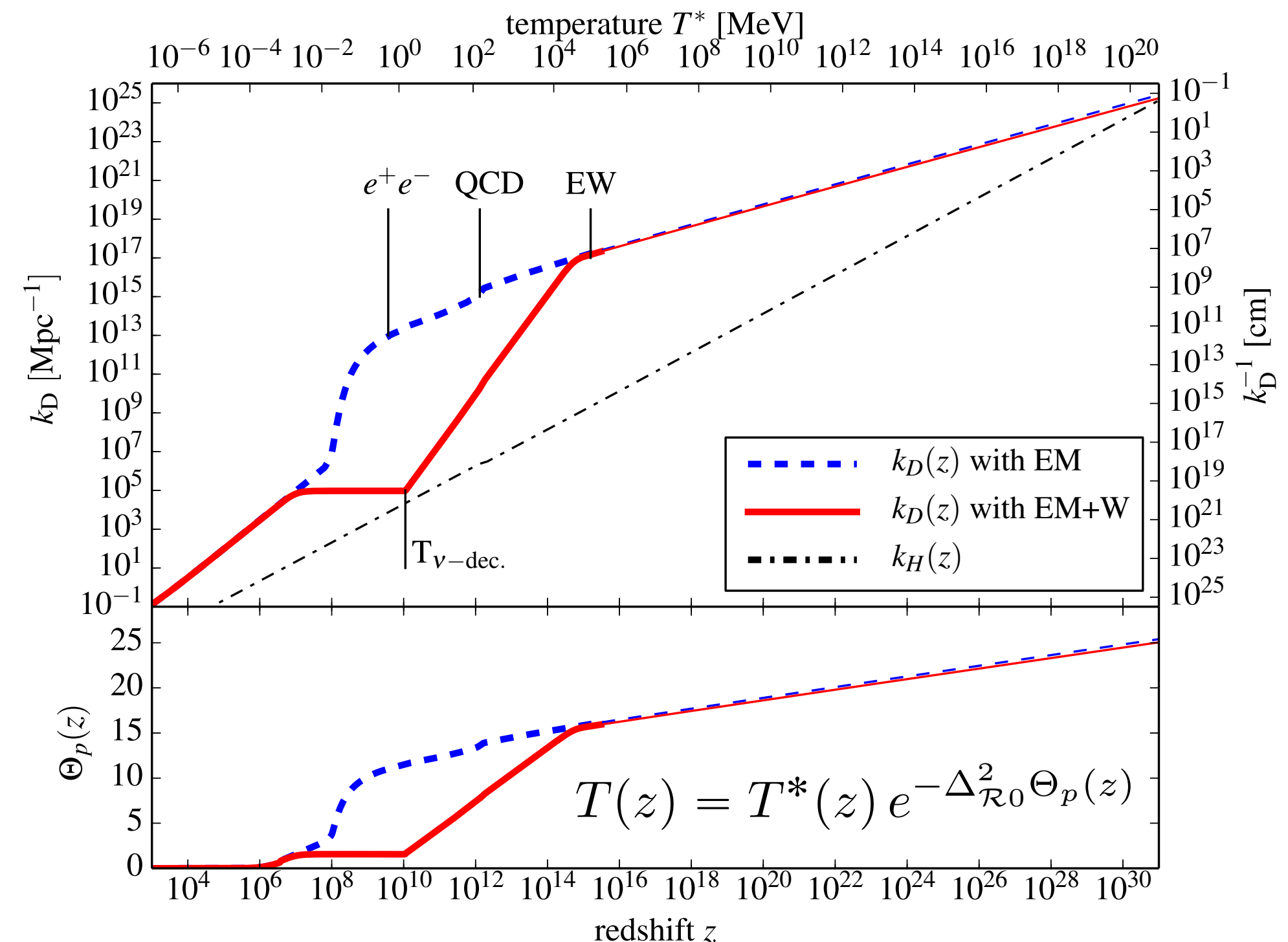
$$\Rightarrow \Delta_{\mathcal{R}0}^2 \lesssim 0.3$$

If baryogenesis happens
above 1 TeV.

