

# Three Themes on Dark Energy

Federico Piazza



# Nobel Prize in Physics 2011



Photo: Roy Kaltschmidt. Courtesy:  
Lawrence Berkeley National Laboratory

**Saul Perlmutter**



Photo: Belinda Pratten, Australian  
National University

**Brian P. Schmidt**



Photo: Homewood Photography

**Adam G. Riess**

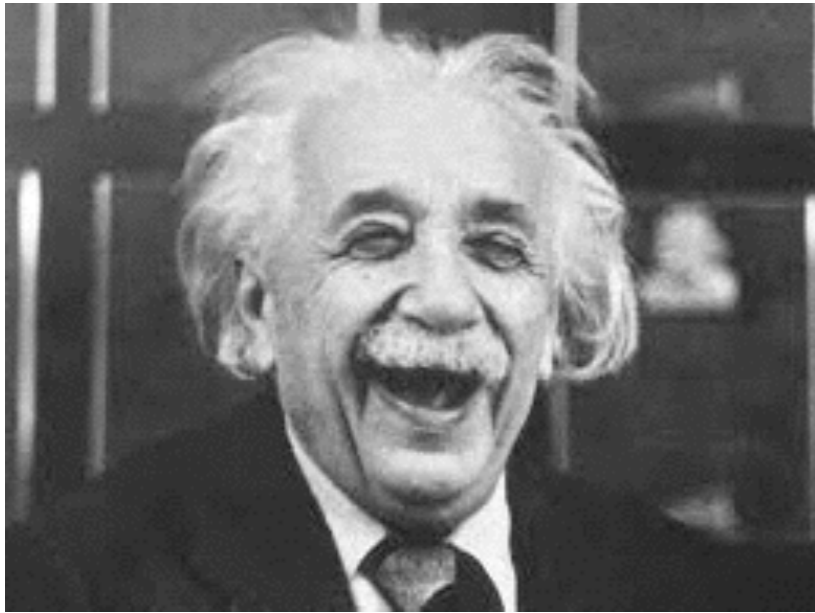
The Universe is accelerating!

Why?!



# The three themes:

- Dark energy and modified gravity: a more **systematic** approach...?
- The **EFT** of dark energy (at work!)
- Modified gravity effects that **pierce the screen**



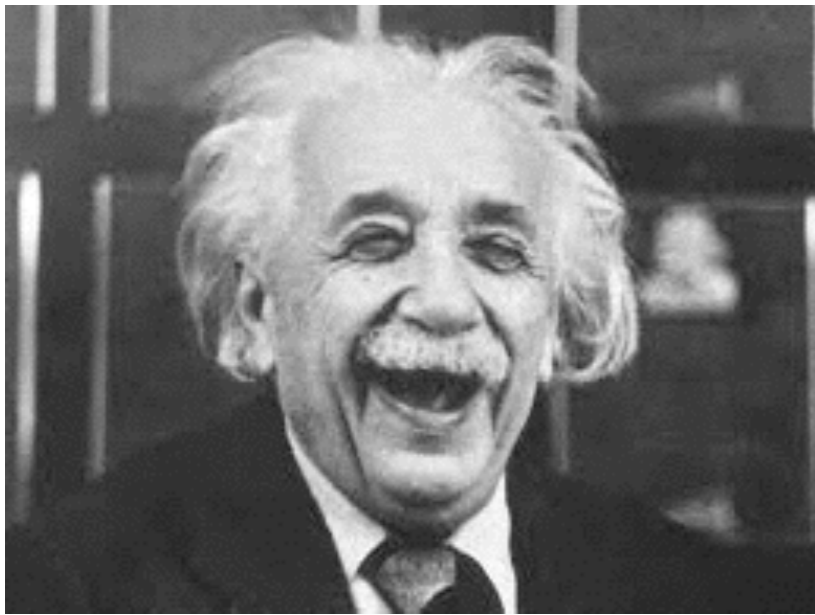
$\Lambda$ CDM



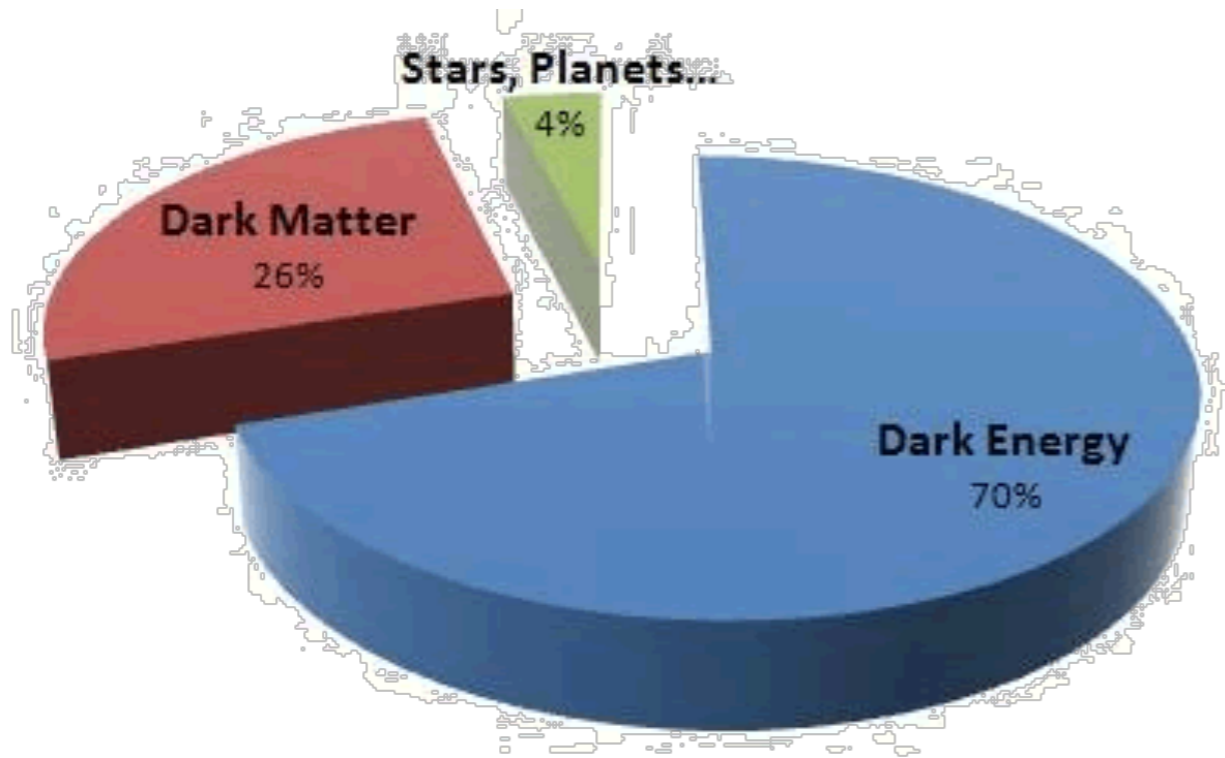
$g_{\mu\nu} + \text{STUFF}$



Other fundamental ingredients?

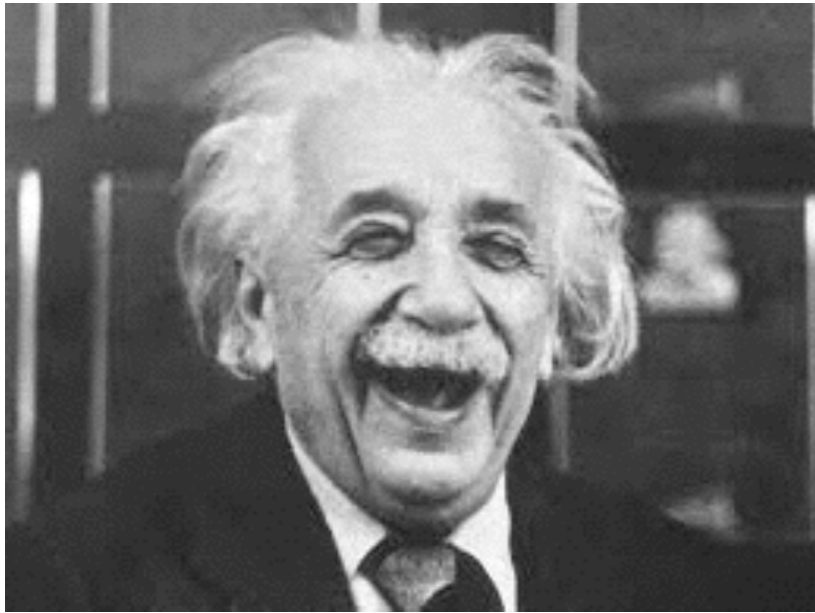


$\Lambda$ CDM



$$\Lambda \sim (10^{-3} eV)^4$$

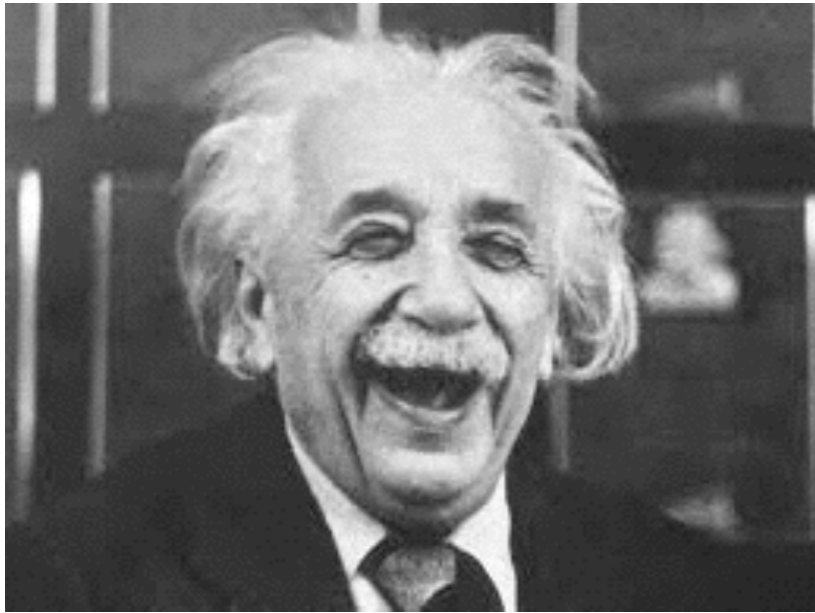
$\Lambda$ CDM cosmology



$\Lambda$ CDM

The only consistent  
low energy theory for  
a massless spin-two field  $g_{\mu\nu}$ .





$\Lambda$ CDM

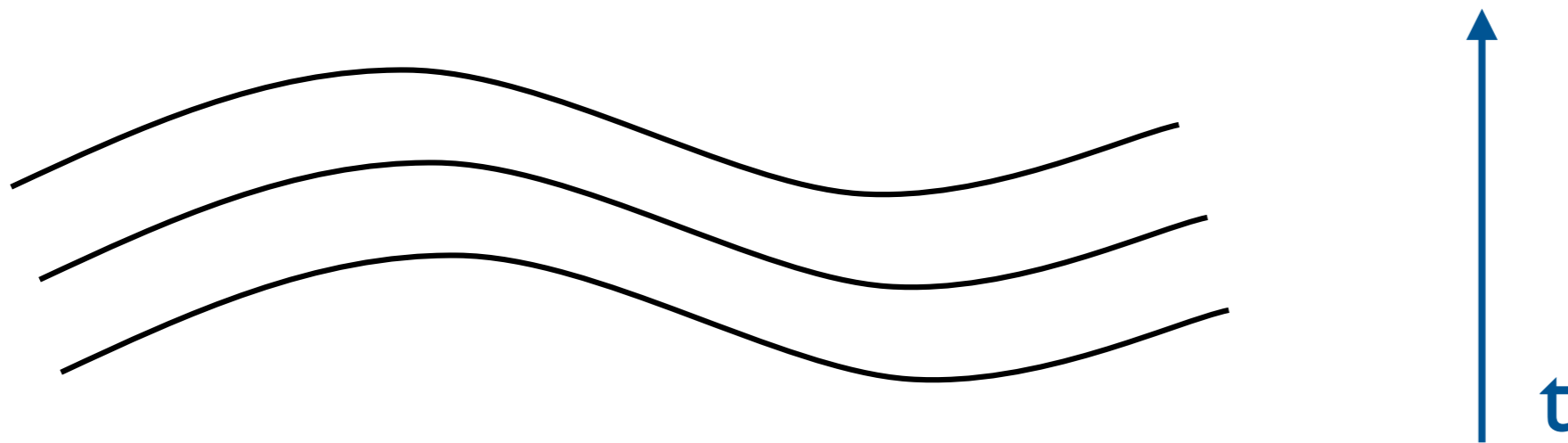
The only consistent  
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$g_{\mu\nu} + \text{STUFF}$



# The skeleton of MG



A scalar field, ok, but more importantly (and more deeply?)...

Minkowski:

$$\phi(t)$$

$$K_i$$

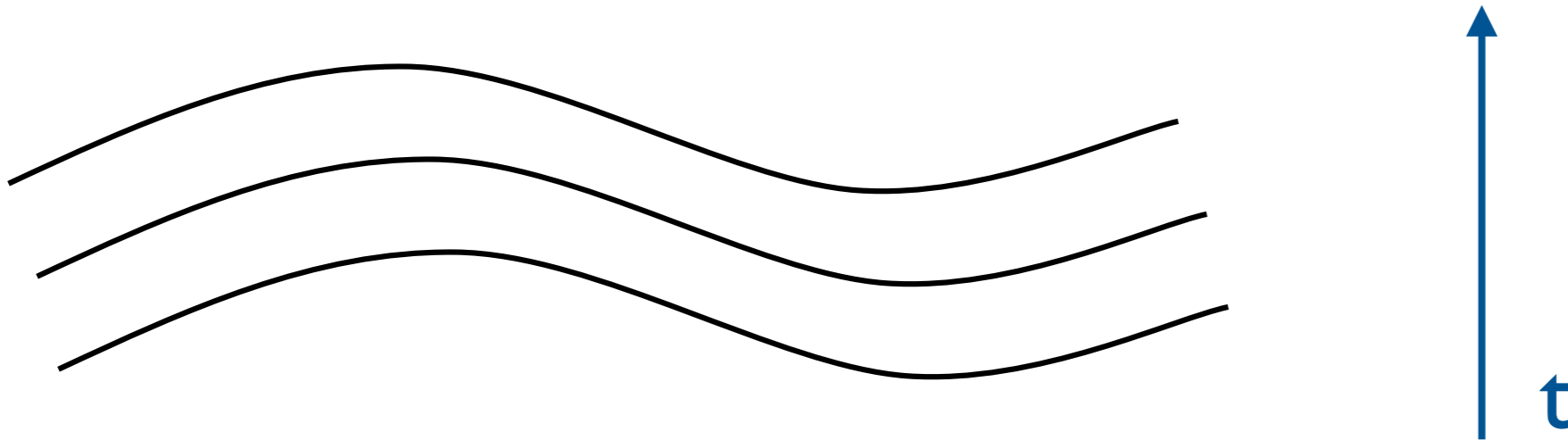
$$H$$

$$Q$$

Internal Charge



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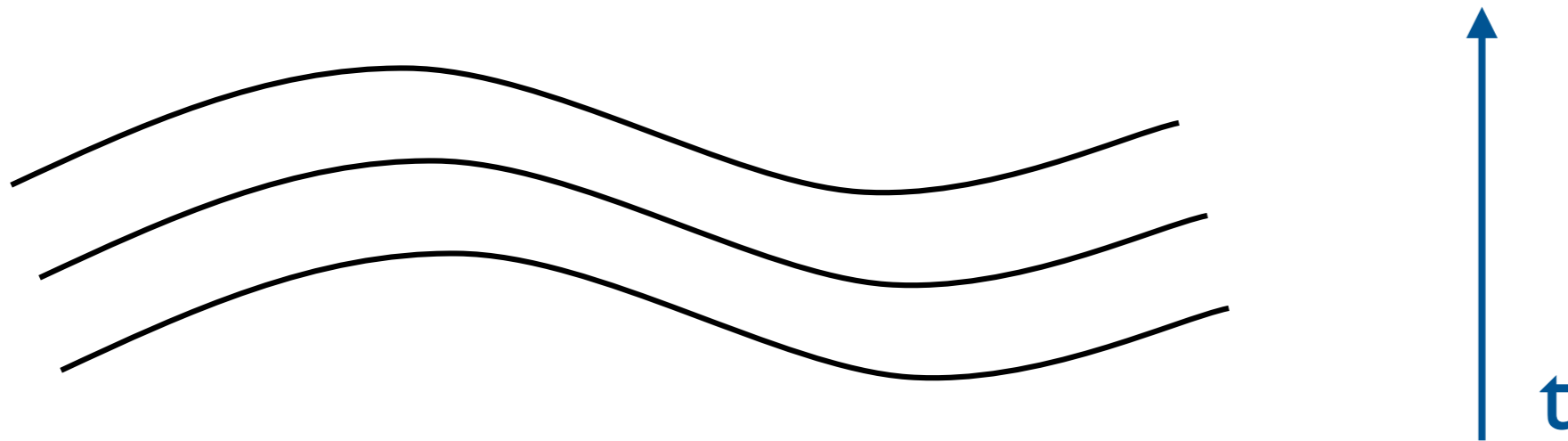
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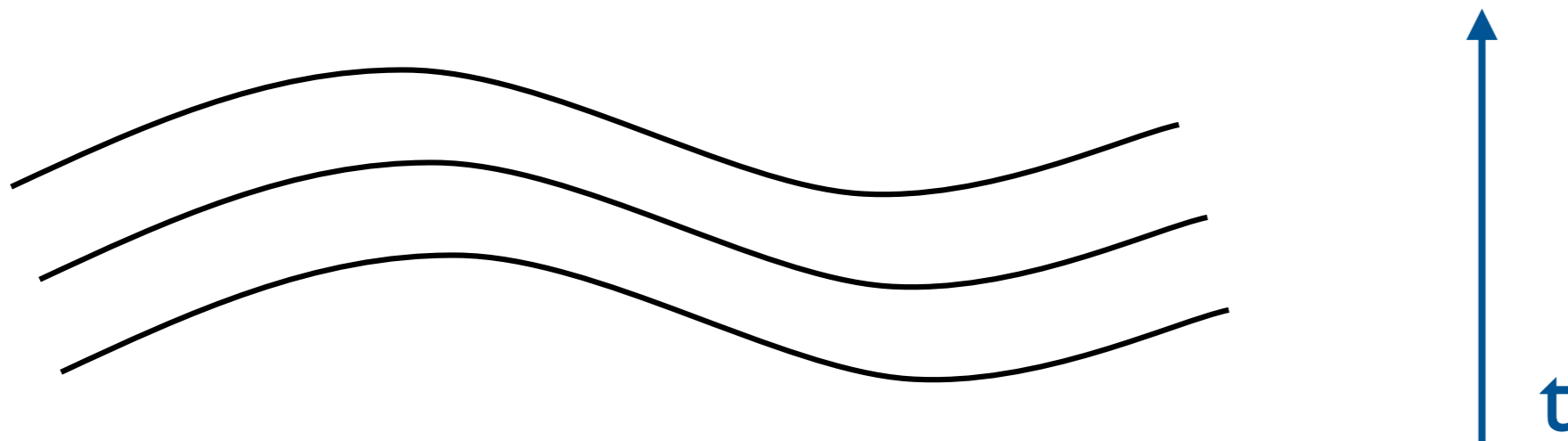
~~$H$~~

$Q$

Internal Charge



# The skeleton of MG



A scalar field, ok, but more importantly (and more deeply?)...

Minkowski:

$\phi(t)$

~~$K_i$~~

~~$H$~~

~~$Q$~~

Internal Charge

$H - \mu Q$



# The skeleton of MG: Minkowski theory

- Poincaré invariant theory
- Fields in some representation of Lorentz group
- Boosts **spontaneously** broken
- Unbroken translations and rotations



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- Poincaré invariant theory
- Fields in some representation of Lorentz group
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$$\left\{ \begin{array}{l} \bar{P}^\mu \\ \bar{J}^i \end{array} \right. \quad \begin{array}{l} \text{translations} \\ \text{rotations} \end{array}$$

$$[\bar{J}_i, \bar{P}_j] = i\epsilon_{ijk} \bar{P}_k$$

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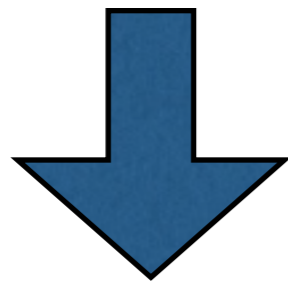


# Classifying Condensed Matter

Full Symmetry group: Poincaré

$$\left\{ \begin{array}{l} P^\mu \\ J^i \\ K^i \end{array} \right. \quad \begin{array}{l} \text{translations} \\ \text{rotations} \\ \text{boosts} \end{array}$$

+ internal 'Q' symmetries



$$\left\{ \begin{array}{l} \bar{P}^\mu \\ \bar{J}^i \end{array} \right. \quad \begin{array}{l} \text{translations} \\ \text{rotations} \end{array}$$

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# Classifying Condensed Matter

Ex:

$$\begin{cases} \bar{H} &= H - \mu Q \\ \bar{P}^i &= P^i \\ \bar{J}^i &= J^i \end{cases}$$

internal symmetry:  $U(1)$

Superfluid

1 Goldstone

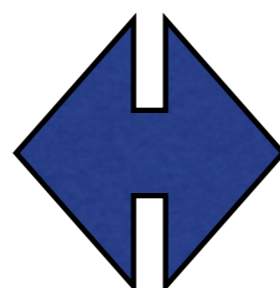
$$\langle \phi(x) \rangle = \mu t$$



# Classifying Condensed Matter

System	Modified generators			# G.B.	Internal symmetries	Extra spacetime symmetries
	$P_t$	$P_i$	$J_i$			
1. type-I framid				3		
2. type-I superfluid	✓			1	$U(1)$	
3. type-I galileid		✓		1		Gal (3+1,1) <sup>4</sup>
4. type-II framid			✓	6	$SO(3)$	
5. type-II galileid	✓	✓		1		Gal (3+1,1) <sup>4</sup>
6. type-II superfluid	✓		✓	4	$SO(3) \times U(1)$	
7. solid		✓	✓	3	$ISO(3)$	
8. supersolid	✓	✓	✓	4	$ISO(3) \times U(1)$	

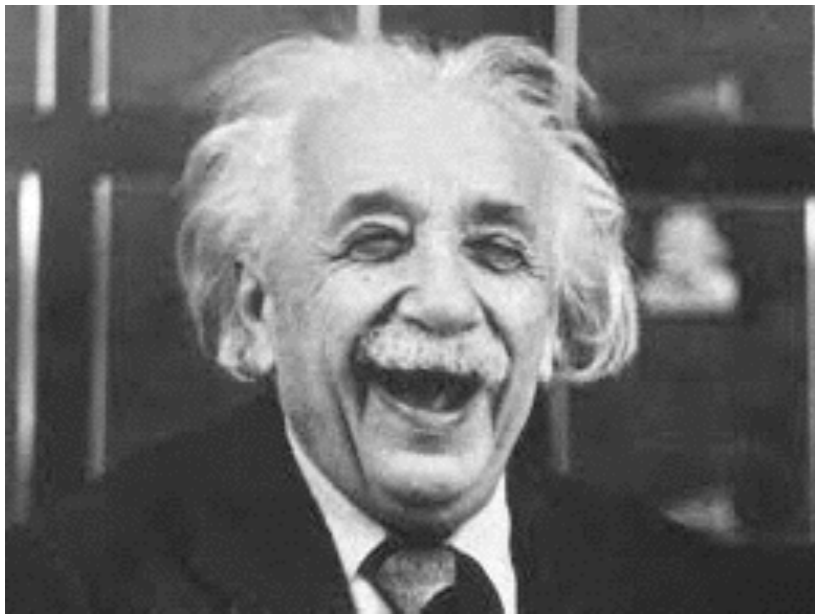
Condensed matter



Cosmology/modified gravity

superfluids  
solids  
framids

shift-symmetric scalar  
solid inflation  
Einstein aether



$\Lambda$ CDM

The only consistent  
low energy theory for  
a massless spin-two field  $g_{\mu\nu}$ .



$g_{\mu\nu} + \text{STUFF}$



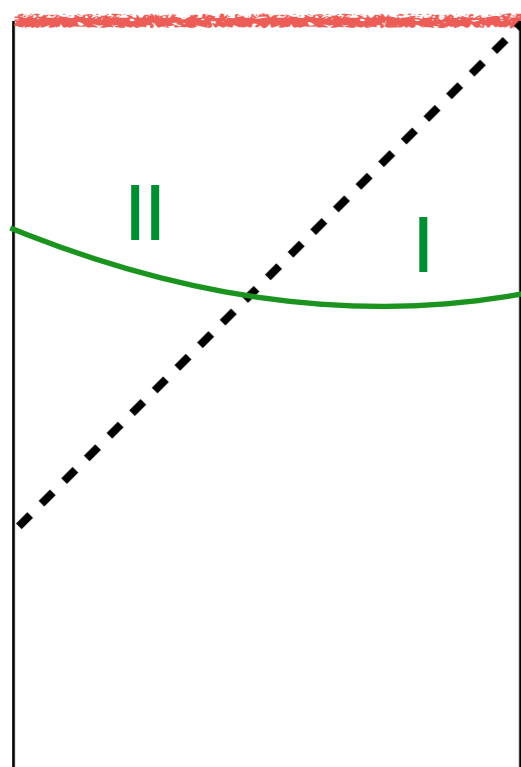
Other fundamental ingredients?



# Where could the EFT ‘mantra’ be wrong?

Quantum gravity: not necessarily confined to the UV

BH in AdS



CFT

$$\mathcal{H} = \mathcal{H}_I \otimes \mathcal{H}_{II}$$

Inside dof: **duplicate** of those outside

Papadodimas, Raju, 2012-2016

**‘ER=EPR’**

Entanglement defines (and generalizes) spacetime

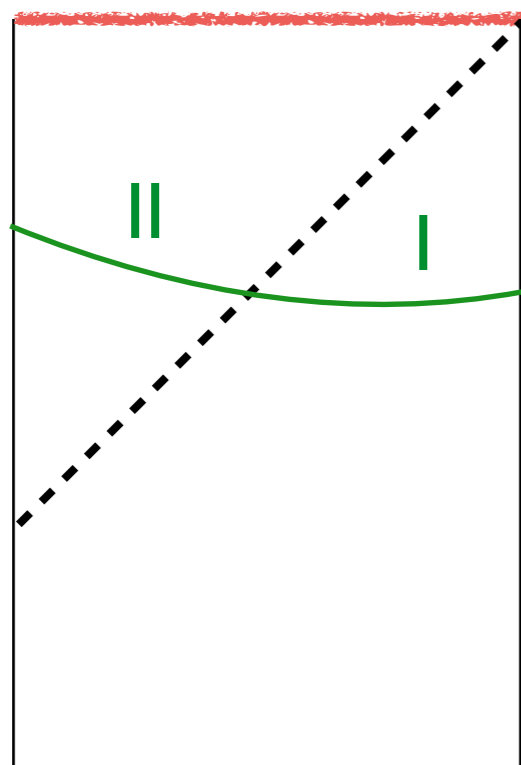
Susskind, Maldacena, 2013



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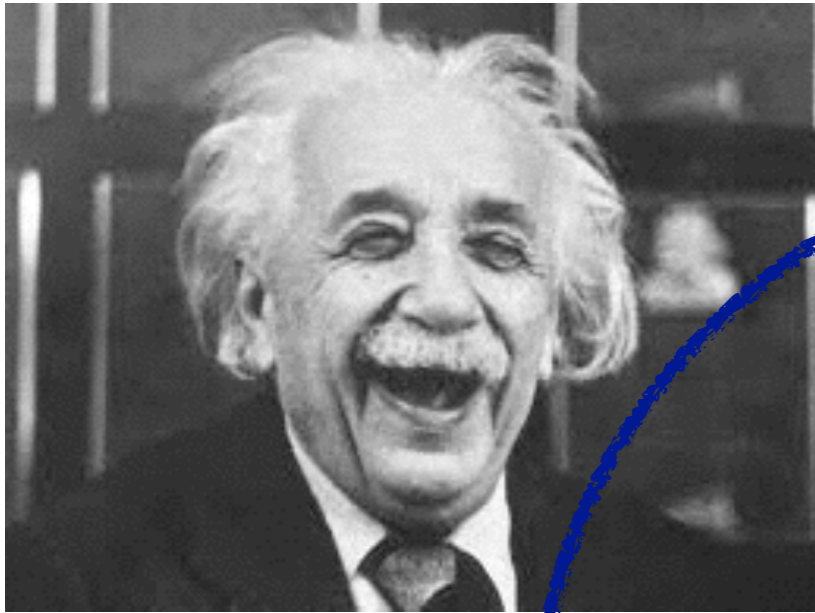
Papadodimas, Raju, 2012-2016

**‘ER=EPR’**

Entanglement defines (and generalizes) spacetime

Susskind, Maldacena, 2013

In cosmology these effects are expected to be small



$\Lambda$ CDM

EFT of DE

+ a scalar field  $\phi$

$g_{\mu\nu} + \text{STUFF}$



Other fundamental ingredients?

# The effective field theory (EFT) of dark energy

- Most general description of **1 scalar degree of freedom** added to GR
- Matter universally coupled (Weak equivalence principle)
- **Cosmological perturbations** as the relevant objects of the theory
- **Background** (0th order) and **perturbation** (linear and +) sectors
- Good parameter space to constrain with data (see **Planck 2015**)

# Unitary gauge in Cosmology (technical detour)

## The Effective Field Theory of Inflation (Creminelli et al. '06, Cheung et al. '07)

Main idea: scalar degrees of freedom are 'eaten' by the metric. Ex:

$$\phi(t, \vec{x}) \rightarrow \phi_0(t) \quad (\delta\phi = 0) \quad -\frac{1}{2}\partial\phi^2 \rightarrow -\frac{1}{2}\dot{\phi}_0^2(t) g^{00}$$



# The Action

$$S = \int d^4x \sqrt{-g} \frac{M^2(t)}{2} \left[ R - 2\lambda(t) - 2\mathcal{C}(t)g^{00} \right. \\ \left. + \mu_2^2(t)(\delta g^{00})^2 - \mu_3(t)\delta K\delta g^{00} + \epsilon_4(t) \left( \delta K^\mu{}_\nu \delta K^\nu{}_\mu - \delta K^2 + \frac{R^{(3)}\delta g^{00}}{2} \right) + \dots \right]$$

# The Action

## Background (expansion history)

$$S = \int d^4x \sqrt{-g} \frac{M^2(t)}{2} \left[ R - 2\lambda(t) - 2\mathcal{C}(t)g^{00} \right. \\ \left. + \mu_2^2(t)(\delta g^{00})^2 - \mu_3(t)\delta K\delta g^{00} + \epsilon_4(t) \left( \delta K^\mu{}_\nu \delta K^\nu{}_\mu - \delta K^2 + \frac{R^{(3)}\delta g^{00}}{2} \right) + \dots \right]$$

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Background (expansion history)