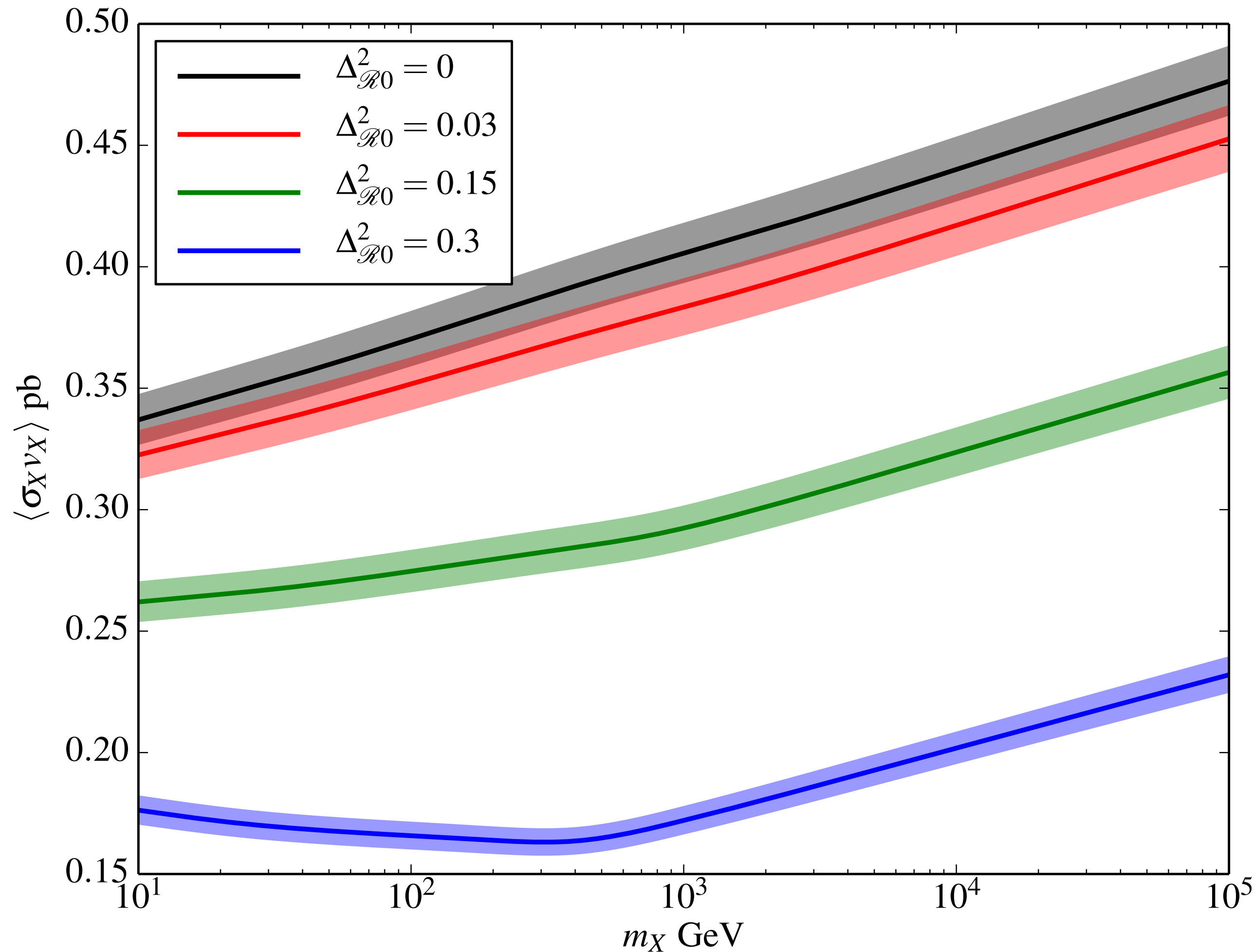
Weak bound, but

1. applies on very small scales
2. dilution factor is substantial

Extrapolation for SM

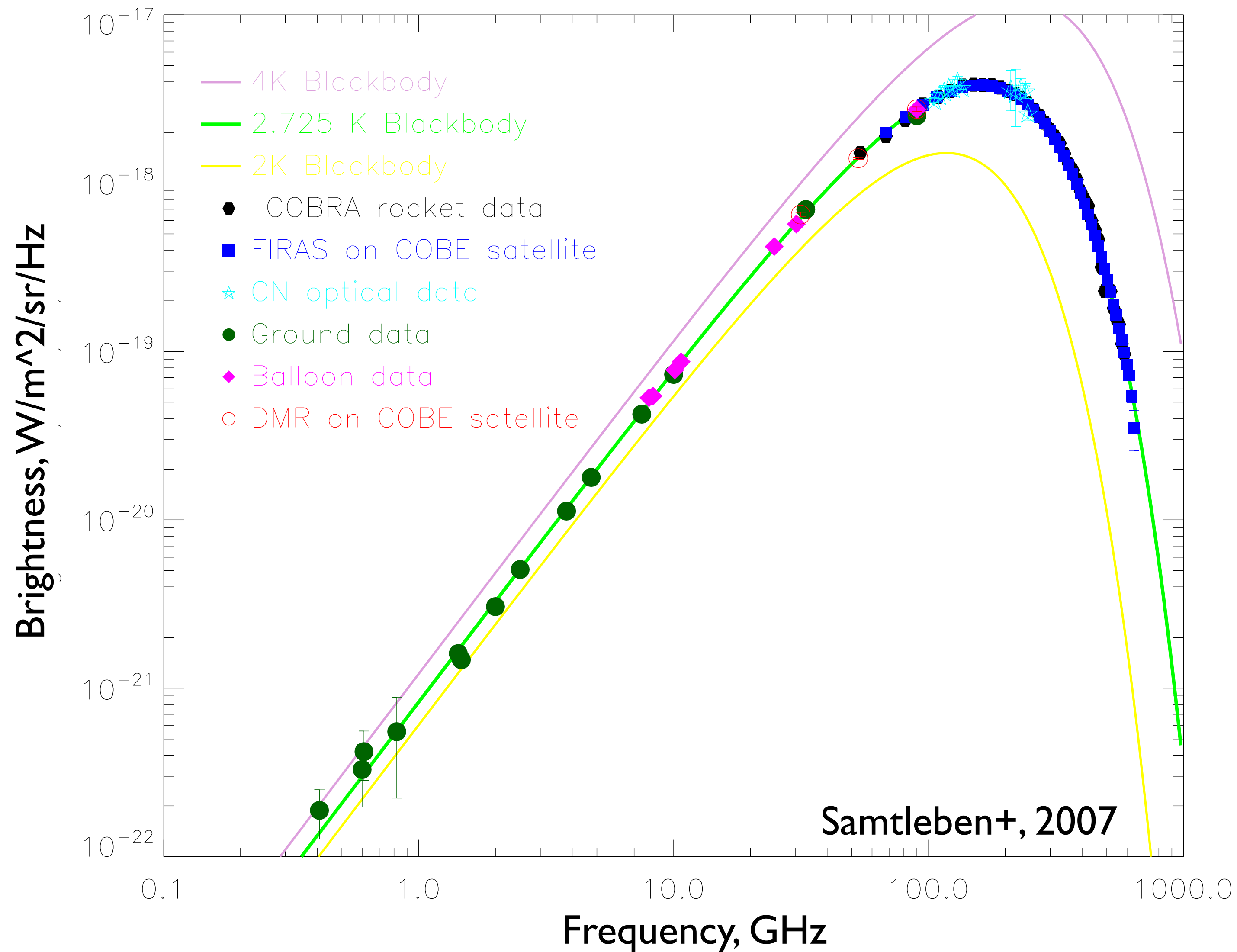


CDM freeze-out (WIMP miracle)



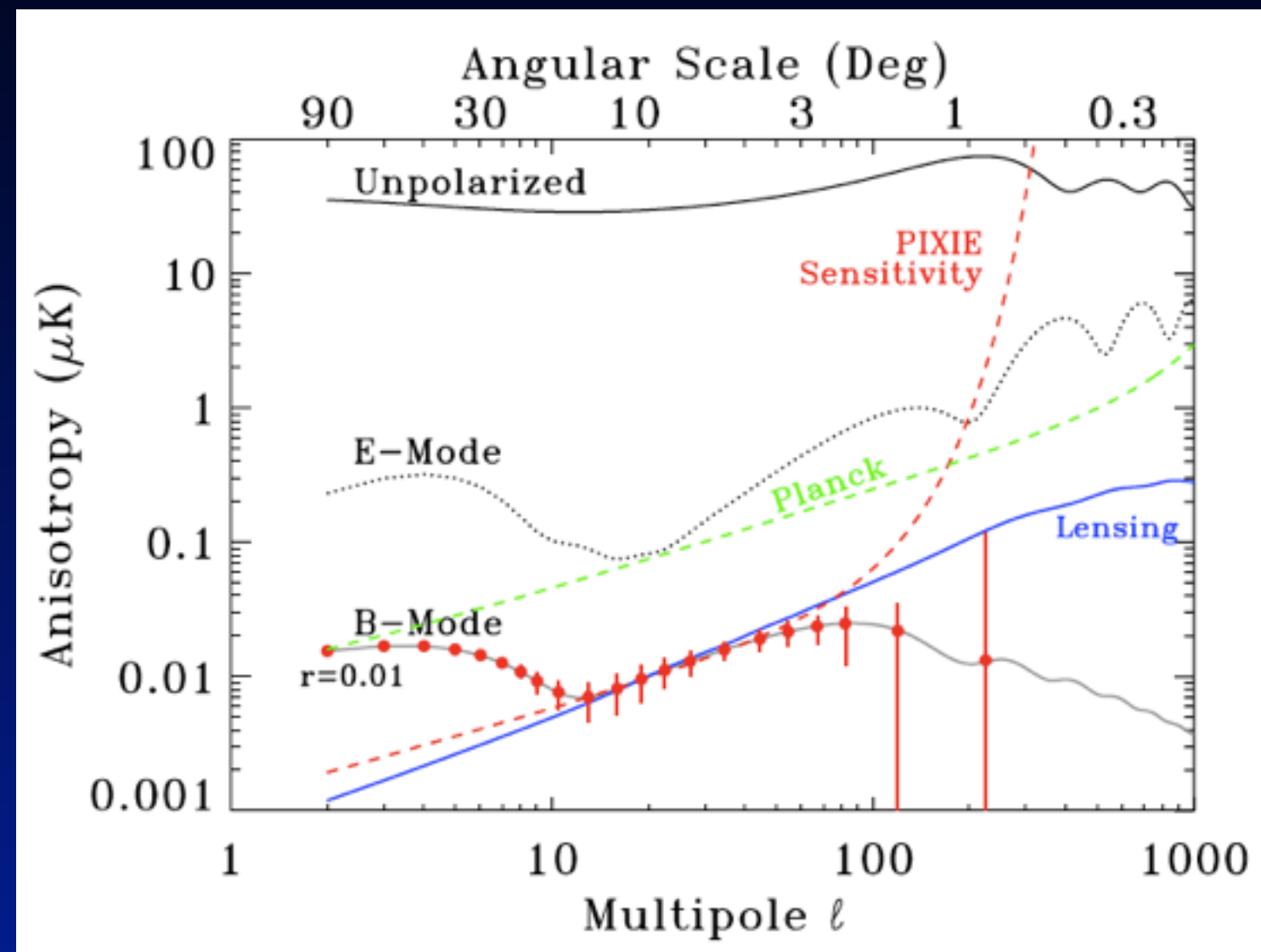
- Effect from revised temperature-redshift relation
- FO density is determined by ‘revised’ CMB temperature
- Shaded region:
 $\Omega_{\text{cdm}} = 0.2594 \pm 0.0074$
(Planck 2- σ)