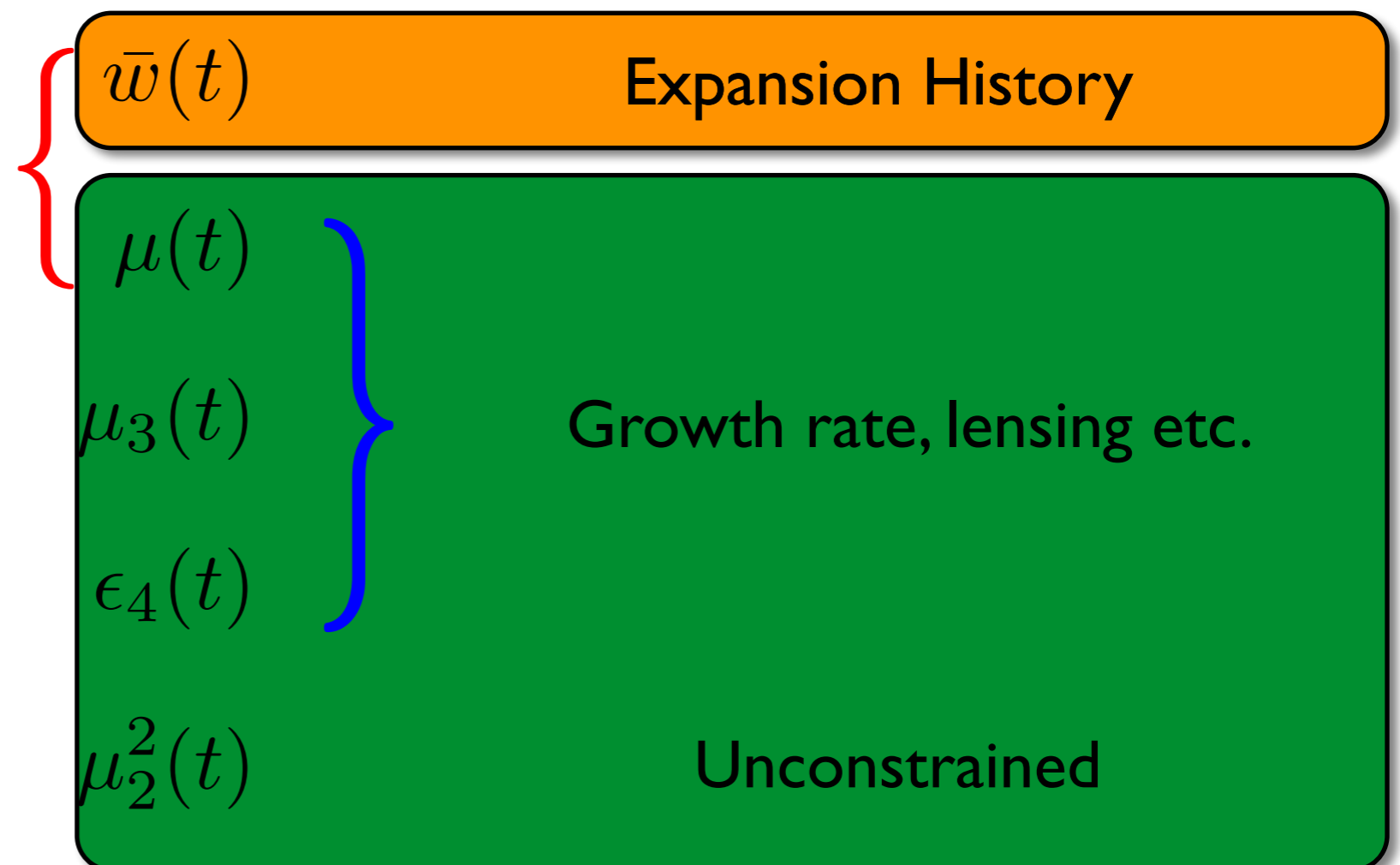
$$S = \int d^4x \sqrt{-g} \frac{M^2(t)}{2} \left[ R - 2\lambda(t) - 2\mathcal{C}(t)g^{00} \right. \\ \left. + \mu_2^2(t)(\delta g^{00})^2 - \mu_3(t)\delta K \delta g^{00} + \epsilon_4(t) \left( \delta K^\mu{}_\nu \delta K^\nu{}_\mu - \delta K^2 + \frac{R^{(3)} \delta g^{00}}{2} \right) + \dots \right]$$

only affect perturbations

# Complete background separation

$$S = \int d^4x \sqrt{-g} \frac{M^2(t)}{2} \left[ R - 2\lambda(t) - 2\mathcal{C}(t)g^{00} \right. \\ \left. + \mu_2^2(t)(\delta g^{00})^2 - \mu_3(t)\delta K\delta g^{00} + \epsilon_4(t) \left( \delta K^\mu_\nu \delta K^\nu_\mu - \delta K^2 + \frac{R^{(3)}\delta g^{00}}{2} \right) + \dots \right]$$

$$\lambda(t), \mathcal{C}(t), \mu(t) \equiv \frac{d \ln M^2(t)}{dt}$$



# Complete background separation

$$S = \int d^4x \sqrt{-g} \frac{M^2(t)}{2} \left[ R - 2\lambda(t) - 2\mathcal{C}(t)g^{00} + \mu_2^2(t)(\delta g^{00})^2 - \mu_3(t)\delta K\delta g^{00} + \epsilon_4(t) \left( \delta K^\mu_\nu \delta K^\nu_\mu - \delta K^2 + \frac{R^{(3)}\delta g^{00}}{2} \right) + \dots \right]$$

$$\lambda(t), \mathcal{C}(t), \mu(t) \equiv \frac{d \ln M^2(t)}{dt}$$

Alternatively

$$\alpha_K(t), \alpha_M(t), \alpha_B(t), \alpha_T(t)$$

Bellini, Sawicki '14

Gleyzes, Langlois, F.P., Vernizzi '14

Gleyzes, Langlois, Vernizzi '14

$\bar{w}(t)$

Expansion History

$\mu(t)$

$\mu_3(t)$

$\epsilon_4(t)$

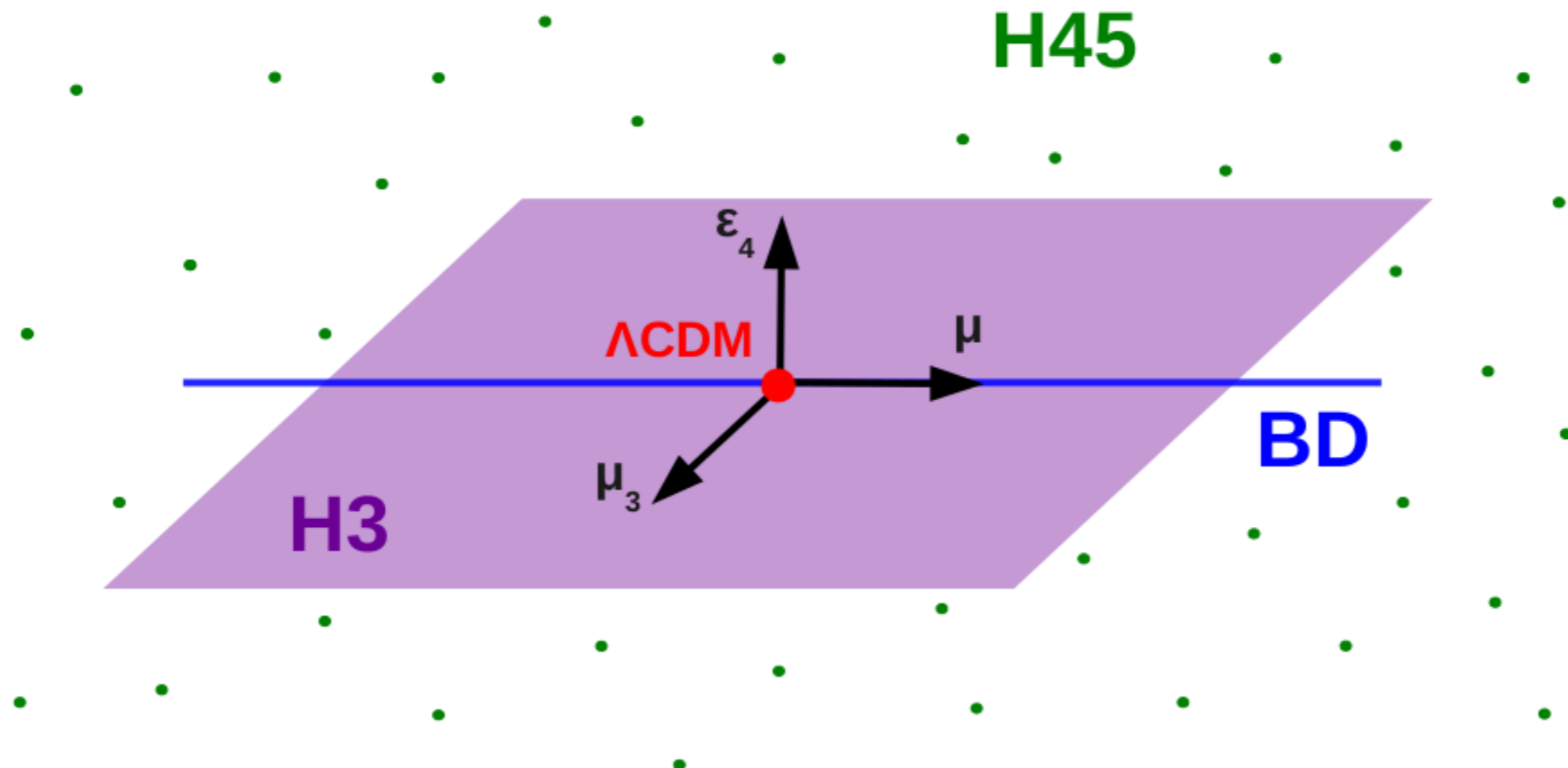
$\mu_2^2(t)$

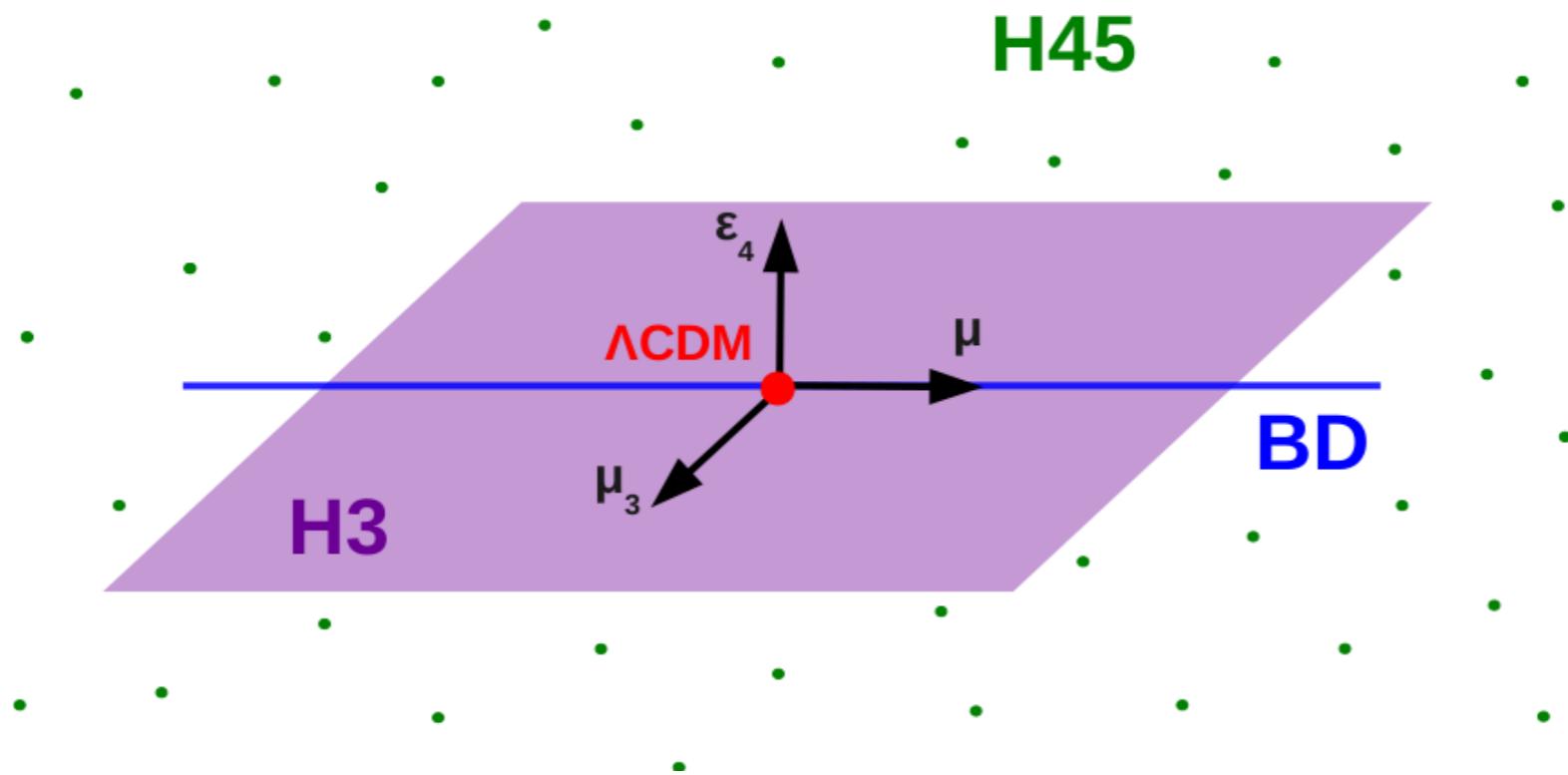
Growth rate, lensing etc.

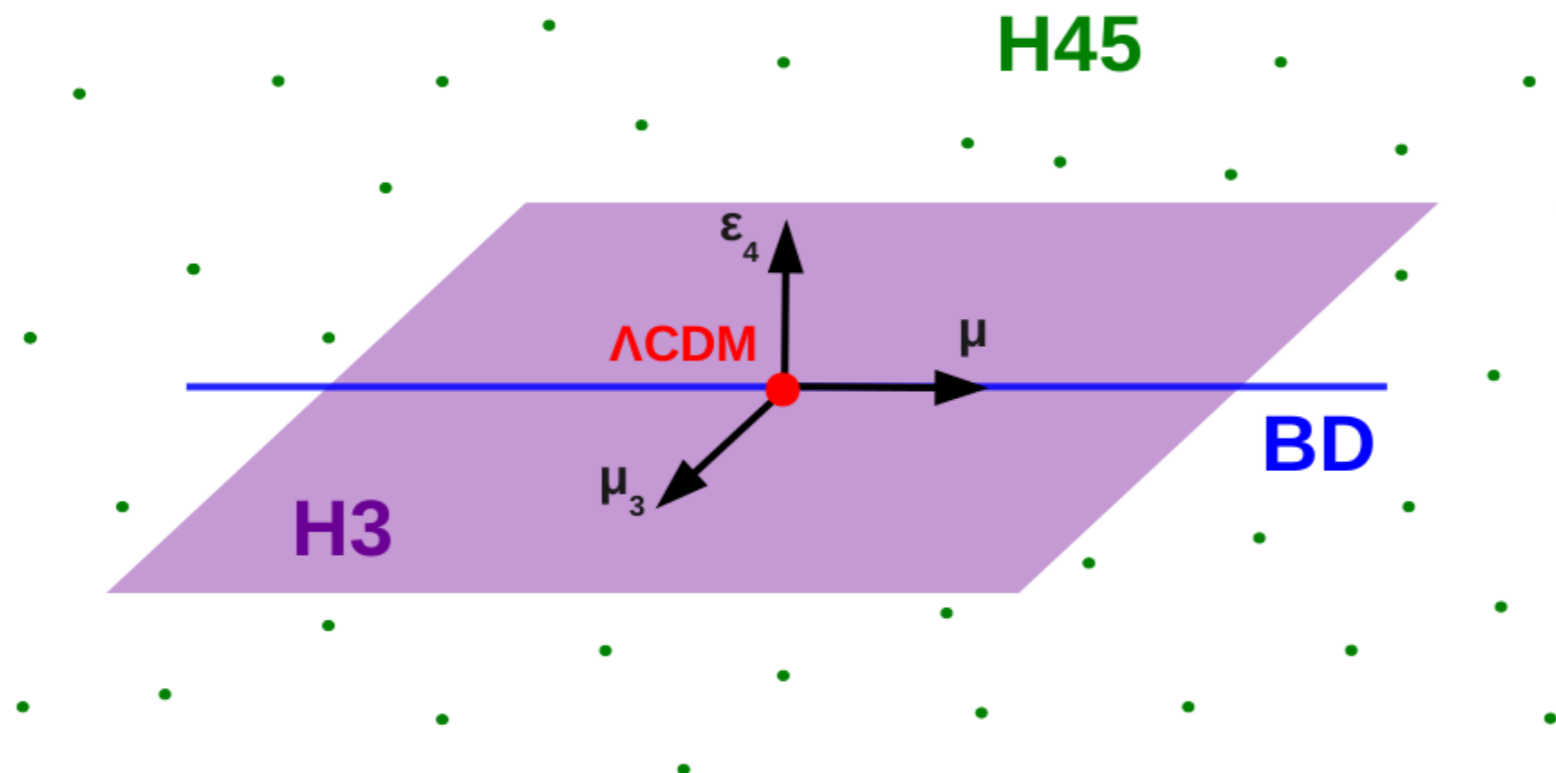
Unconstrained

# The space of modified gravity

$$S = \int d^4x \sqrt{-g} \frac{M^2(t)}{2} \left[ R - 2\lambda(t) - 2\mathcal{C}(t)g^{00} + \mu_2^2(t)(\delta g^{00})^2 - \mu_3(t)\delta K\delta g^{00} + \epsilon_4(t) \left( \delta K^\mu{}_\nu \delta K^\nu{}_\mu - \delta K^2 + \frac{R^{(3)}\delta g^{00}}{2} \right) + \dots \right]$$



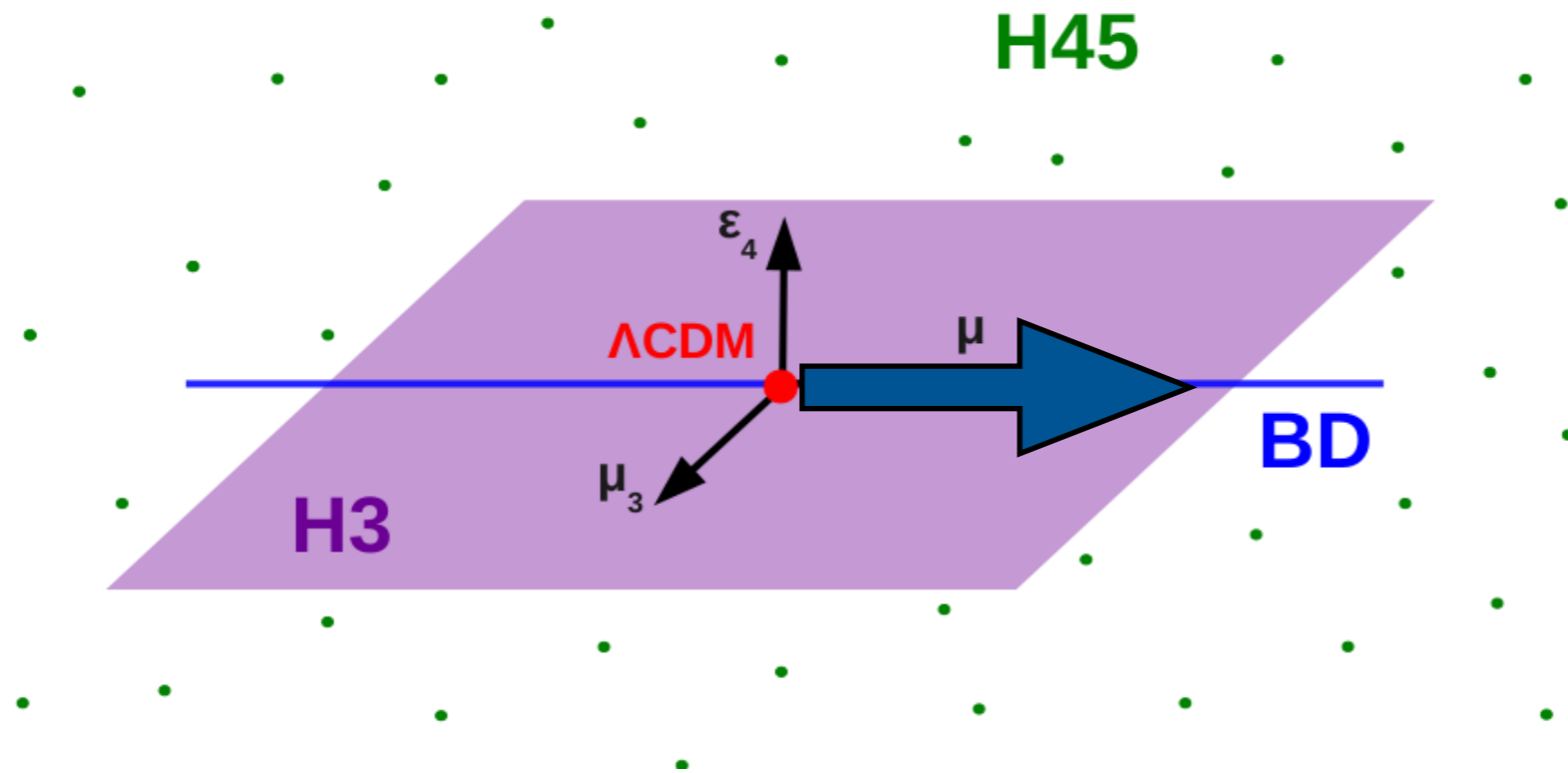




Quintessence  
k-essence  
etc.

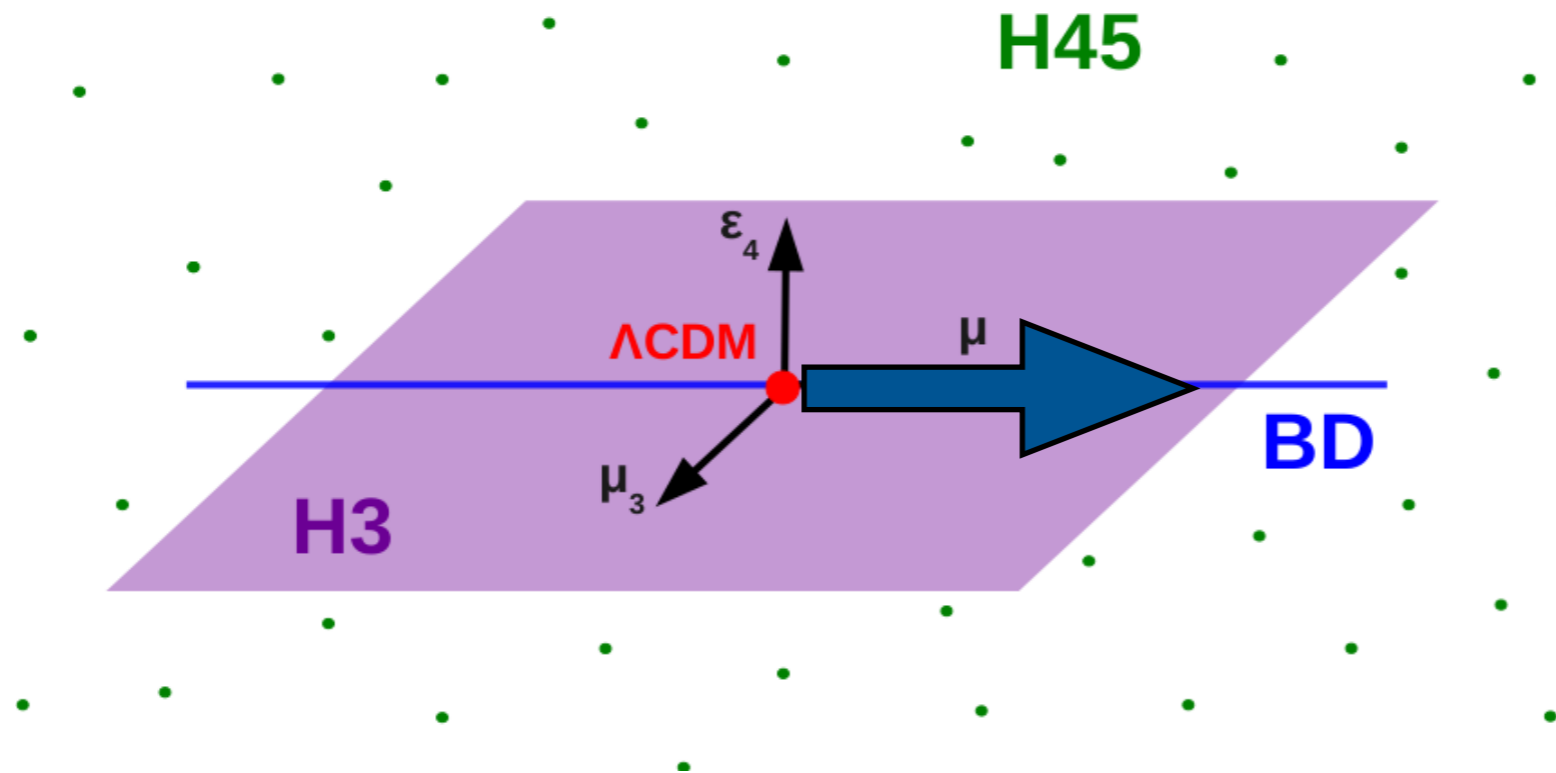
Minimally coupled

$(w \neq -1)$



The  $\mu$  direction (Brans-Dicke,  $F(R)$  theories etc.)

$$\mu \equiv \frac{d \log M^2}{dt}$$



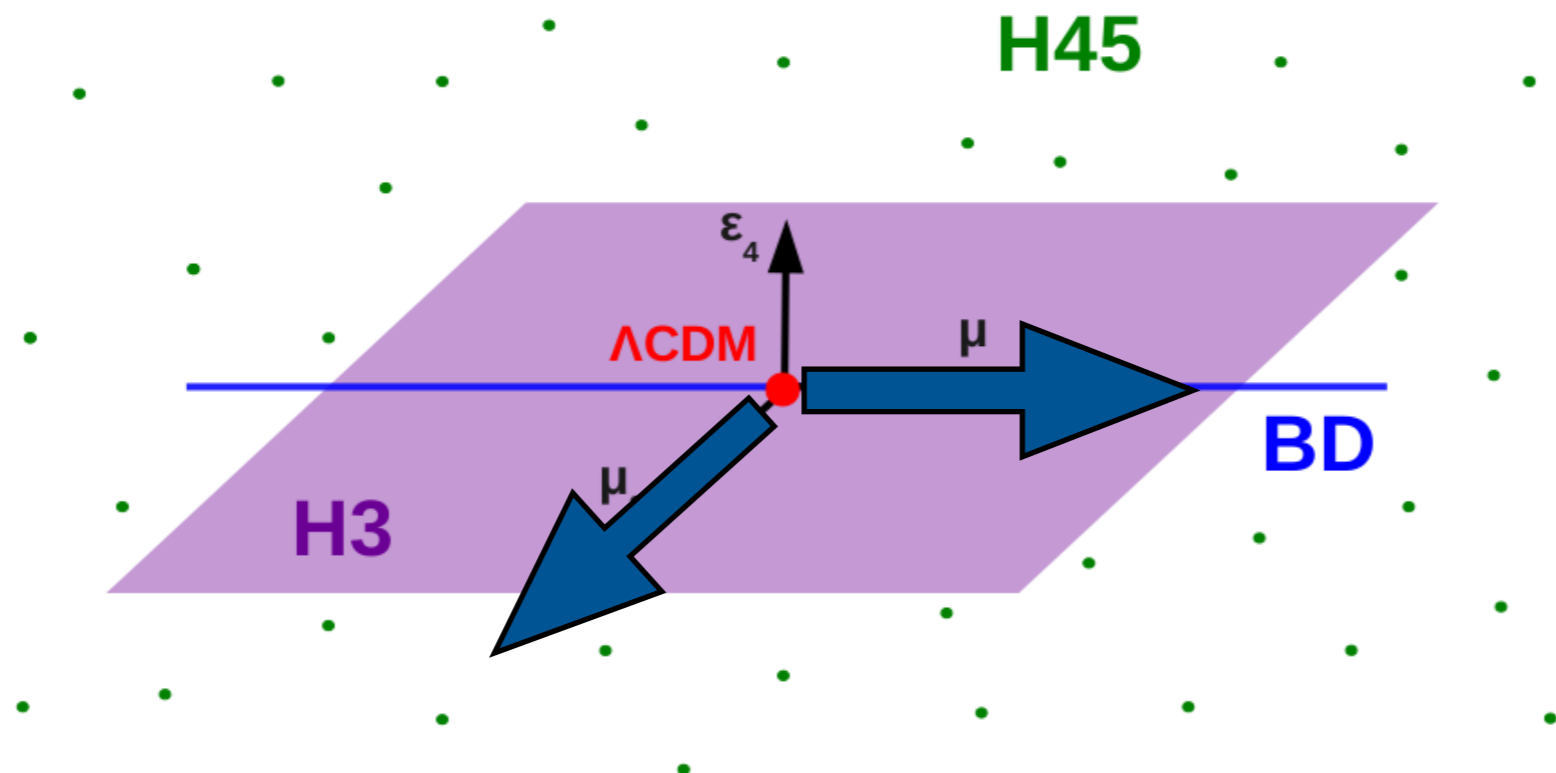
The  $\mu$  direction (Brans-Dicke, F(R) theories etc.)

$$\mu \equiv \frac{d \log M^2}{dt}$$

self-acceleration

$$H^2 = \frac{1}{3M^2(t)} [\rho_m(t) + \rho_{DE}(t)]$$

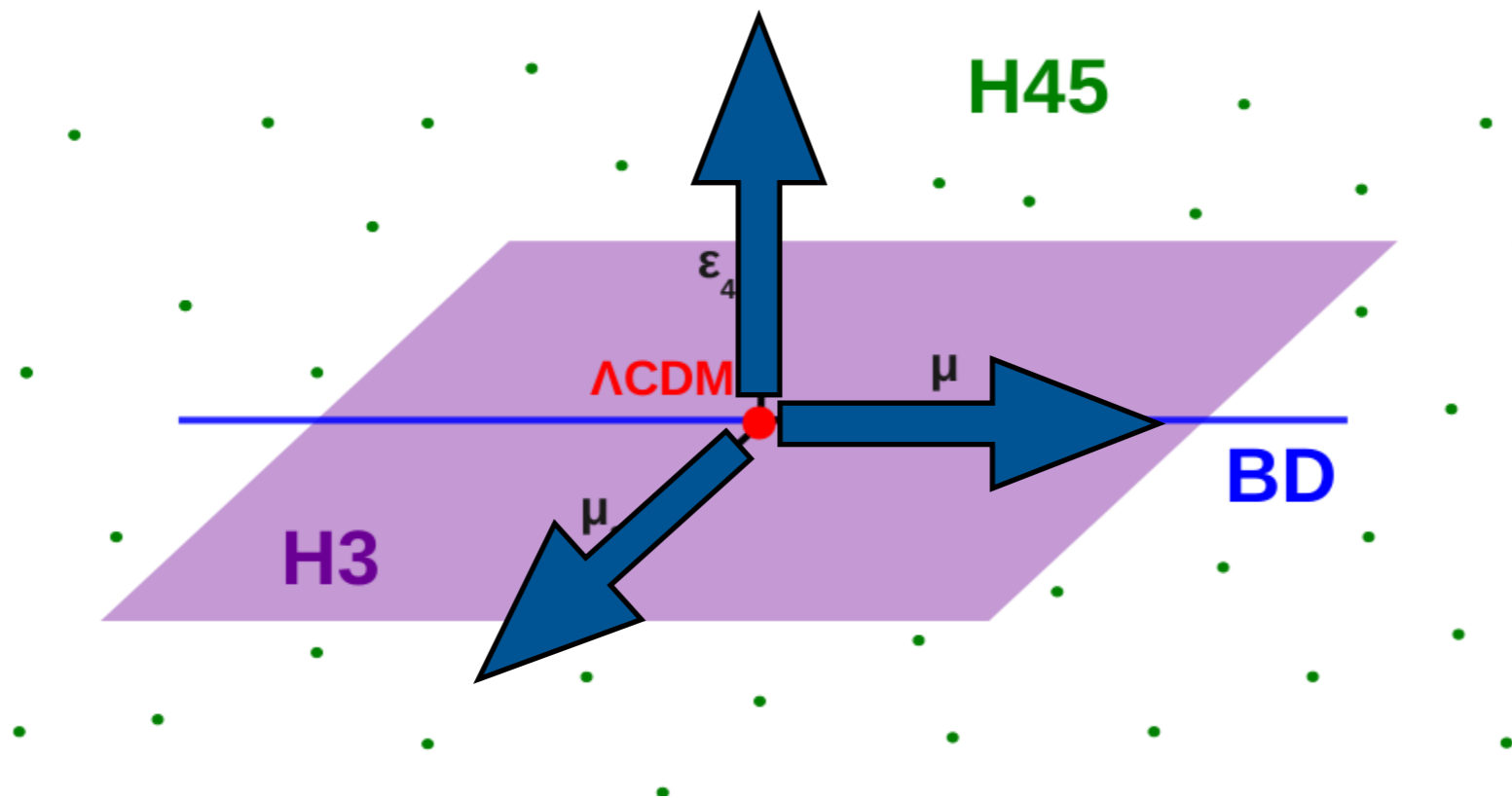
‘normal’ negative pressure



The  $\mu_3$  direction

“Galilean Cosmology” (Chow and Khoury, 2009)

Galileon 3/ Horndeski 3



## “Generalized Galileons” ( $\equiv$ Horndeski)

(Deffayet et al., 2011)

$$\mathcal{L}_2 = A(\phi, X) ,$$

$$\mathcal{L}_3 = B(\phi, X)\Box\phi ,$$

$$\mathcal{L}_4 = C(\phi, X)R - 2C_{,X}(\phi, X)[(\Box\phi)^2 - (\nabla_\mu\nabla_\nu\phi)^2] ,$$

$$\mathcal{L}_5 = D(\phi, X)G^{\mu\nu}\nabla_\mu\nabla_\nu\phi + \frac{1}{3}D_{,X}(\phi, X)[(\Box\phi)^3 - 3(\Box\phi)(\nabla_\mu\nabla_\nu\phi)^2 + 2(\nabla_\mu\nabla_\nu\phi)^3] ,$$

# The space of modified gravity

$$S = \int d^4x \sqrt{-g} \frac{M^2(t)}{2} \left[ R - 2\lambda(t) - 2\mathcal{C}(t)g^{00} + \mu_2^2(t)(\delta g^{00})^2 - \mu_3(t)\delta K\delta g^{00} + \epsilon_4(t) \left( \delta K^\mu{}_\nu \delta K^\nu{}_\mu - \delta K^2 + \frac{R^{(3)}\delta g^{00}}{2} \right) + \dots \right]$$