CMB is very very black-body!

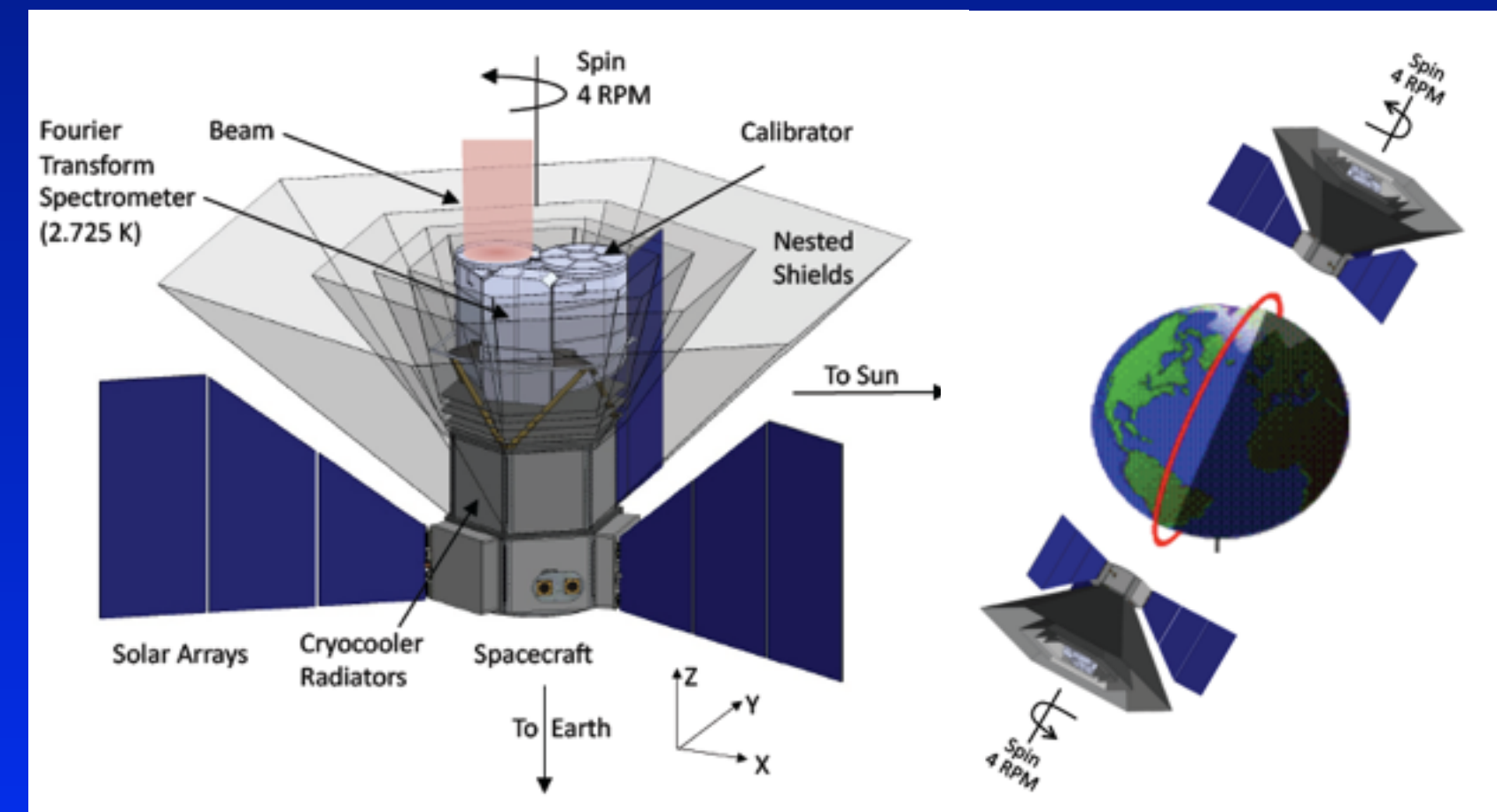