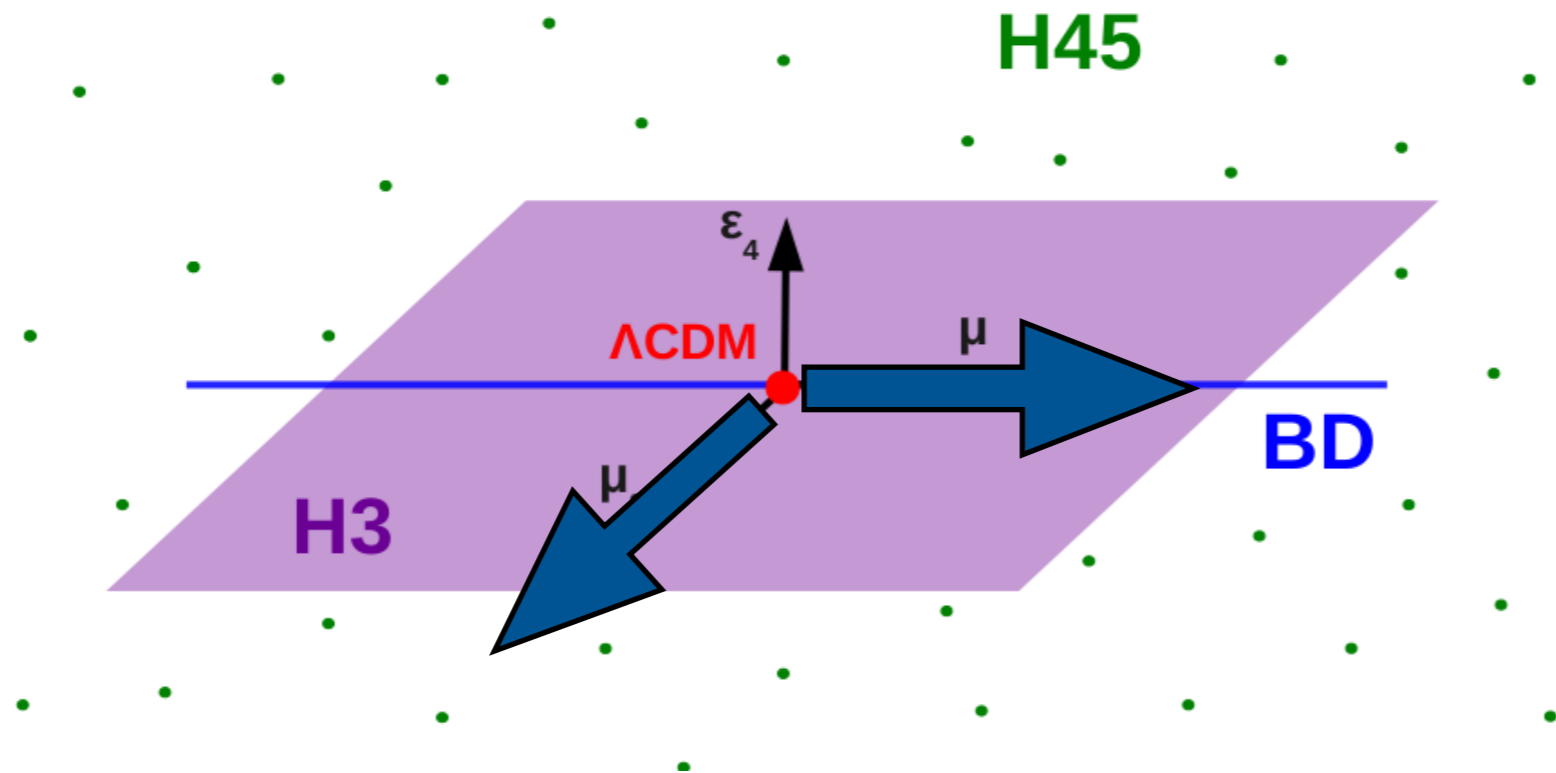
$\epsilon_4(t)$   
 $\nwarrow$

$\tilde{\epsilon}_4(t)$   
 $\nearrow$

## Beyond Horndeski

The most general (linear) theory without higher derivatives on the propagating degree of freedom

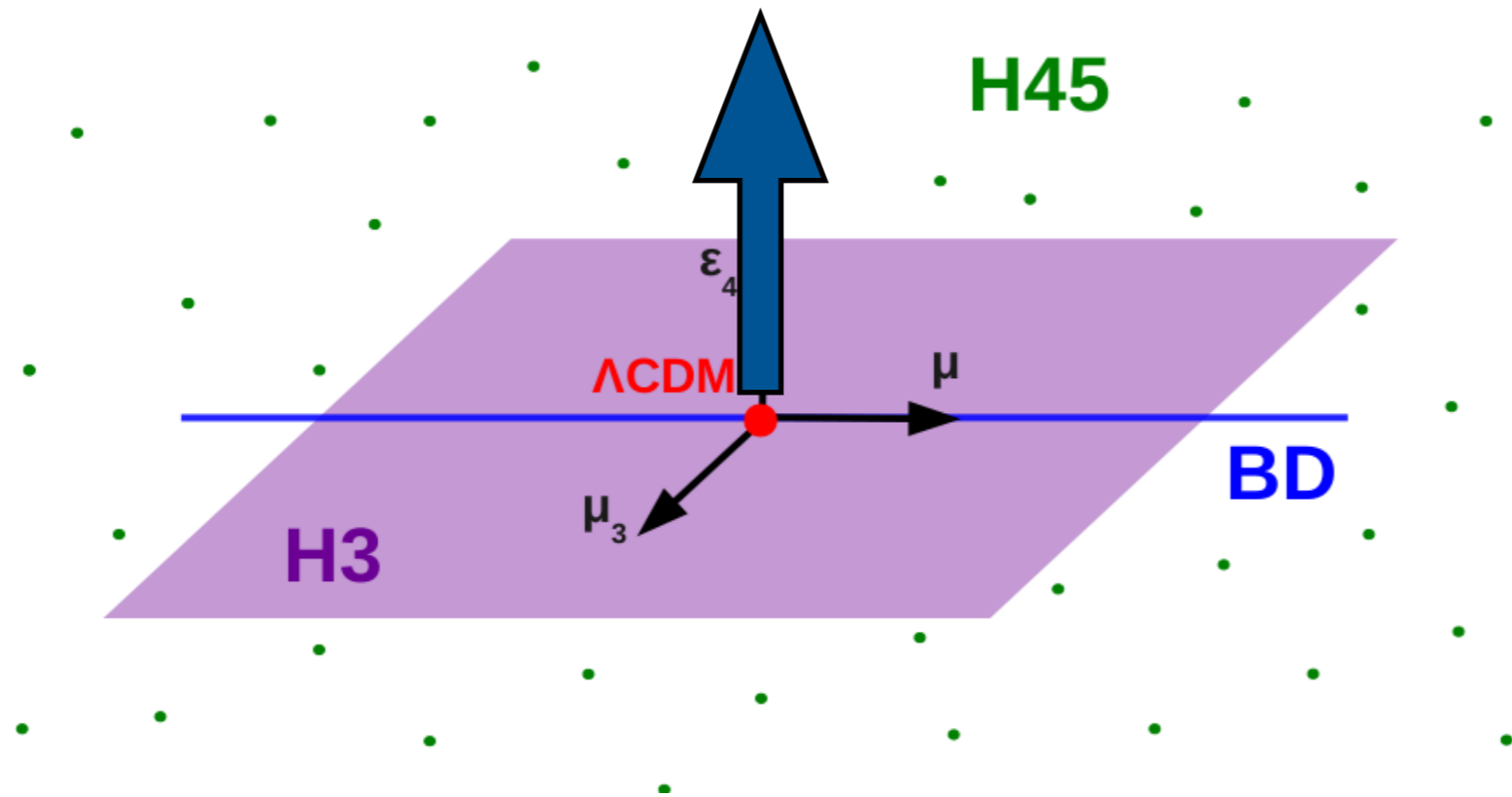
Newtonian gauge: scalar d.o.f.:  $\Phi, \Psi, \pi$



$$\mathcal{L} = (\mu - \mu_3) \vec{\nabla} \Phi \vec{\nabla} \pi + \dots$$

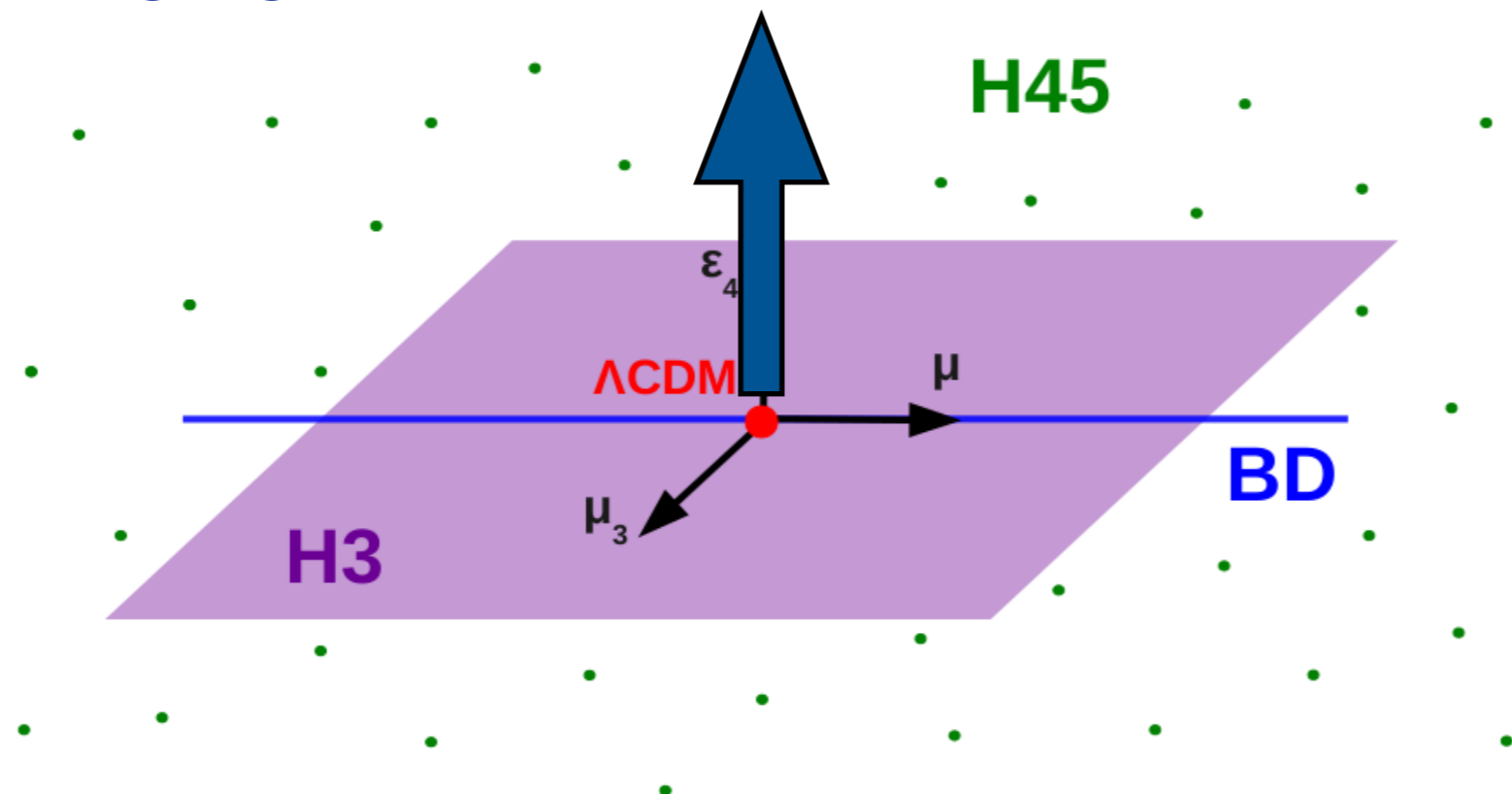
kinetic couplings metric-scalar

Newtonian gauge: scalar d.o.f.:  $\Phi, \Psi, \pi$



$$\mathcal{L} = (\dot{\epsilon}_4 + H\epsilon_4) \vec{\nabla} \Psi \vec{\nabla} \pi$$

Newtonian gauge: scalar d.o.f.:  $\Phi, \Psi, \pi$

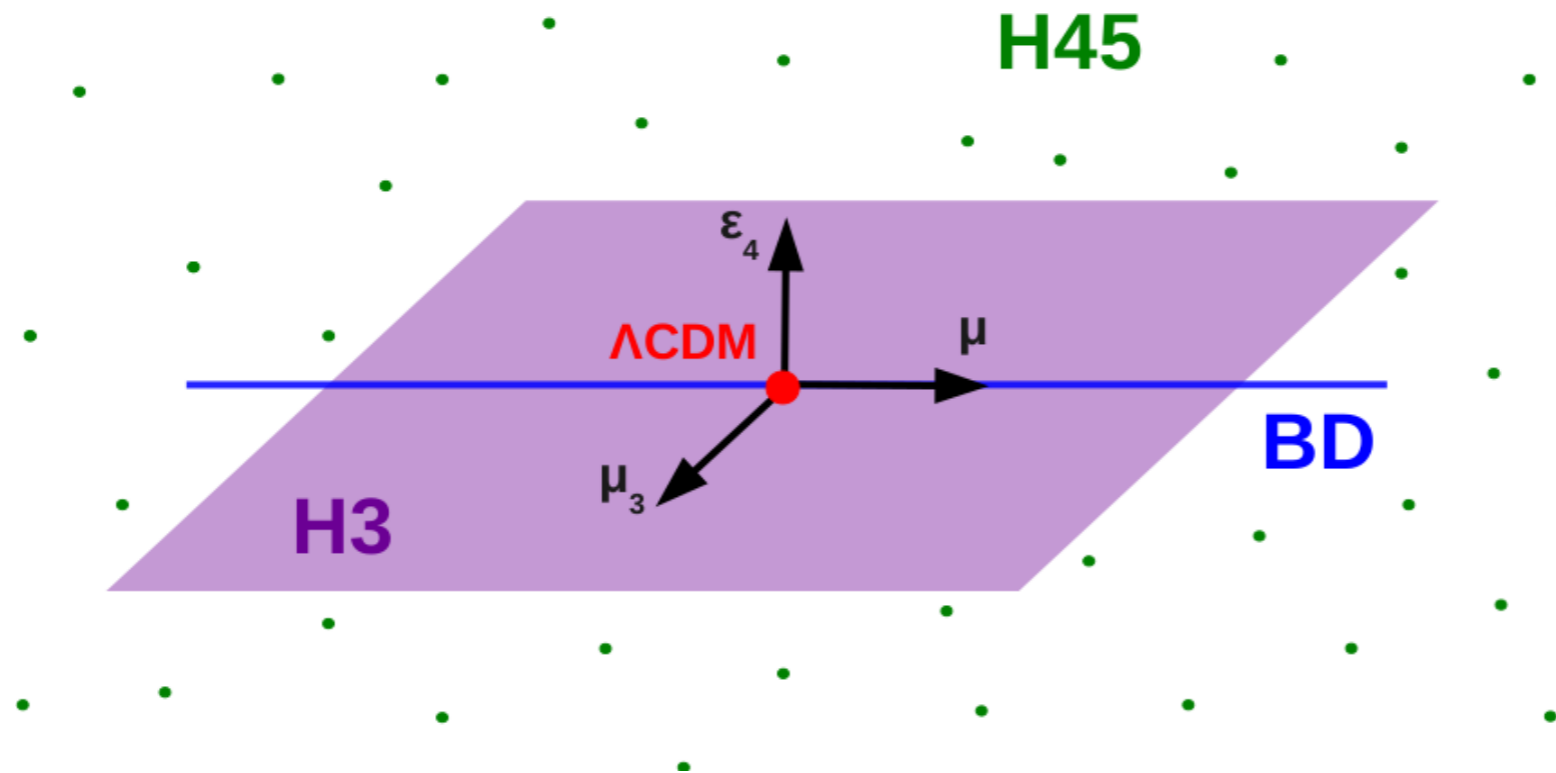


$$\mathcal{L} = (\dot{\epsilon}_4 + H\epsilon_4) \vec{\nabla} \Psi \vec{\nabla} \pi$$

$$c_T^2 = \frac{1}{1 + \epsilon_4}$$

but also: speed of gravitational waves!

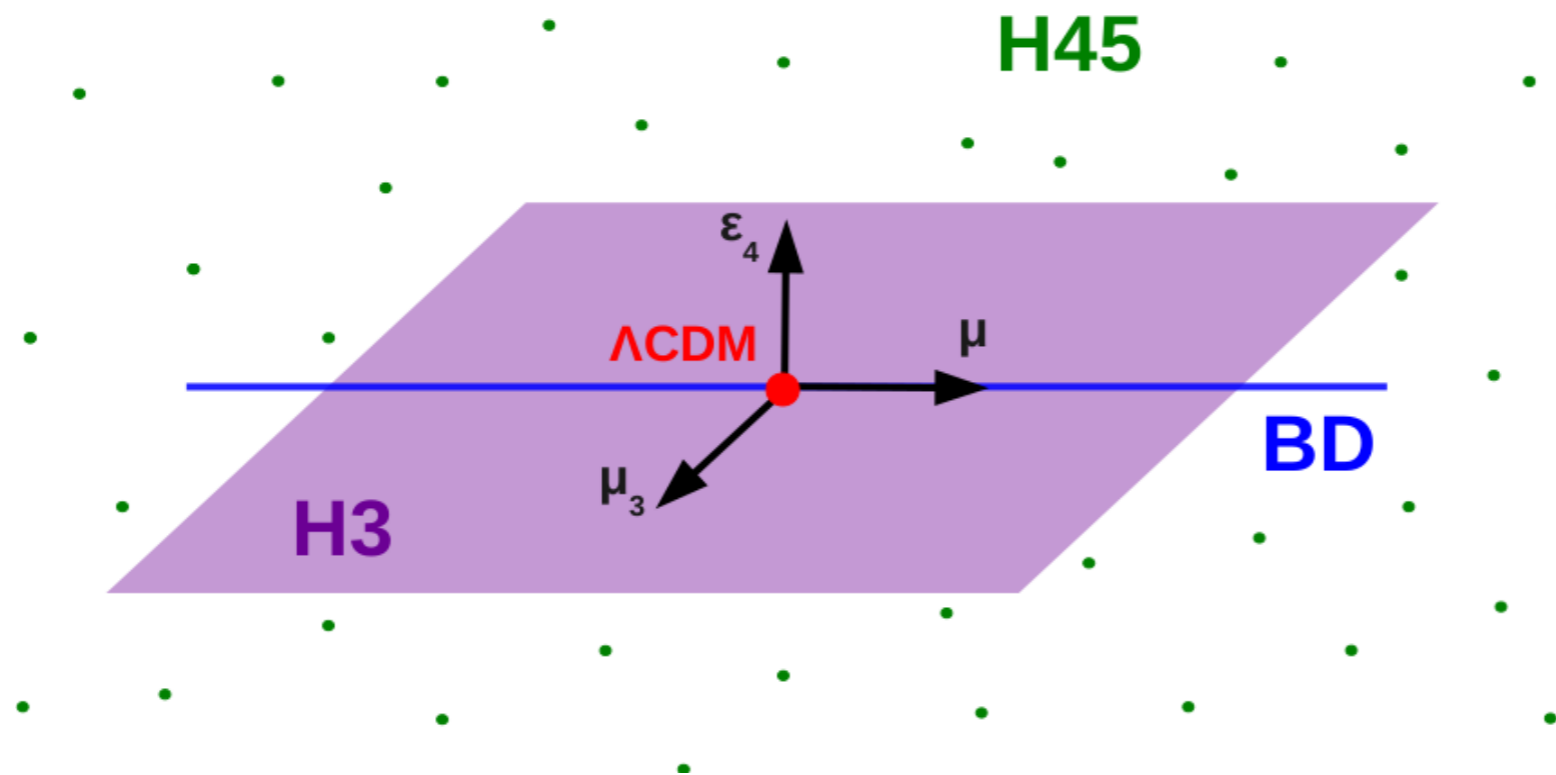
Newtonian gauge: scalar d.o.f.:  $\Phi, \Psi, \pi$



‘Observables’ in the perturbation sector:  
effective Newton constant and gravitational slip parameter

$$-\frac{k^2}{a^2}\Phi = 4\pi G_{\text{eff}}[\mu, \mu_3, \epsilon_4](t) \rho_m \delta_m$$

$$\frac{\Psi}{\Phi} = \gamma[\mu, \mu_3, \epsilon_4](t)$$



The space of theories: not so smooth...

# Stability conditions

$$S_\pi = \int a^3(t) M^2(t) \left[ A(\mu, \mu_2^2, \mu_3, \epsilon_4) \dot{\pi}^2 + B(\mu, \mu_3, \epsilon_4) \frac{(\vec{\nabla} \pi)^2}{a^2} \right] + \text{lower order in derivatives.}$$

↑  
No ghost:  $A > 0$

↑  
No gradient instabilities:  $B < 0$

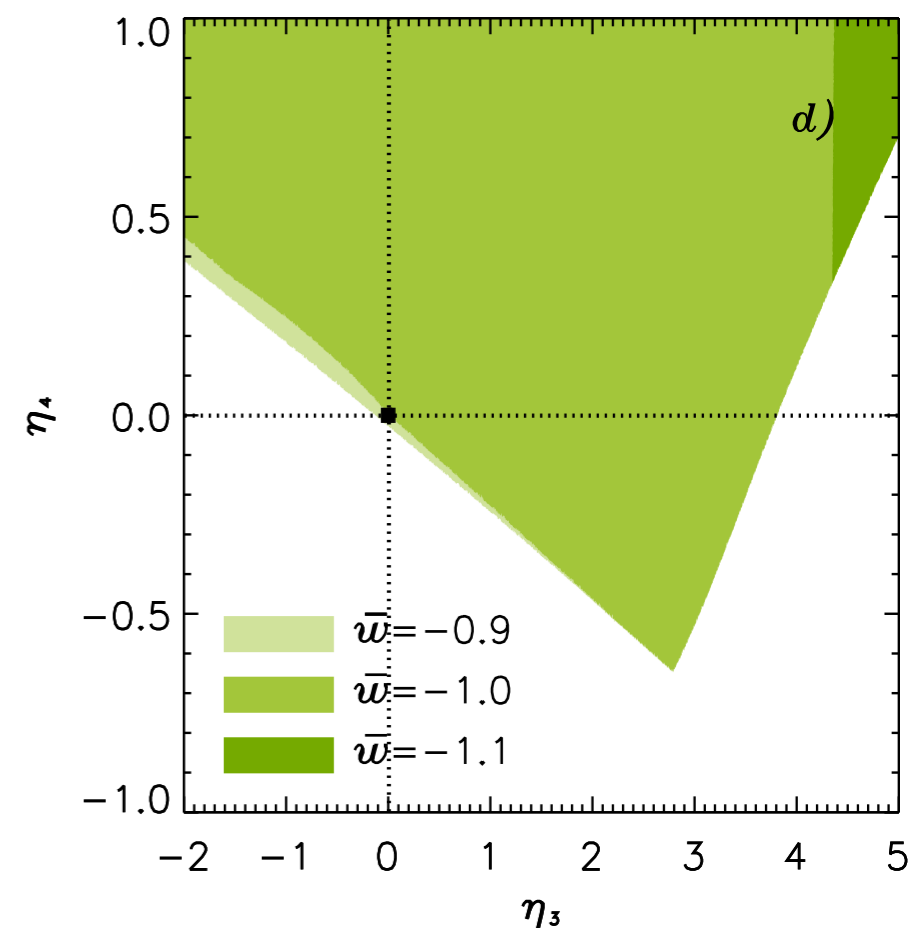
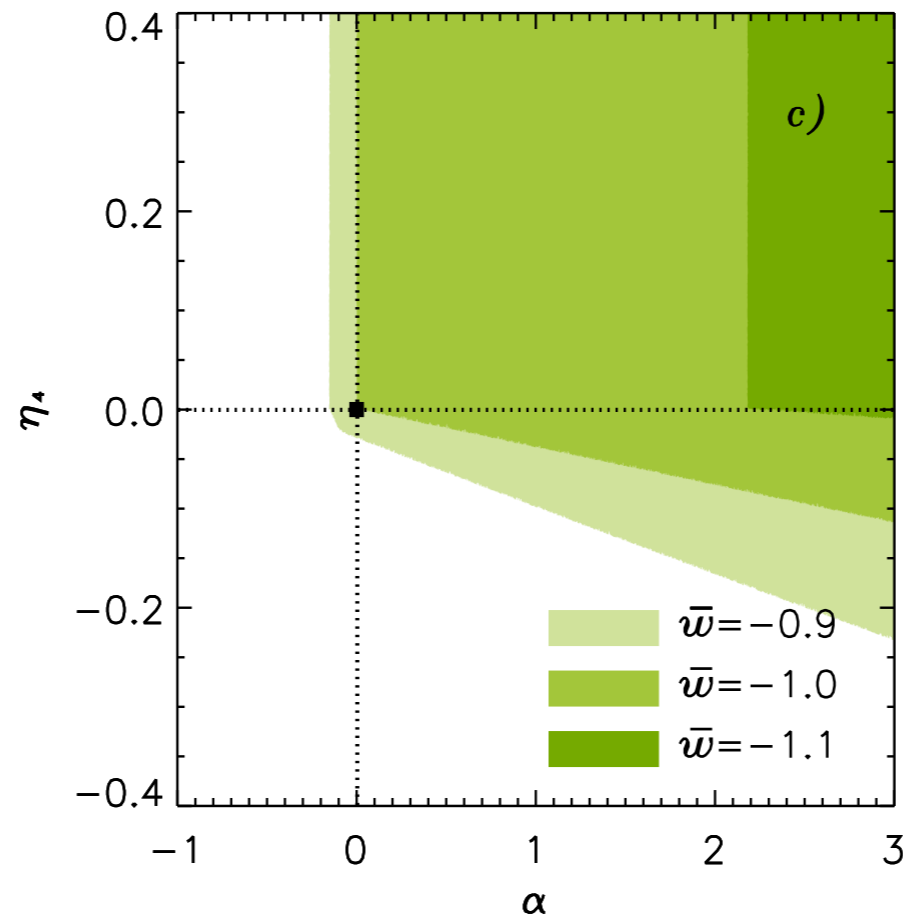
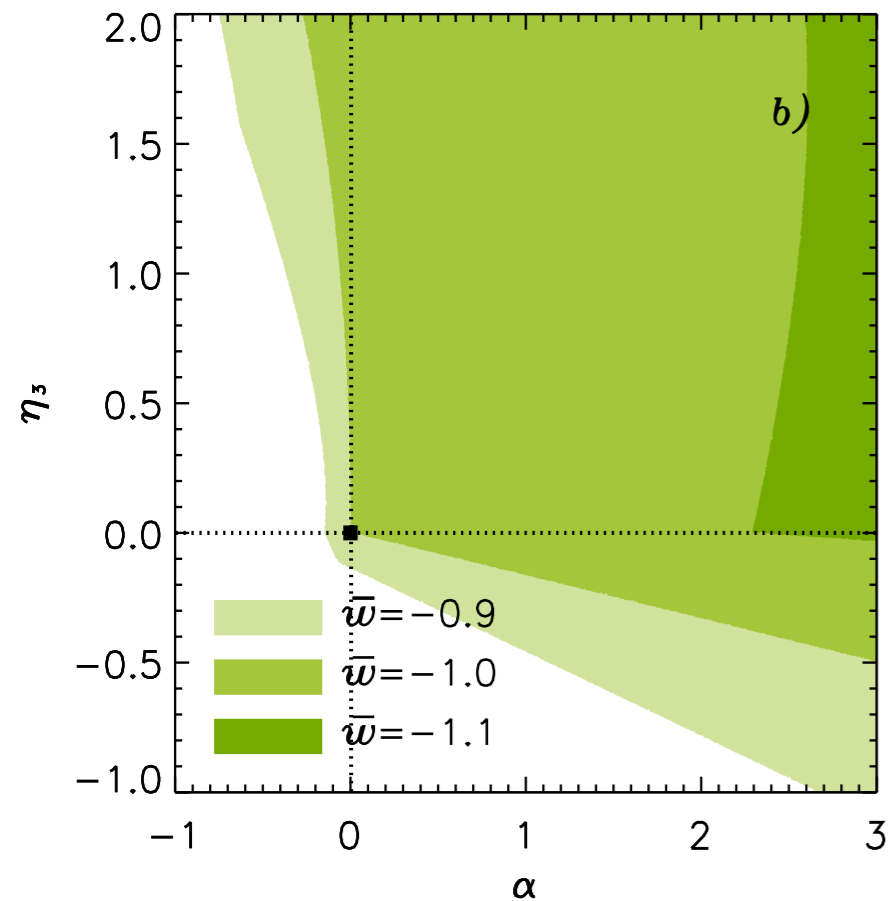
# Stability conditions

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No ghost:  $A > 0$

No gradient instabilities:  $B < 0$

$$\mu_2^2 = 0$$



# Stability conditions

$$S_\pi = \int a^3(t) M^2(t) \left[ A(\mu, \mu_2^2, \mu_3, \epsilon_4) \dot{\pi}^2 + B(\mu, \mu_3, \epsilon_4) \frac{(\vec{\nabla} \pi)^2}{a^2} \right] + \text{lower order in derivatives.}$$

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Basic requirement

Option 1:

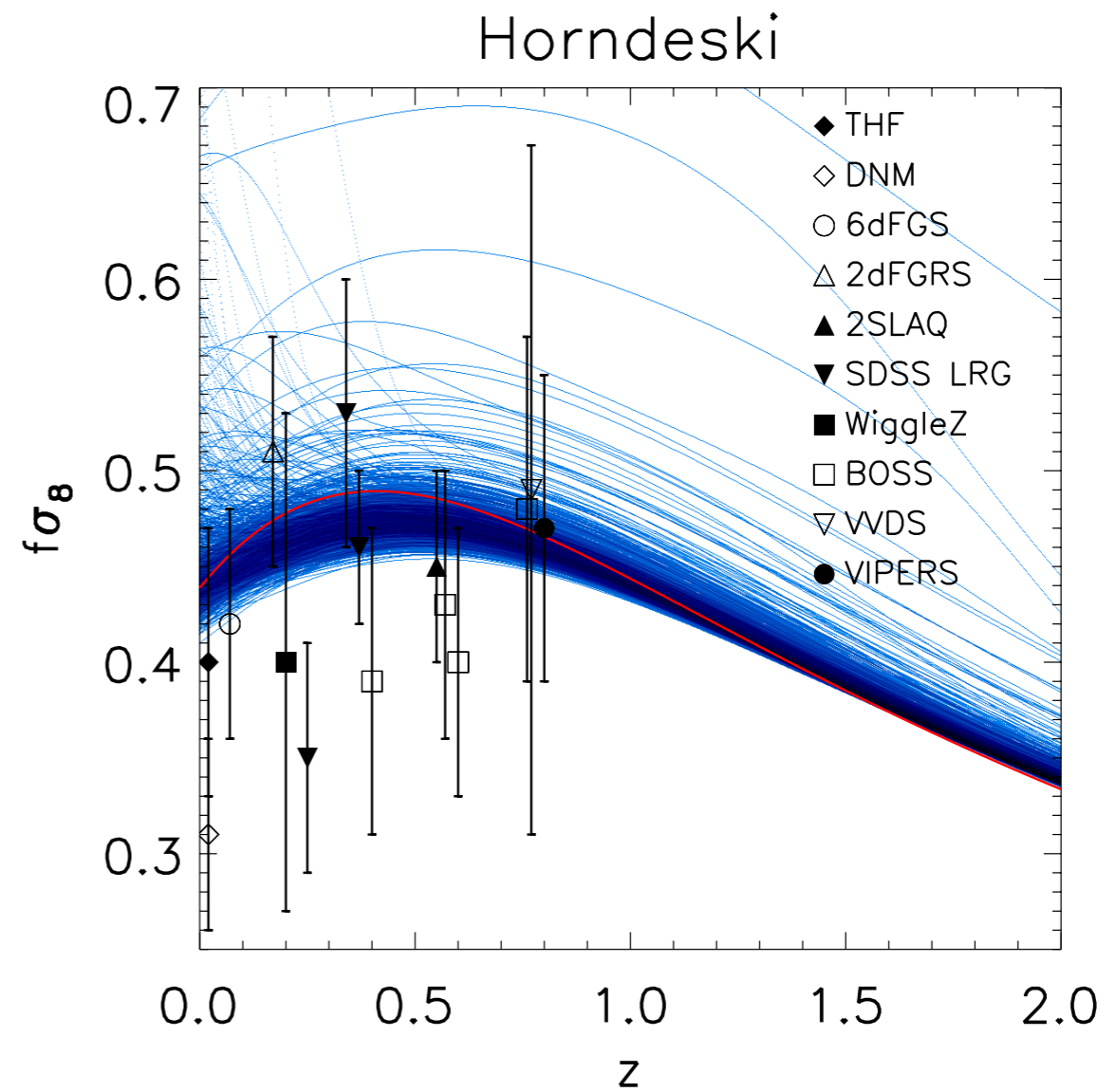
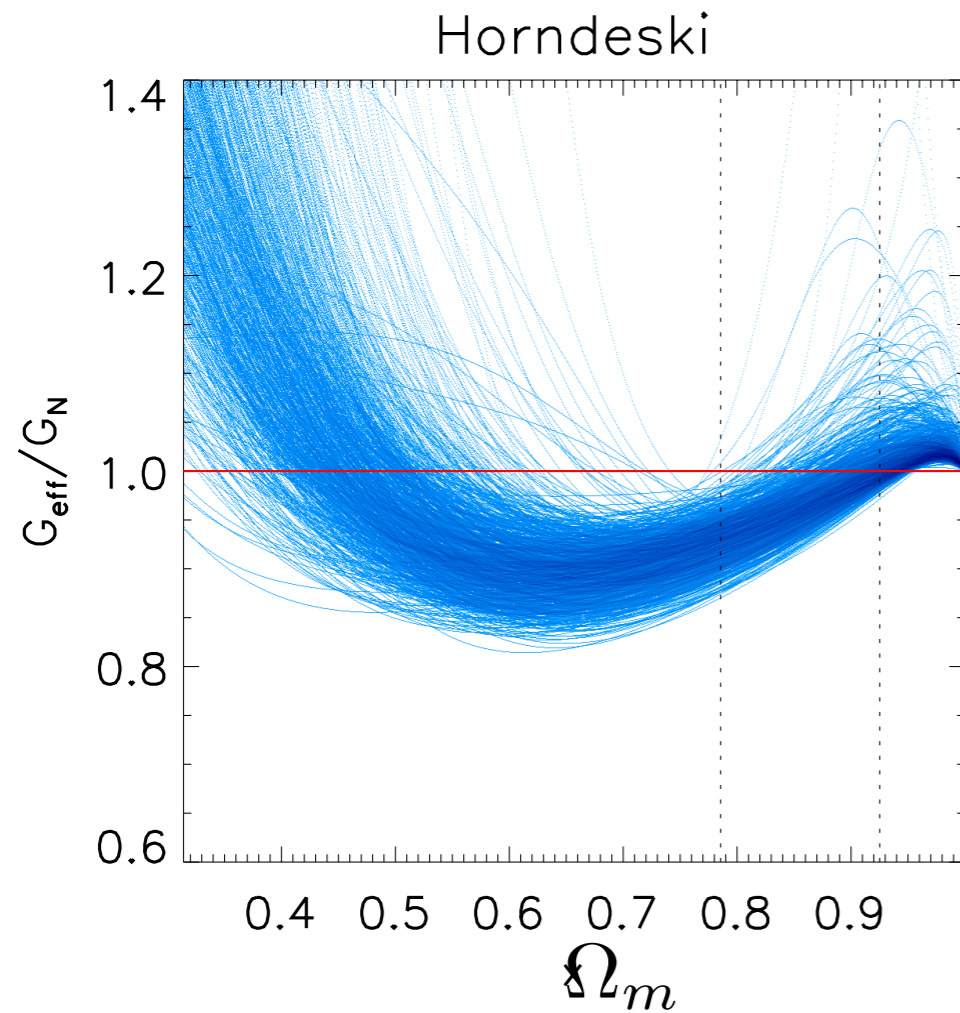
$$\& \ c_s^2 < 1$$