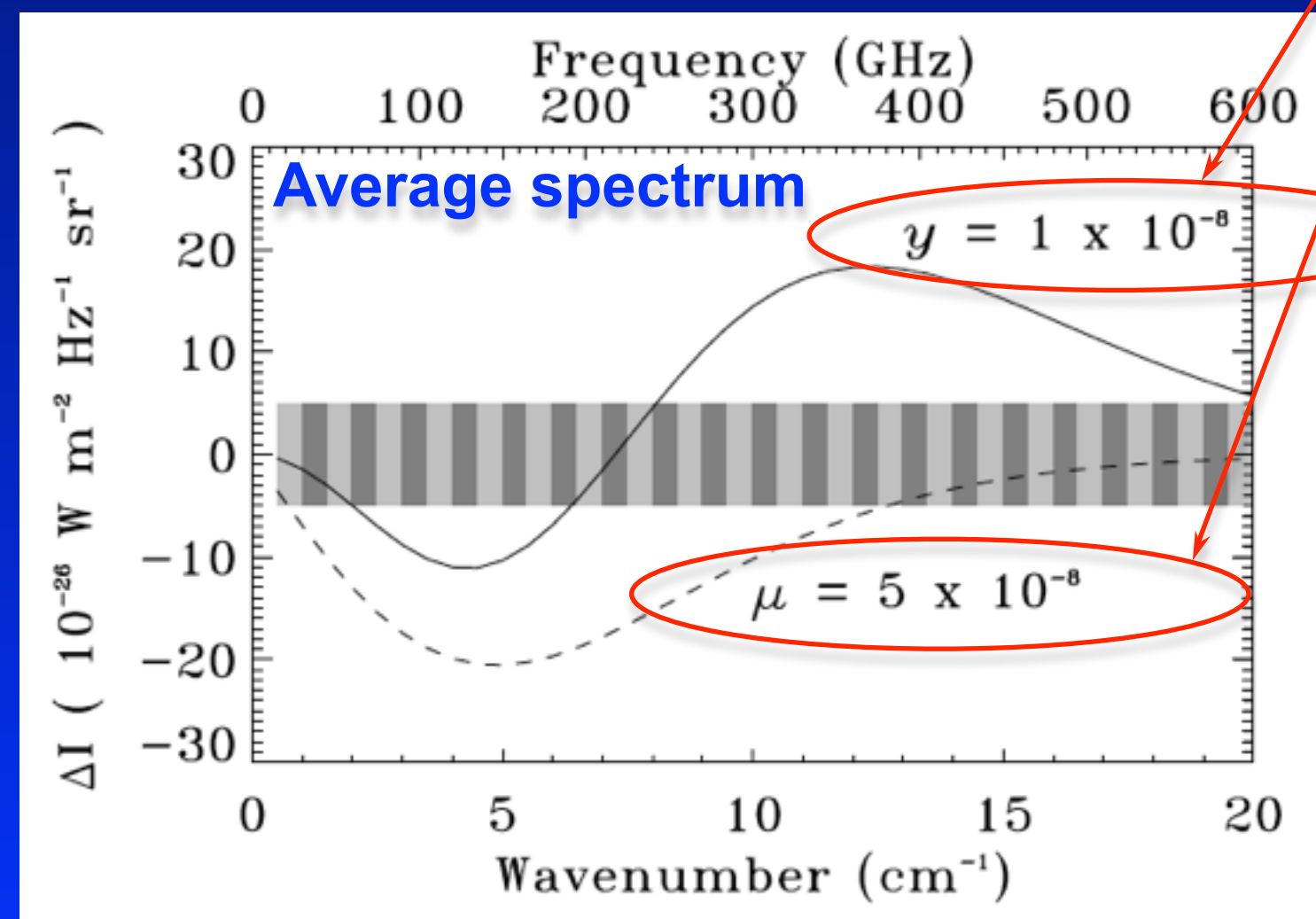


- $T_0 = 2.527 \pm 0.001$ K
from COBE/FIRAS
(Mather+ 1994, Fixen
+ 1996, Fixen+2003)
- $|y| \leq 1.5 \times 10^{-5}$
- $|\mu| \leq 9 \times 10^{-5}$

PIXIE: Primordial Inflation Explorer



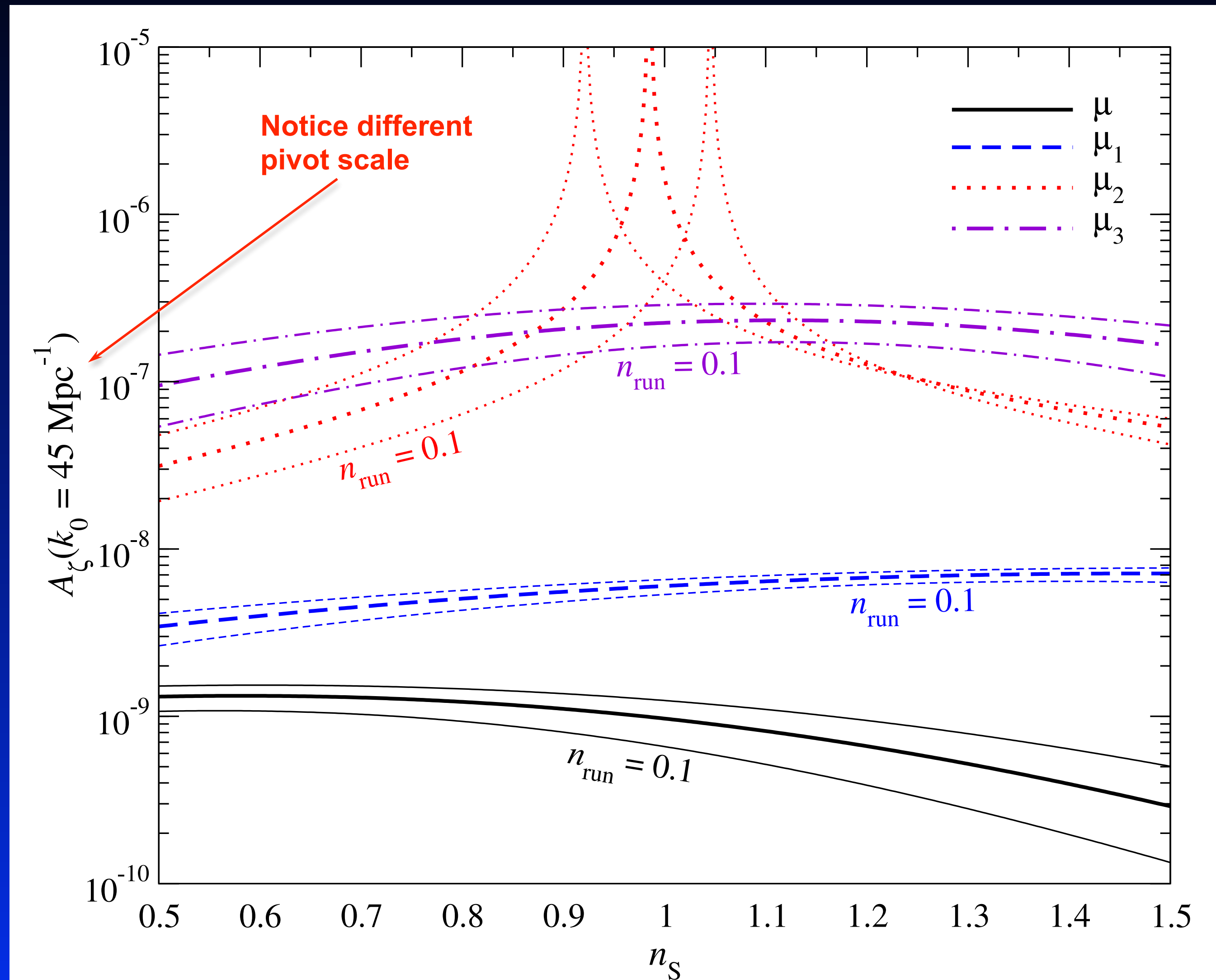
- 400 spectral channel in the frequency range 30 GHz and 6THz ($\Delta\nu \sim 15\text{GHz}$)
- about 1000 (!!!) times more sensitive than COBE/FIRAS
- B-mode polarization from inflation ($r \approx 10^{-3}$)
- improved limits on μ and y
- was proposed 2011 as NASA EX mission (i.e. cost ~ 200 M\$)