Option 2:

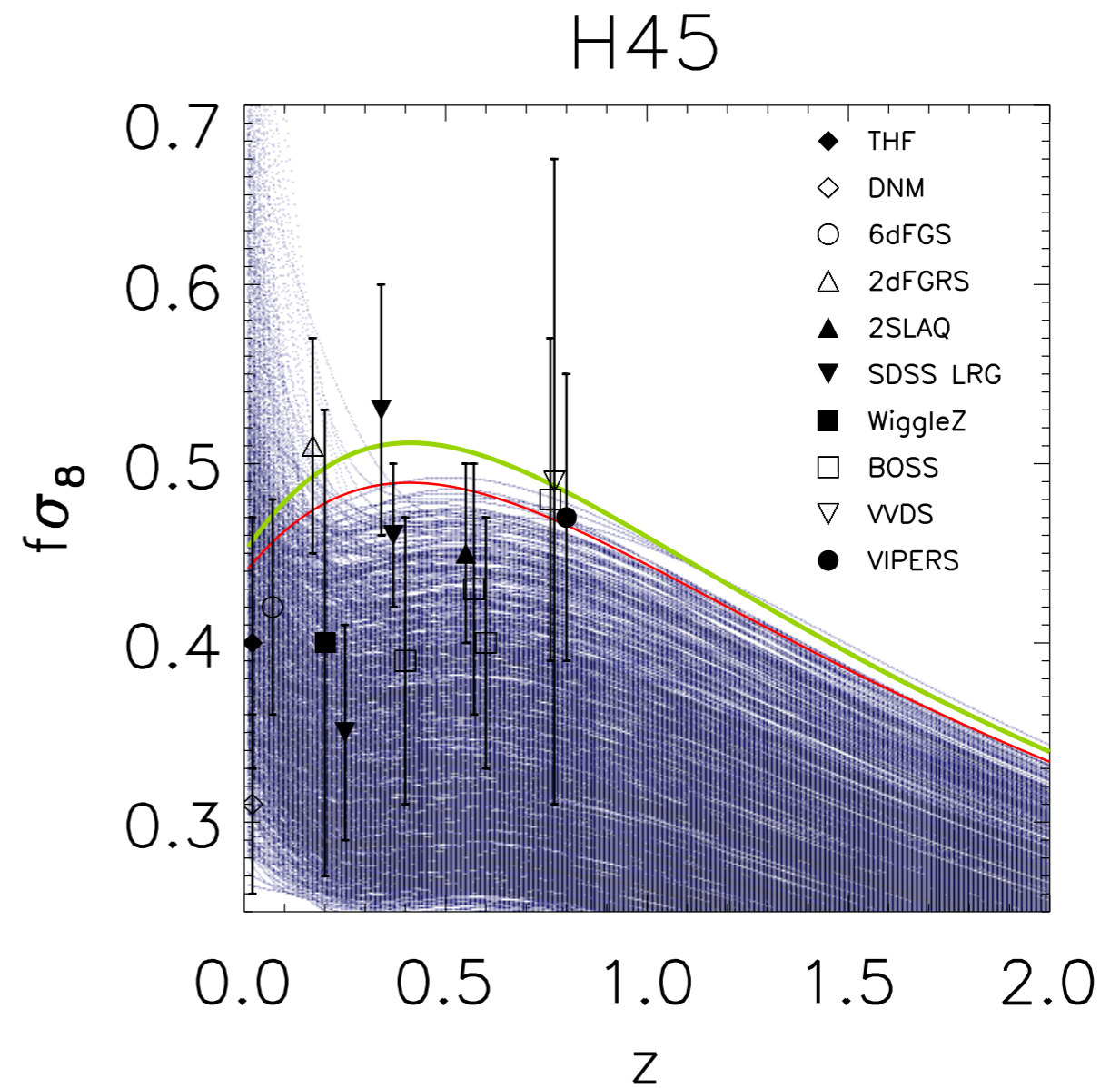
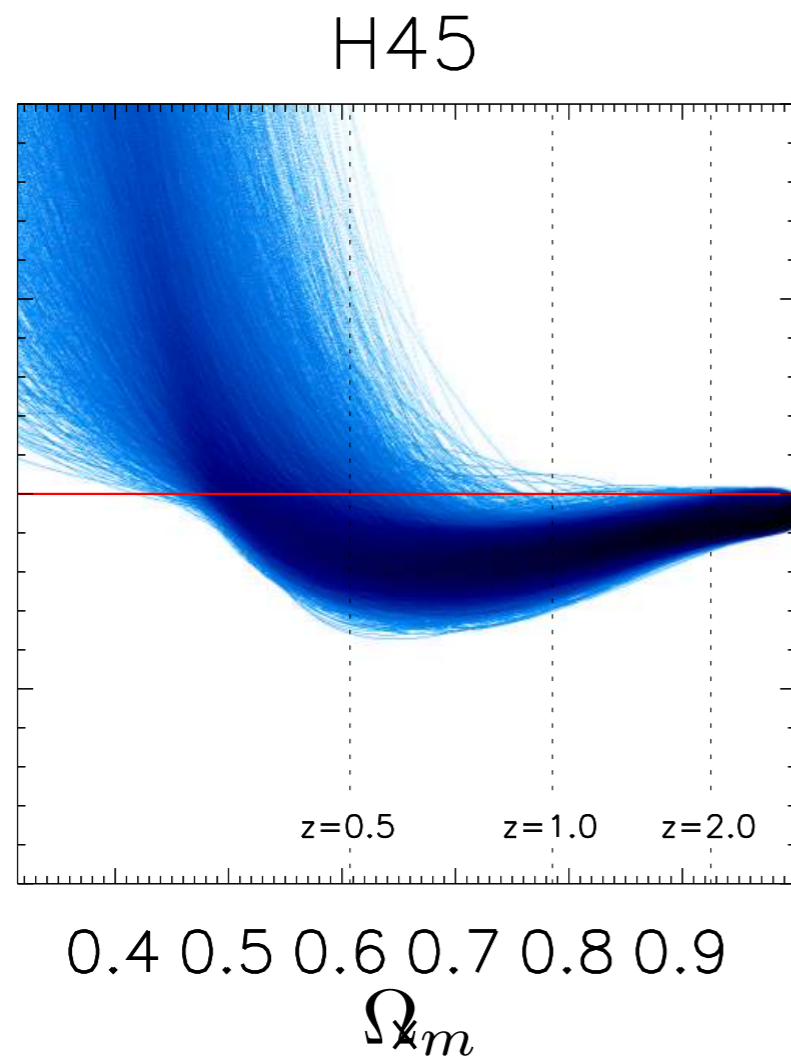
$$\& \ c_T^2 < 1$$

Stability requirements make a strong selection

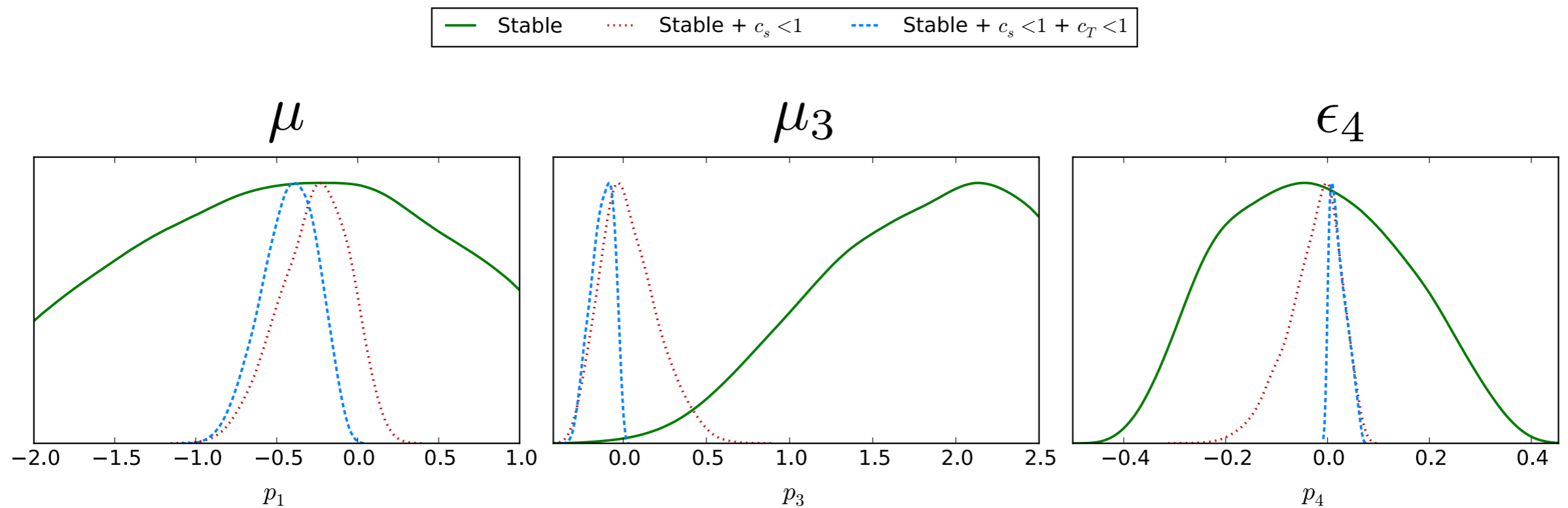
# Growth rate



# Growth rate (early DE)

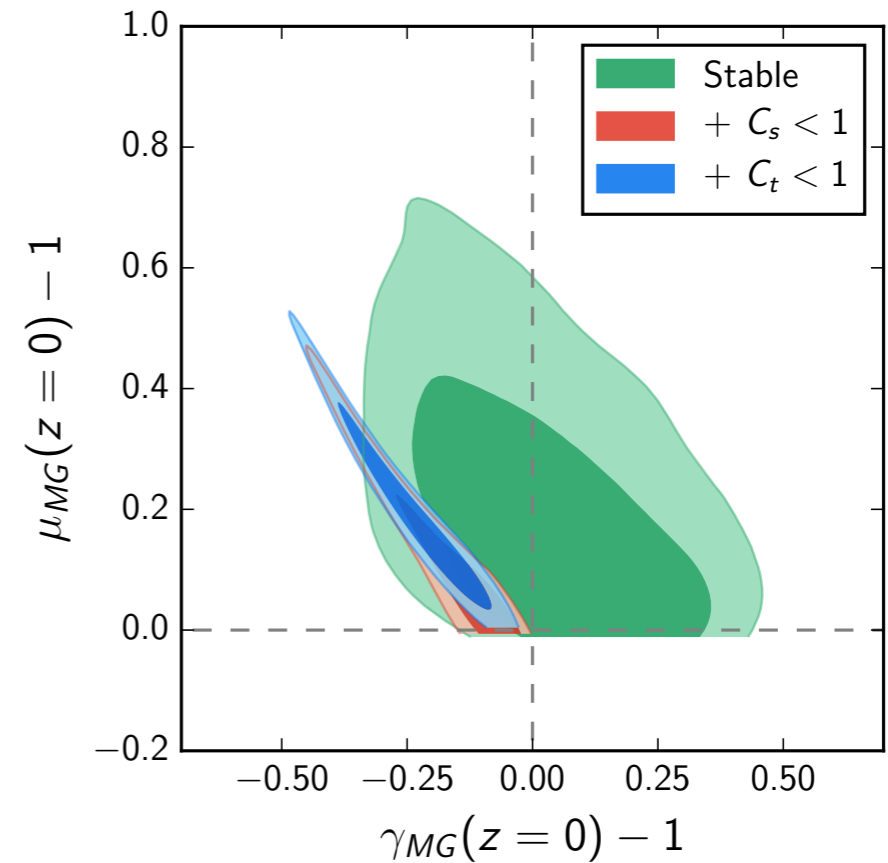
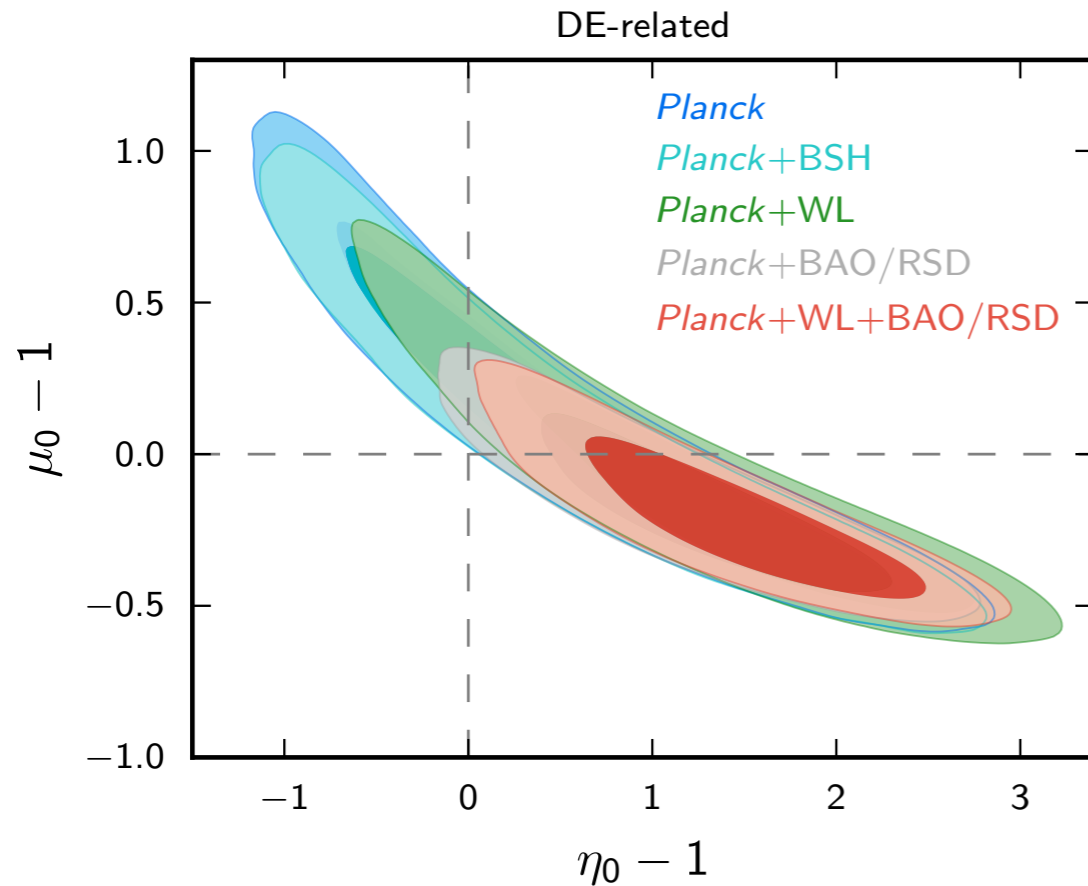


# Fitting Planck 2015 CMB data



Viability conditions play an important role in determining the posteriors

# Fitting Planck 2015 CMB data

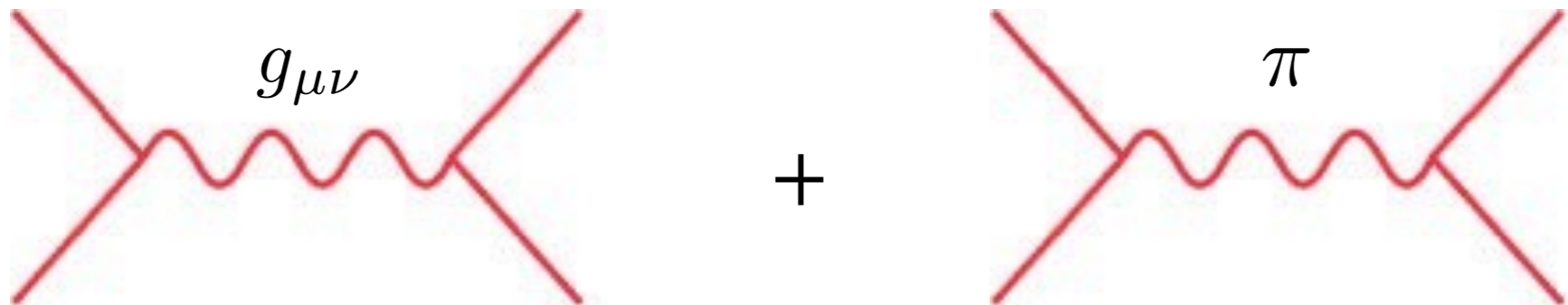


Ad-hoc parameterizations of  $G_{\text{eff}}$  do not correspond to actual stable theories...