Kogut et al, JCAP, 2011, arXiv:1105.2044

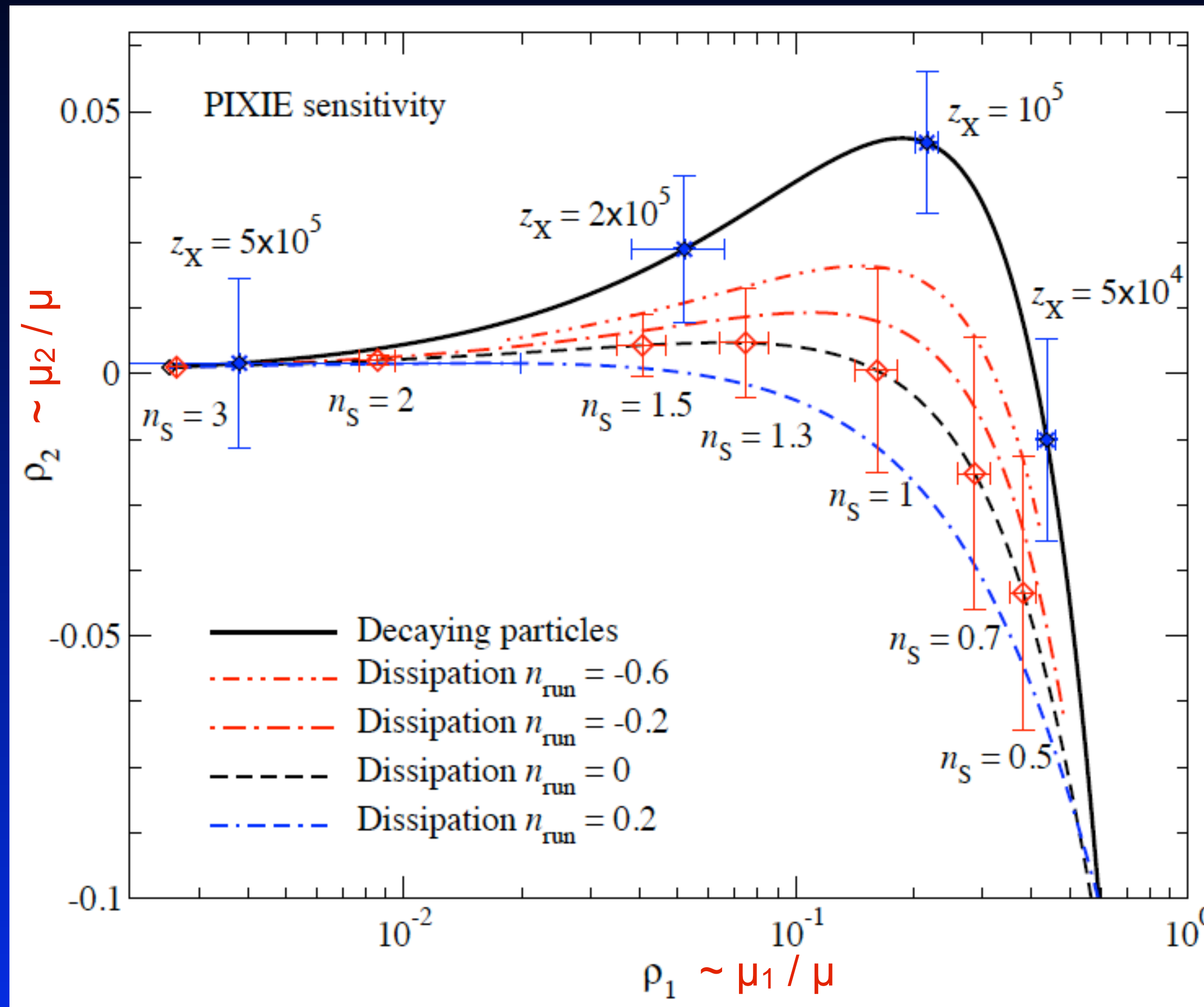
slide courtesy: Jens Chluba

Dissipation scenario: 1σ -detection limits for PIXIE



$$P_\zeta(k) = 2\pi^2 A_\zeta k^{-3} (k/k_0)^{n_S - 1 + \frac{1}{2} n_{\text{run}} \ln(k/k_0)}$$

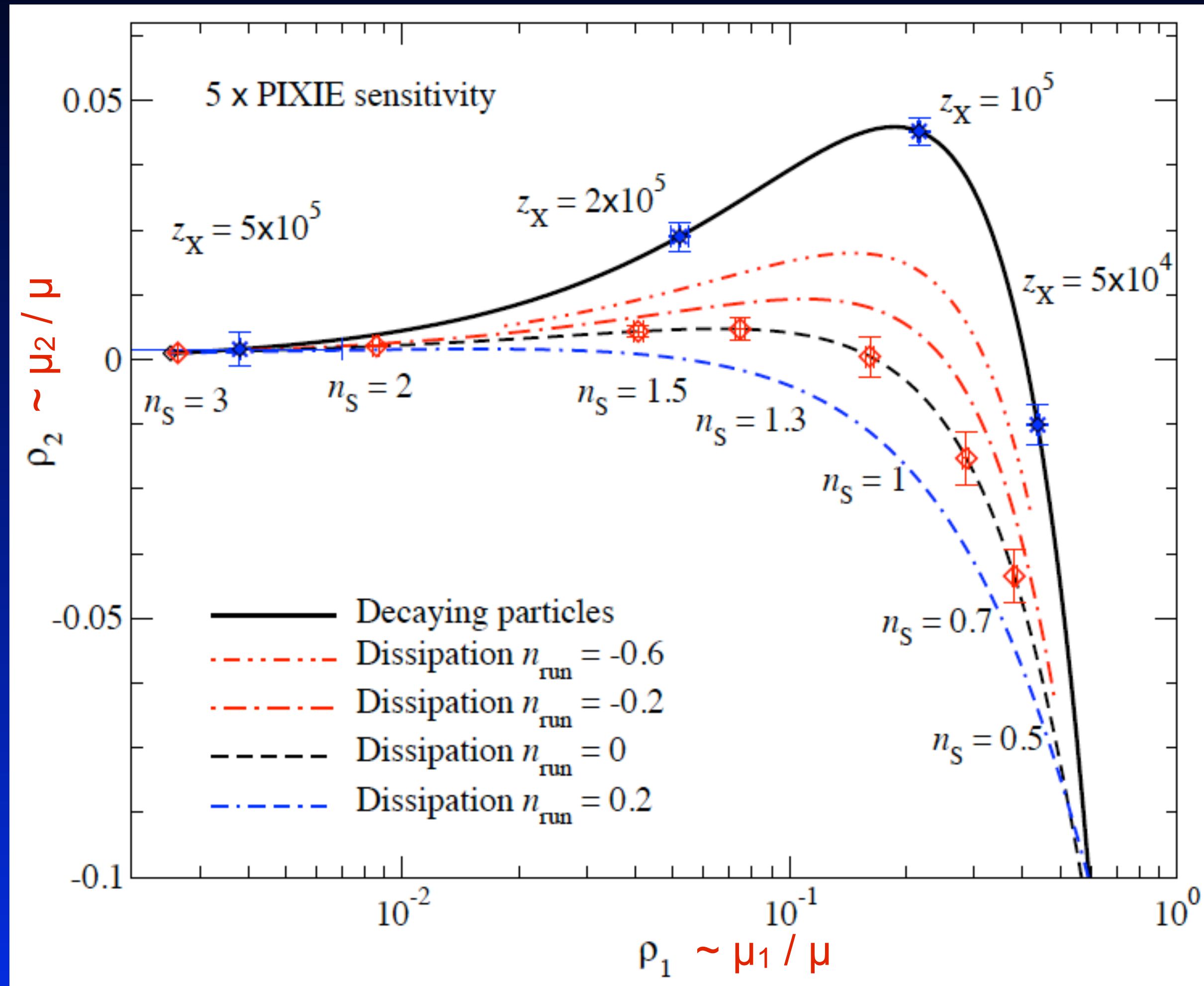
Distinguishing dissipation and decaying particle scenarios



- measurement of μ , μ_1 & μ_2
- trajectories of decaying particle and dissipation scenarios differ!
- scenarios can in principle be distinguished

$$A_\zeta = 5 \times 10^{-8}$$

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Conclusion

- Dissipation of small-scale acoustic modes provides yet another way of constraining primordial power spectrum!
- Here, we provide a new limit only using the standard model of particle physics and cosmology. But, extension beyond the standard model is also trivial.
- The thermal history in the early Universe has to be modified with dissipation. Watch out! Too much small-scale power will spoil your thermal history.
- Future CMB spectral distortion measurement (e.g. PIXIE, COrE+) will put a tighter constraint on $10 < k < 10^4 \text{ Mpc}^{-1}$.