CMB data alone do not show any preference for modified gravity

# Protecting solar system gravity with screening

$$\mathcal{L} = -\frac{M_*^2}{2} h_{\mu\nu} \mathcal{E}^{\mu\nu}_{\alpha\beta}[\phi_0] h^{\alpha\beta} - \mathcal{A}^{\mu\nu}[\phi_0] \partial_\mu \pi \partial_\nu \pi - \pi T + \frac{1}{2} h^{\mu\nu} T_{\mu\nu}$$

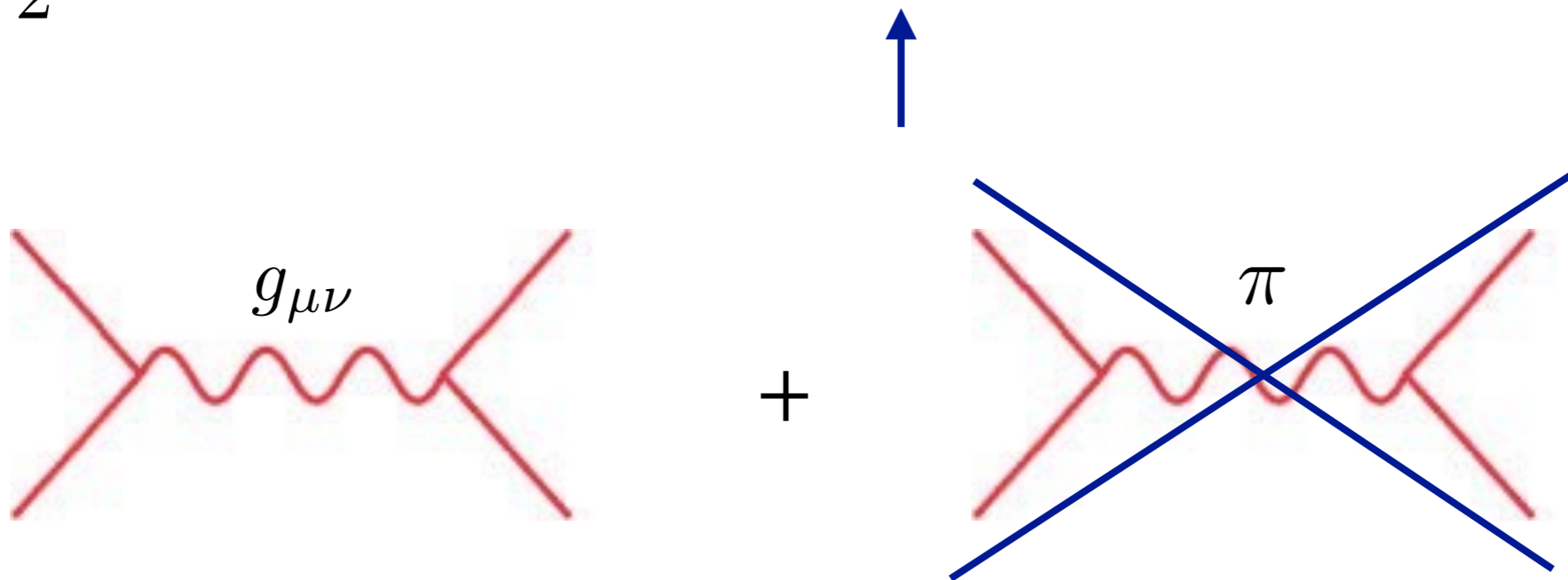


On cosmic scale the scalar contributes  $O(1)$

We need screening!

# Vainshtein screening

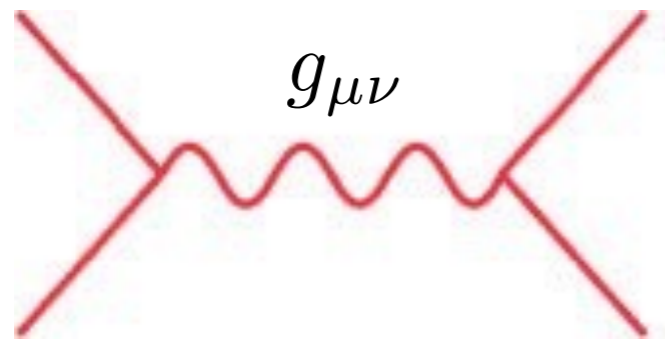
$$\mathcal{L} = -\frac{M_*^2}{2} h_{\mu\nu} \mathcal{E}^{\mu\nu}_{\alpha\beta}[\phi_0] h^{\alpha\beta} - \mathcal{A}^{\mu\nu}[\phi_0] \partial_\mu \pi \partial_\nu \pi - \pi T + \frac{1}{2} h^{\mu\nu} T_{\mu\nu}$$



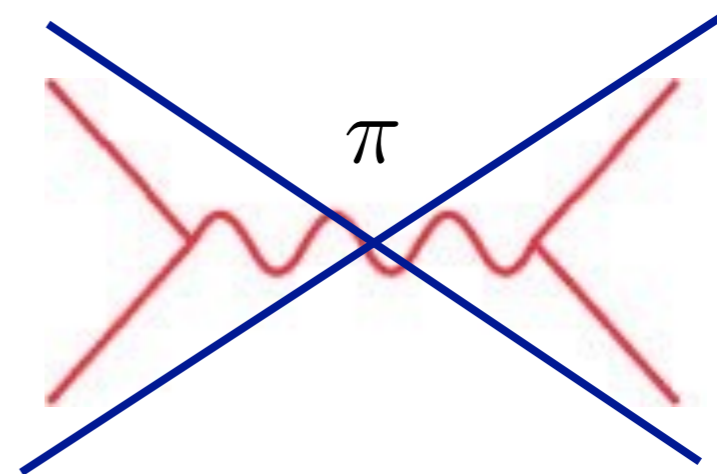
Vainshtein: non-linear effects suppress the scalar contribution

# Vainshtein screening

$$\mathcal{L} = -\frac{M_*^2}{2} h_{\mu\nu} \mathcal{E}_{\alpha\beta}^{\mu\nu}[\phi_0] h^{\alpha\beta} - \mathcal{A}^{\mu\nu}[\phi_0] \partial_\mu \pi \partial_\nu \pi - \pi T + \frac{1}{2} h^{\mu\nu} T_{\mu\nu}$$



+



Vainshtein: non-linear effects suppress the scalar contribution

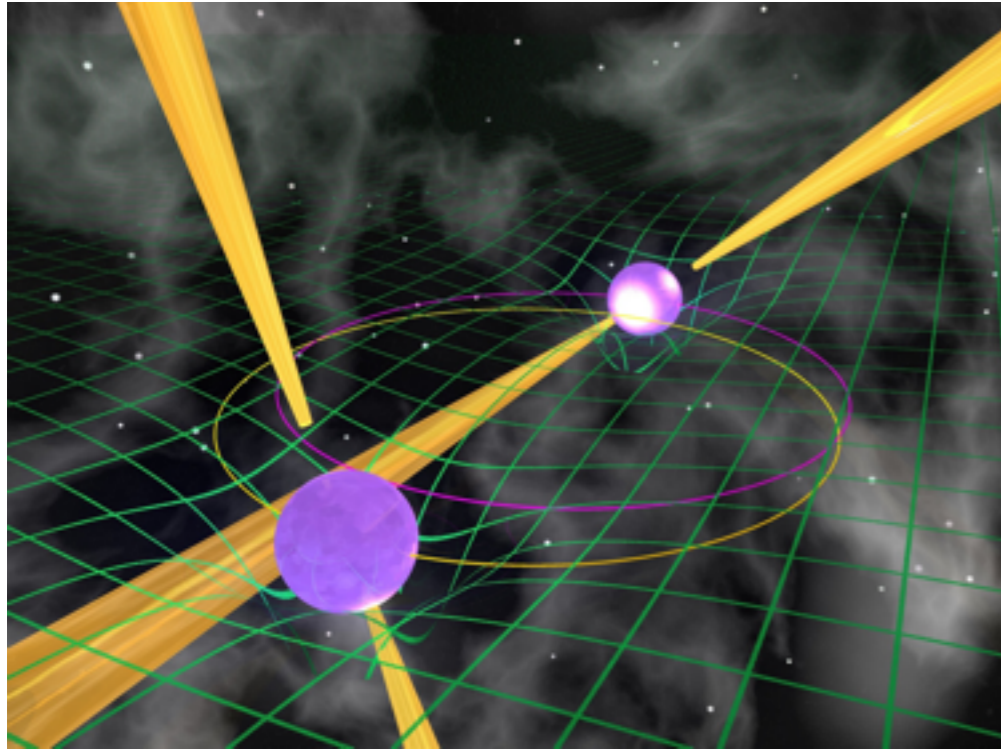
However: there can be modifications in the pure-graviton sector.  
This are, generally, unscreanable!

Babichev, Deffayet, Esposito-Farese 2012

Beltran, F.P., Velten, 2015

# Gravitational wave speed (as in heaven as on hearth)

J. Beltran, F.P., H. Velten, 2015

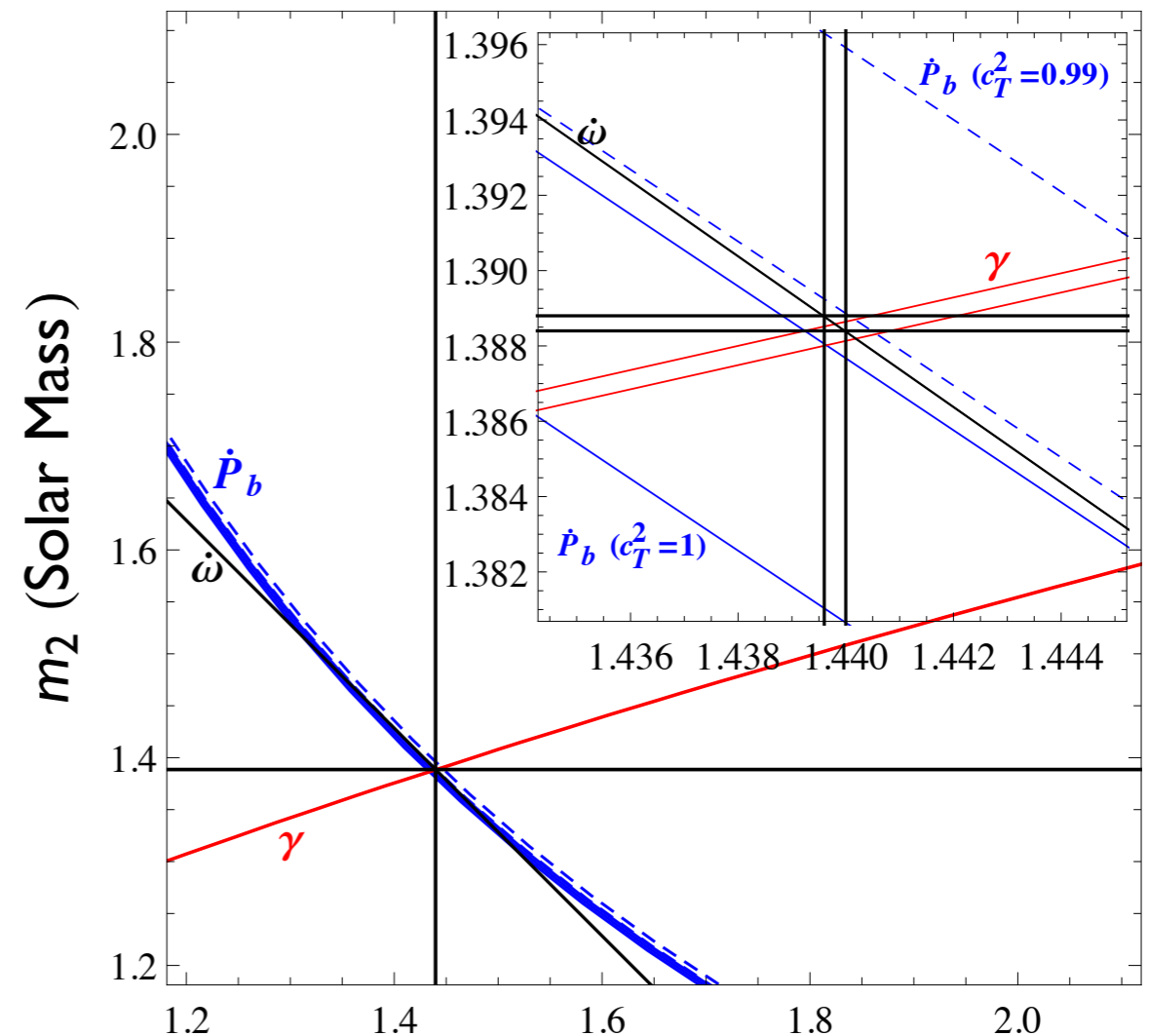


Hulse-Taylor  
binary pulsars

$$c_T^2 = \frac{1}{1 + \epsilon_4}$$

$$\epsilon_4 \lesssim 10^{-2}$$

See also Blas, Sanctuary 2011



# Gravitational wave speed (as in heaven as on earth)

J. Beltran, F.P., H. Velten, 2015

LES

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Statistical and Quantum  
Information, etc.

Astrophysics

Fields and Fields

and Optical Physics

ics, Fluid Dynamics,  
etc.

n Physics

er: Structure, etc.

er: Electronic Properties,

atter, Biological, and  
Physics

## Gravitation and Astrophysics

### Evading the Vainshtein Mechanism with Anomalous Gravitational Wave Speed: Constraints on Modified Gravity from Binary Pulsars

Jose Beltrán Jiménez, Federico Piazza, and Hermano Velten

Phys. Rev. Lett. **116**, 061101 (2016) – Published 9 February 2016

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Featured in Physics

Editors' Suggestion

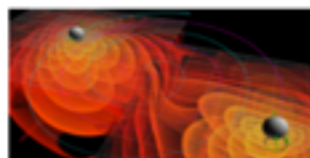
PDF

HTML

### Observation of Gravitational Waves from a Binary Black Hole Merger

B. P. Abbott *et al.* (LIGO Scientific Collaboration and Virgo Collaboration)

Phys. Rev. Lett. **116**, 061102 (2016) – Published 11 February 2016



Gravitational waves emitted by the merger of two black holes  
have been detected, setting the course for a new era of  
observational astrophysics.

[Show Abstract](#)

The condition MG's condition is in...



$$G_N \sim \frac{1}{8\pi M^2(t_0)[1 + \epsilon_4(t_0)]^2}$$

$$\frac{\dot{G}_N}{G_N} < 0.02H_0 \quad (\text{Lunar Laser Ranging})$$

self-acceleration

$$H^2 = \frac{1}{3M^2(t)} [\rho_m(t) + \rho_{DE}(t)]$$
A blue curved arrow originates from the word 'self-acceleration' and points to the '1' in the numerator of the fraction in the Friedmann equation.

# Final remarks

- EFT of DE powerful unifying framework
- Loads of new data from future Galaxy surveys
- Lot of data-fitting work ahead of us

Either

or...

Tension persisting and  
eased by MG

